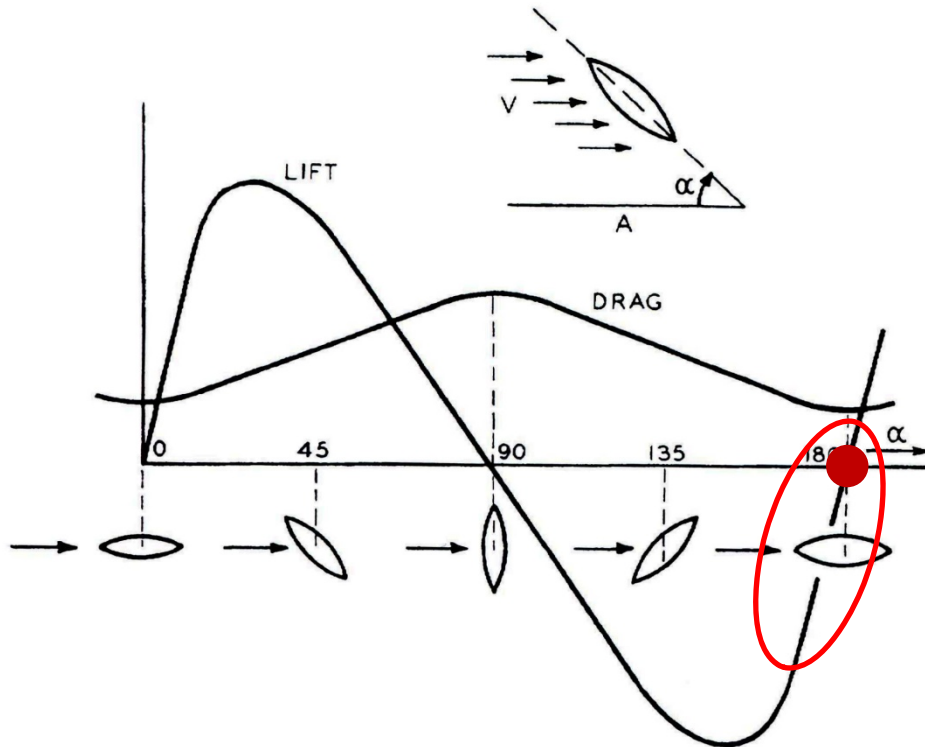
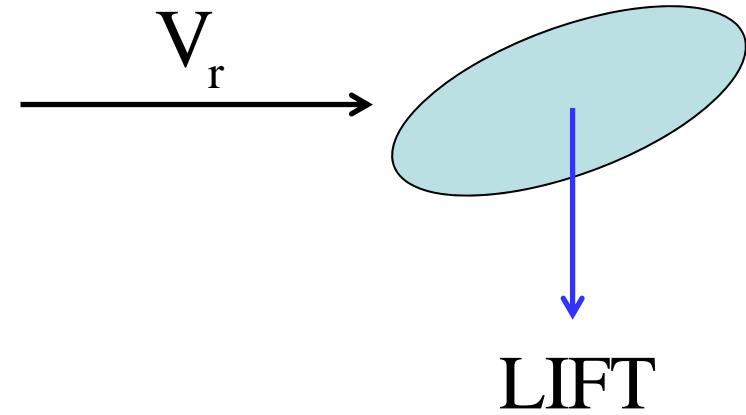
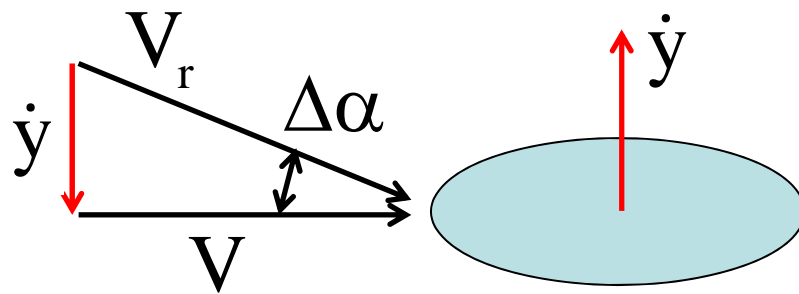
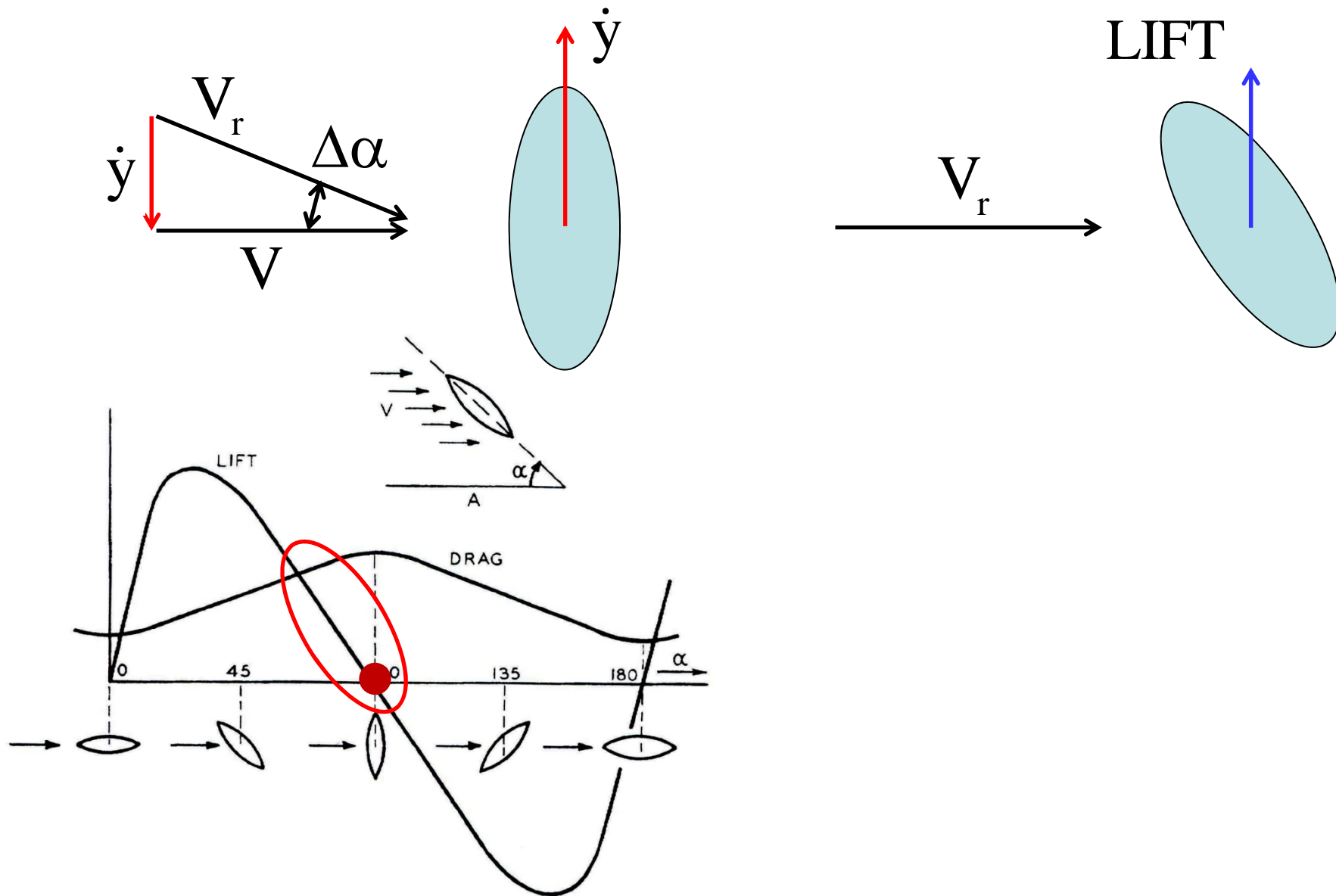


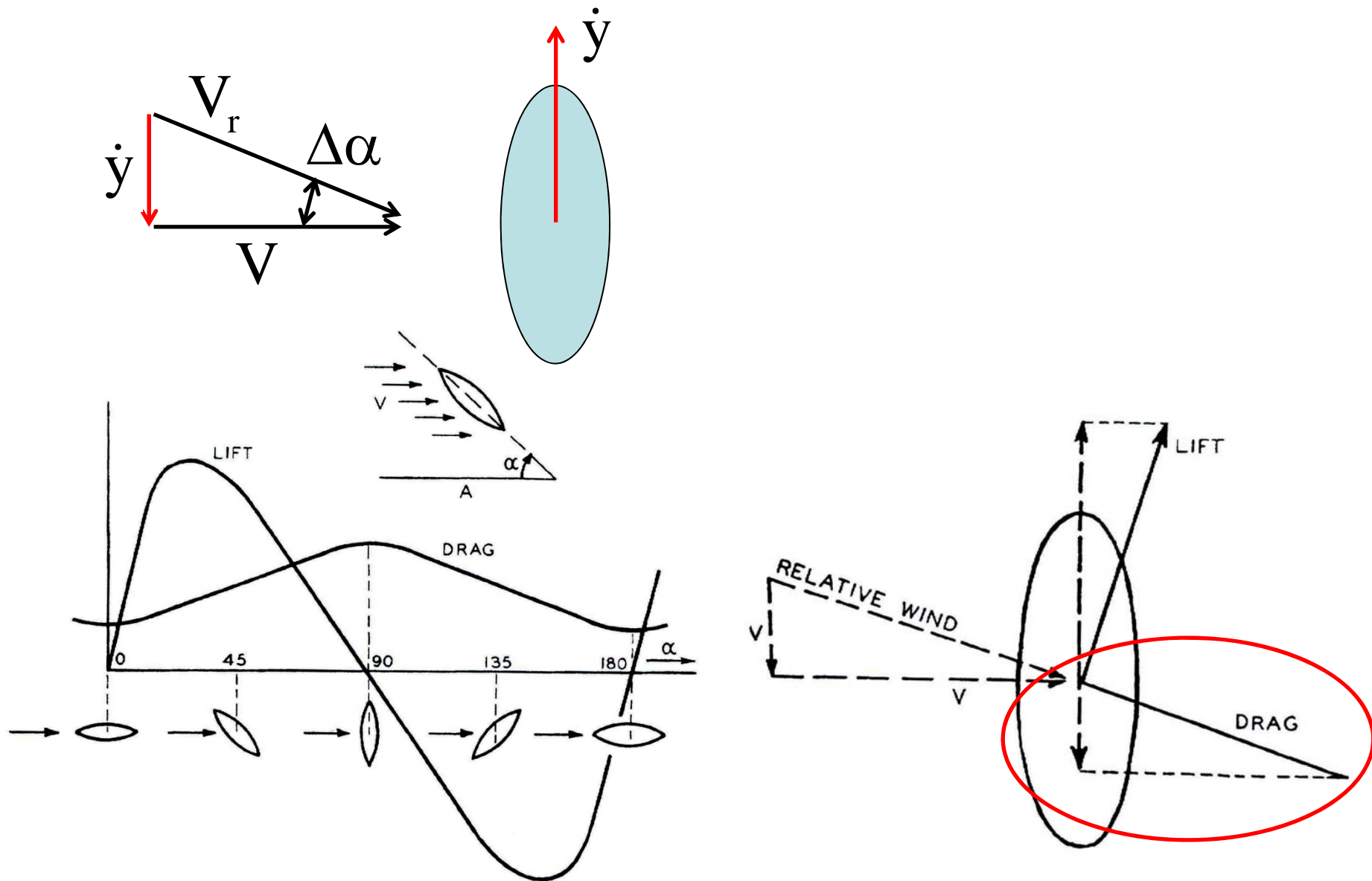
**Crosswind galloping**



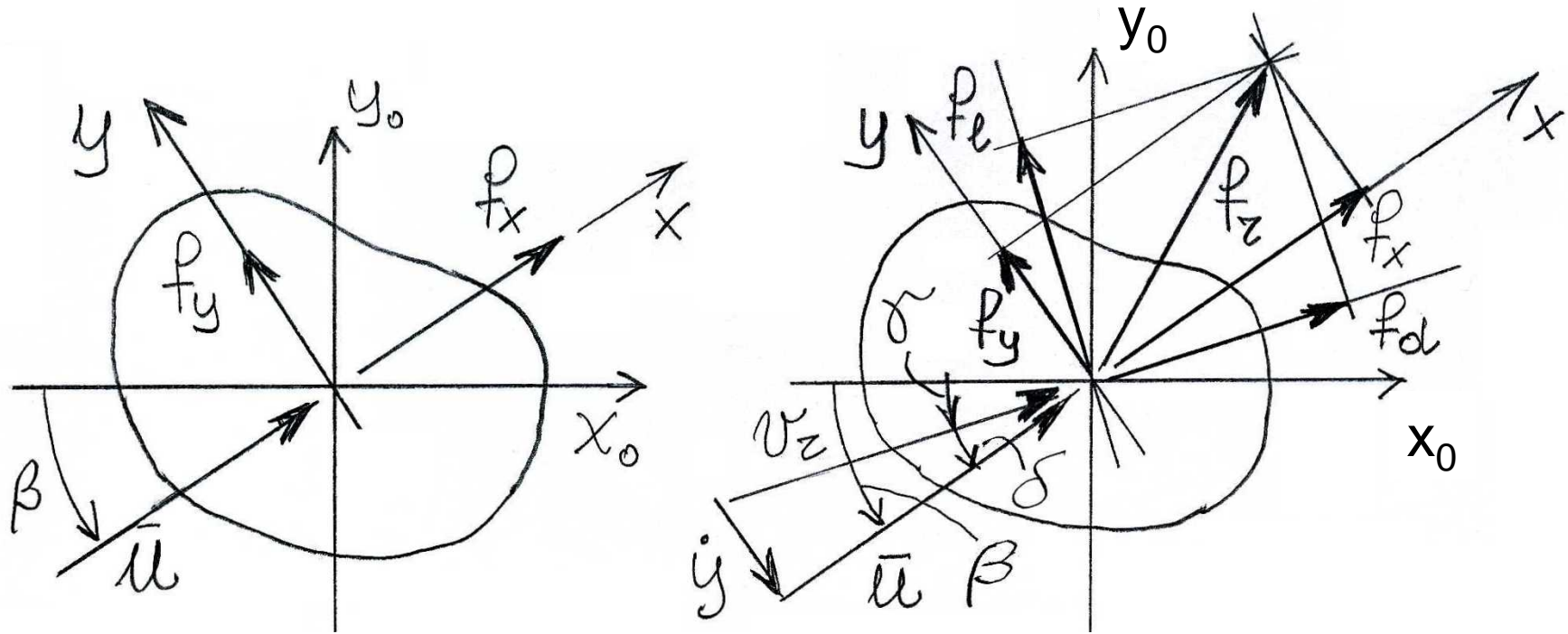
**Crosswind galloping**



Crosswind galloping



Crosswind galloping

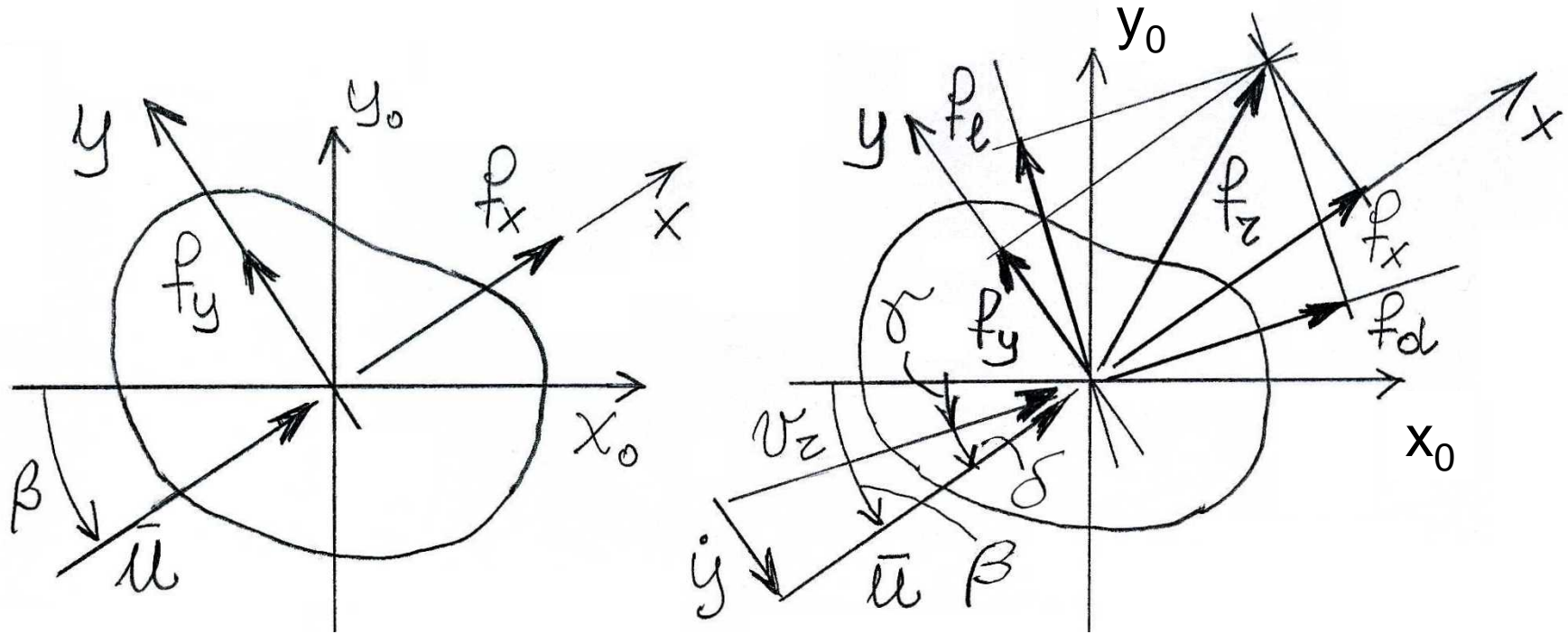


$$f_x = \frac{1}{2} \rho \bar{u}^2 b c_d(\beta); \quad f_y = \frac{1}{2} \rho \bar{u}^2 b c_l(\beta)$$

Quasi – steady theory

$$f_d = \frac{1}{2} \rho v_r^2 b c_d(\gamma); \quad f_l = \frac{1}{2} \rho v_r^2 b c_l(\gamma) \Rightarrow$$

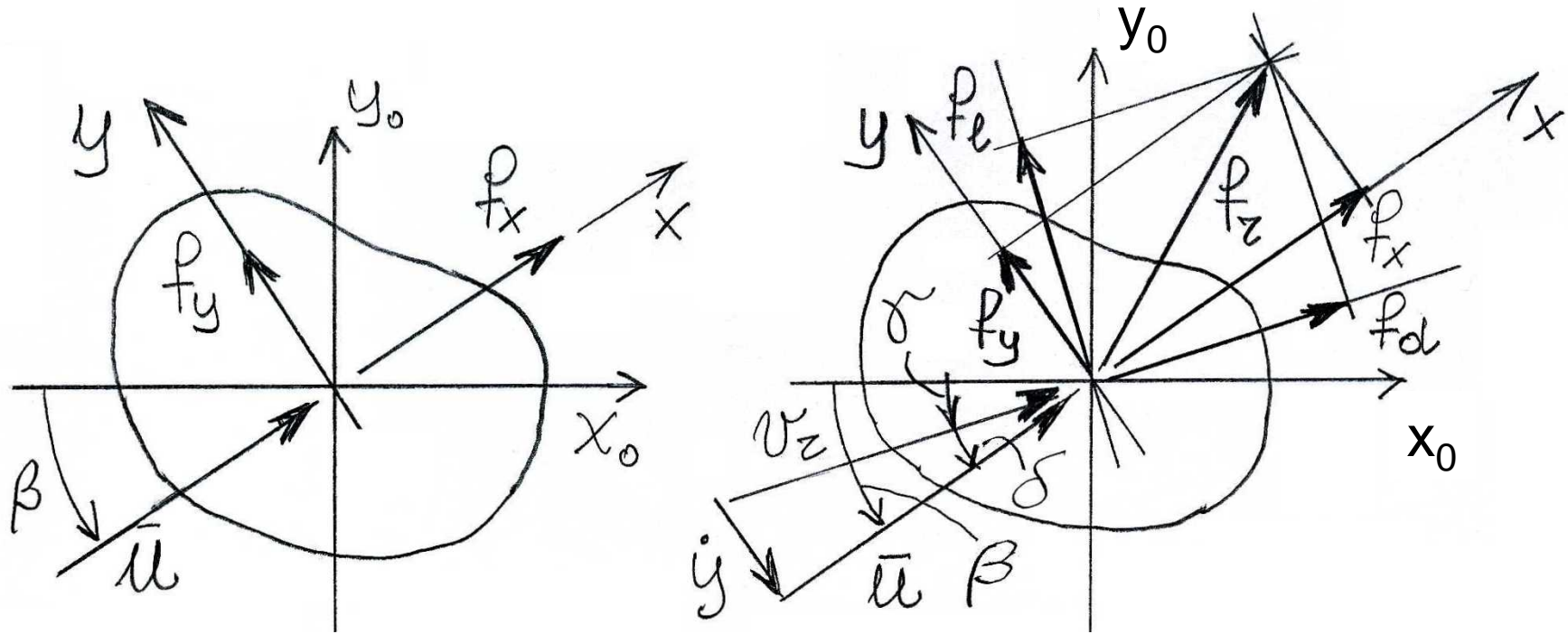
$$f_y = -f_d \sin \delta + f_l \cos \delta = \frac{1}{2} \rho v_r^2 b [-c_d(\gamma) \sin \delta + c_l(\gamma) \cos \delta]$$



$$f_y = -f_d \sin \delta + f_l \cos \delta = \frac{1}{2} \rho v_r^2 b [-c_d(\gamma) \sin \delta + c_l(\gamma) \cos \delta]$$

$$\gamma = \beta - \delta; \quad \delta = \arctg \frac{\dot{y}}{\bar{u}}; \quad v_r = \frac{\bar{u}}{\cos \delta} \Rightarrow$$

$$f_y = \frac{1}{2} \rho \bar{u}^2 b \frac{1}{\cos^2 \delta} [-c_d(\beta - \delta) \sin \delta + c_l(\beta - \delta) \cos \delta]$$



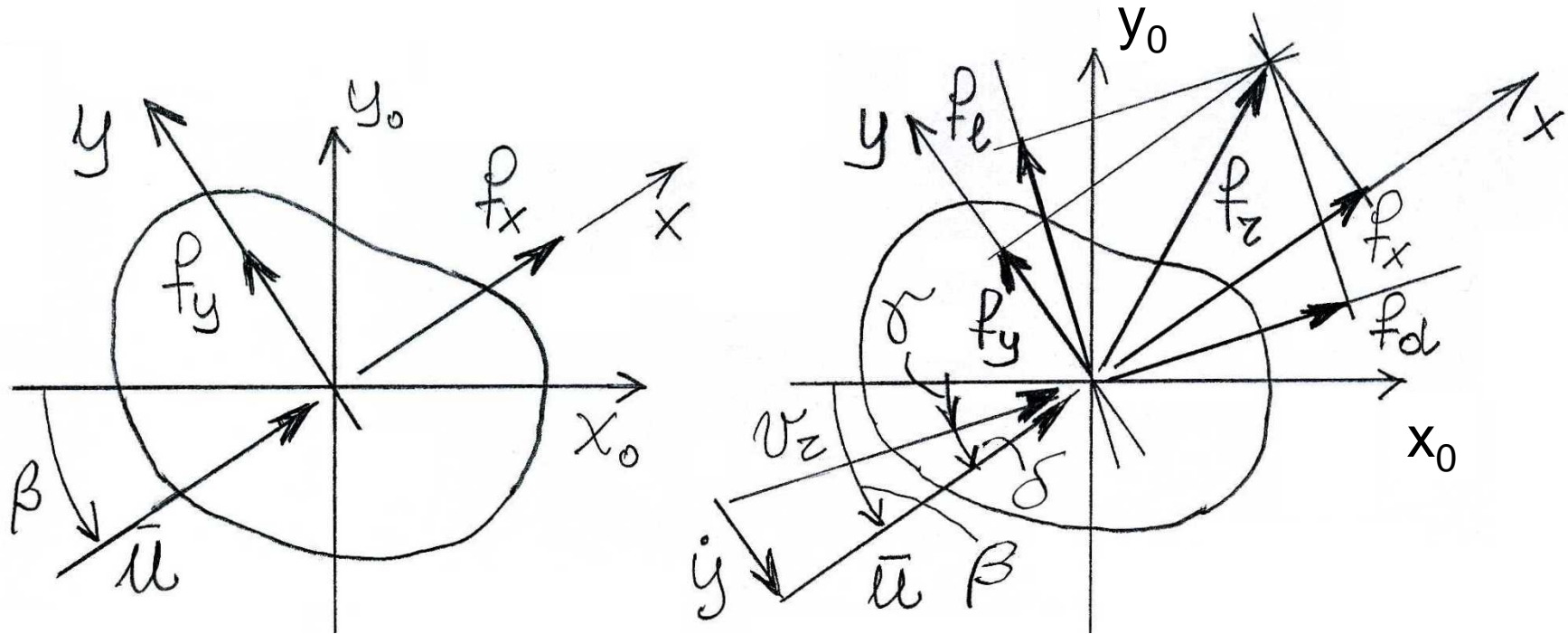
$$f_y = \frac{1}{2} \rho \bar{u}^2 b \frac{1}{\cos^2 \delta} [-c_d (\beta - \delta) \sin \delta + c_l (\beta - \delta) \cos \delta]$$

**Rotation of reference axis:**  $\beta = 0 \Rightarrow$

$$f_y = \frac{1}{2} \rho \bar{u}^2 b \frac{1}{\cos \delta} [-c_d (-\delta) \tan \delta + c_l (-\delta)] = \frac{1}{2} \delta \bar{u}^2 b c_{fy}$$

$$c_{fy} = \frac{1}{\cos \delta} [-c_d (-\delta) \tan \delta + c_l (-\delta)] = \sum_k \frac{1}{k!} \left. \frac{\partial^k c_{fy}(\delta)}{\partial \delta^k} \right|_{\delta=0} \cdot \delta^k$$





$$f_y = \frac{1}{2} \delta \bar{u}^2 b c_{fy} ; \quad c_{fy} = \sum_k \frac{1}{k!} \left. \frac{\partial^k c_{fy}(\delta)}{\partial \delta^k} \right|_{\delta=0} \cdot \delta^k$$

**Linearized analysis** ( $k = 0, 1$ )  $\Rightarrow$  **Incipient instability**

$$c_{fy} = c_1 - (c_d + c'_1) \frac{\dot{y}}{\bar{u}} \quad (c_d = c_d|_{\delta=0} ; c_1 = c_1|_{\delta=0})$$

**Galloping coefficient**

$$a_G = -(c_d + c'_1) \Rightarrow c_{fy} = c_1 + a_G \frac{\dot{y}}{\bar{u}}$$



$$f_y = \frac{1}{2} \delta \bar{u}^2 b c_{fy} ; \quad c_{fy} = c_1 + a_G \frac{\dot{y}}{\bar{u}}$$

**SDOF Equation of motion** (per unit length)

$$\ddot{y} + 2\xi_s \omega_0 \dot{y} + \omega_0^2 y = \frac{1}{m} f_y = \frac{1}{m} \frac{1}{2} \rho \bar{u}^2 b c_{fy} = \frac{1}{m} \frac{1}{2} \rho \bar{u}^2 b c_1 + \frac{1}{m} \frac{1}{2} \rho \bar{u}^2 b a_G \frac{\dot{y}}{\bar{u}} \Rightarrow$$

$$\ddot{y} + \left( 2\xi_s \omega_0 - \frac{1}{m} \frac{1}{2} \rho \bar{u}^2 b a_G \frac{1}{\bar{u}} \right) \dot{y} + \omega_0^2 y = \frac{1}{m} \frac{1}{2} \rho \bar{u}^2 b c_1 \Rightarrow$$

$$\ddot{y} + 2(\xi_s + \xi_a) \omega_0 \dot{y} + \omega_0^2 y = \frac{1}{m} \frac{1}{2} \rho \bar{u}^2 b c_1$$

**Crosswind aerodynamic damping**

$$\xi_a = -\frac{\rho \bar{u} b a_G}{4m\omega_0} = \frac{\rho \bar{u} b (c_d + c'_1)}{4m\omega_0}$$

**Total crosswind damping**

$$\xi_t = \xi_s + \xi_a = \xi_s - \frac{\rho \bar{u} b a_G}{4m\omega_0} = \xi_s + \frac{\rho \bar{u} b (c_d + c'_1)}{4m\omega_0}$$

$$\ddot{y} + 2\xi_t \omega_0 \dot{y} + \omega_0^2 y = \frac{1}{m} \frac{1}{2} \rho \bar{u}^2 b c_1$$

$$\xi_t = \xi_s + \xi_a = \xi_s - \frac{\rho \bar{u} b a_G}{4m\omega_0} = \xi_s + \frac{\rho \bar{u} b (c_d + c'_1)}{4m\omega_0}$$

**GALLOPING necessary condition**

**Glauert – Den Hartog criterion**

$$\xi_a < 0 \Rightarrow a_G > 0 \text{ or } (c_d + c'_1) < 0$$

**GALLOPING necessary and sufficient condition**

$$\xi_t \leq 0 \Rightarrow \xi_s - \frac{\rho \bar{u} b a_G}{4m\omega_0} = \xi_s + \frac{\rho \bar{u} b (c_d + c'_1)}{4m\omega_0} \leq 0$$

## GALLOPING necessary and sufficient condition

$$\xi_t \leq 0 \Rightarrow \xi_s - \frac{\rho \bar{u} b a_G}{4m\omega_0} = \xi_s + \frac{\rho \bar{u} b (c_d + c'_1)}{4m\omega_0} \leq 0 \Rightarrow$$

$$\bar{u} \geq \frac{4m\omega_0 \xi_s}{\rho b a_G} = - \frac{4m\omega_0 \xi_s}{\rho b (c_d + c'_1)}$$

being  $a_G > 0$ ,  $(c_d + c'_1) < 0$

## GALLOPING critical velocity

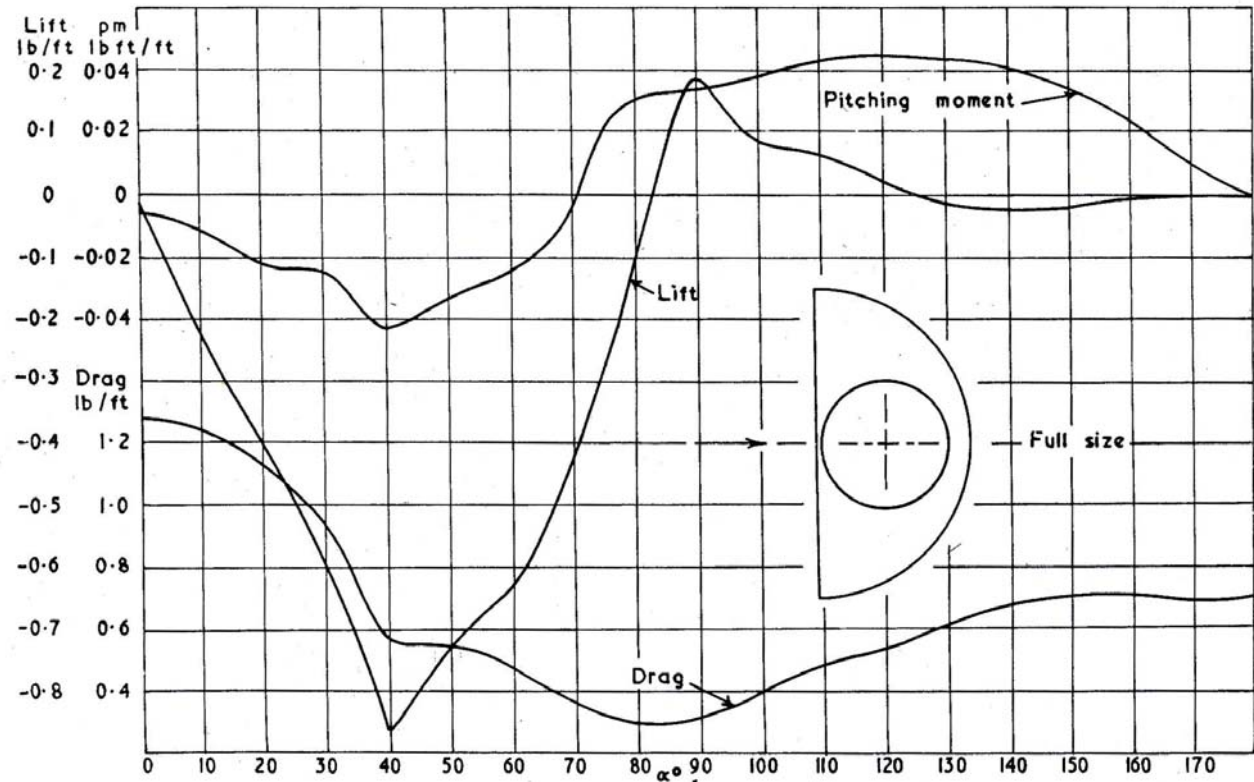
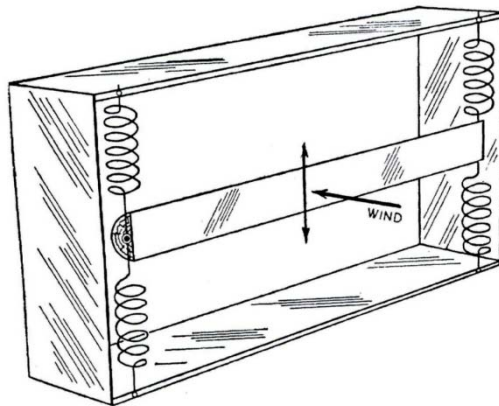
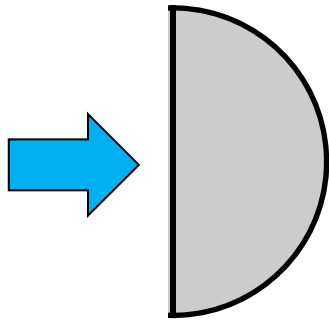
$$\bar{u}_{cr} = \frac{4m\omega_0 \xi_s}{\rho b a_G} = - \frac{4m\omega_0 \xi_s}{\rho b (c_d + c'_1)} \Rightarrow$$

$$\bar{u}_{cr} = \frac{4m\omega_0 \xi_s}{\rho b a_G} \cdot \frac{\pi b}{\pi b} = \frac{\omega_0 b}{\pi a_G} \cdot \frac{4\pi m \xi_s}{\rho b^2} = \frac{\omega_0 b}{\pi a_G} \cdot Sc = \frac{2n_0 b}{a_G} \cdot Sc$$

$$Sc = \frac{4\pi m \xi_s}{\rho b^2}$$

## Necessary condition

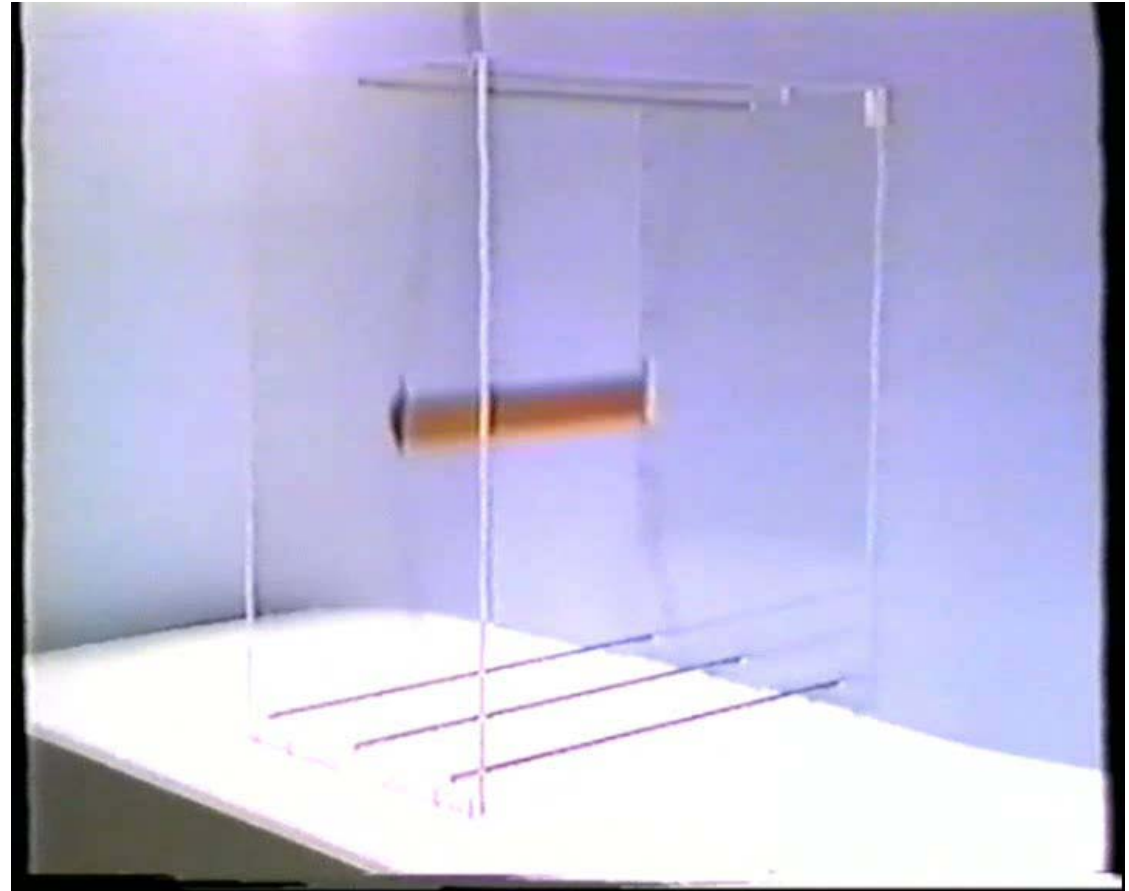
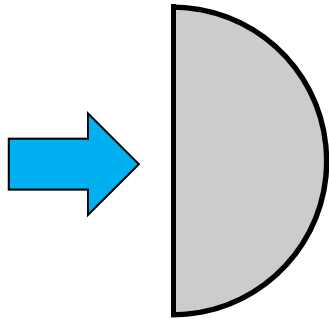
$$c_d + c'_1 < 0$$



D-shaped section

Necessary condition

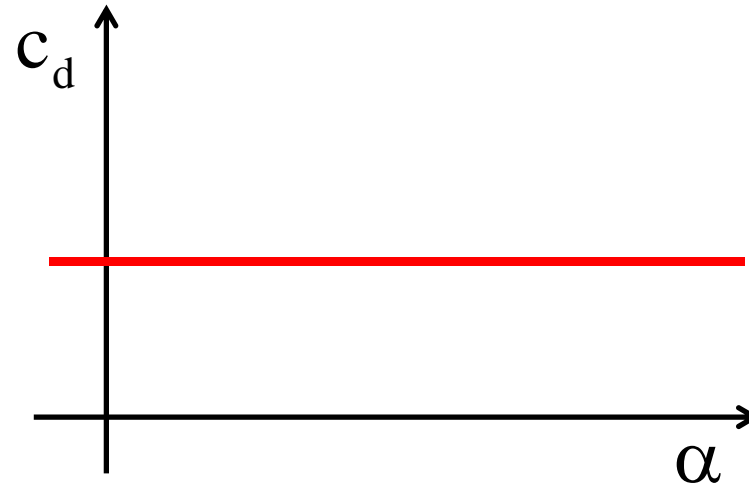
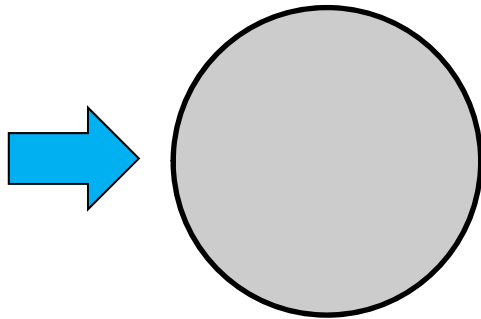
$$c_d + c'_1 < 0$$



D-shaped section

Necessary condition

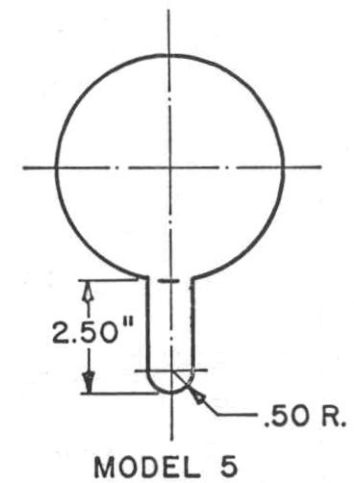
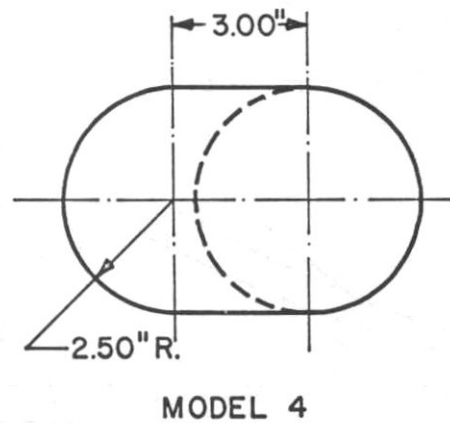
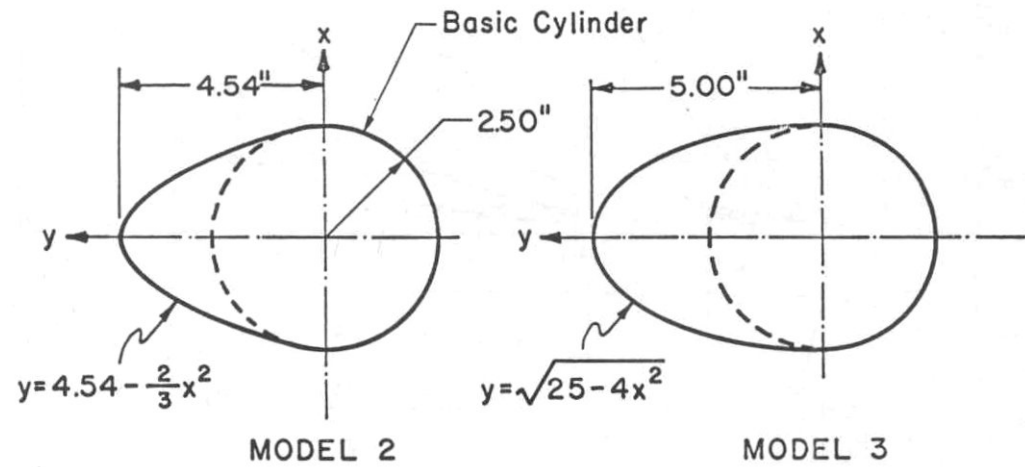
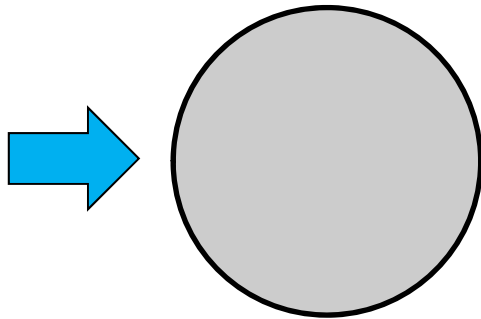
$$c_d + c'_1 < 0$$



Circular section

Necessary condition

$$c_d + c'_1 < 0$$



Iced cable section

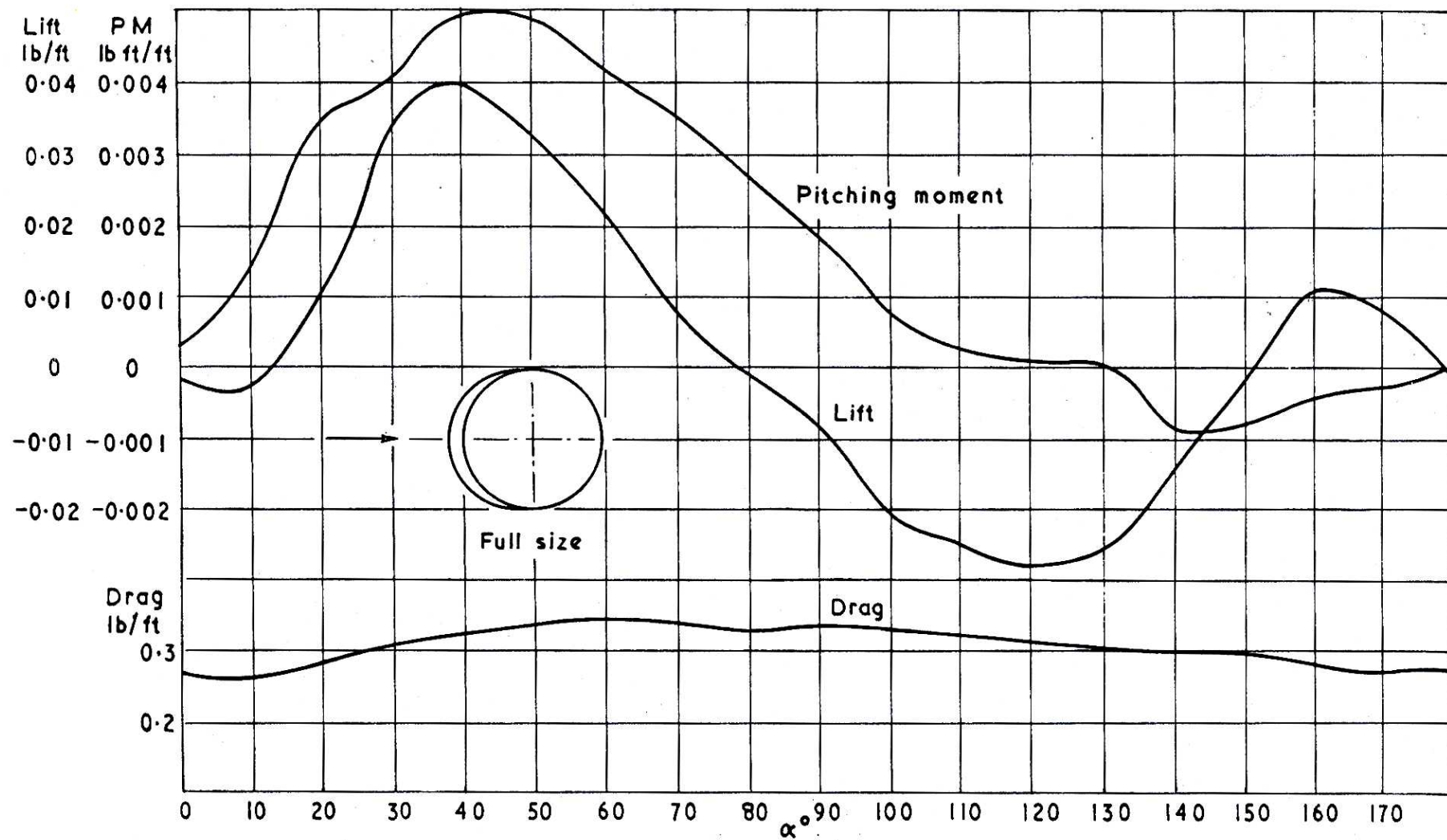




Iced cables

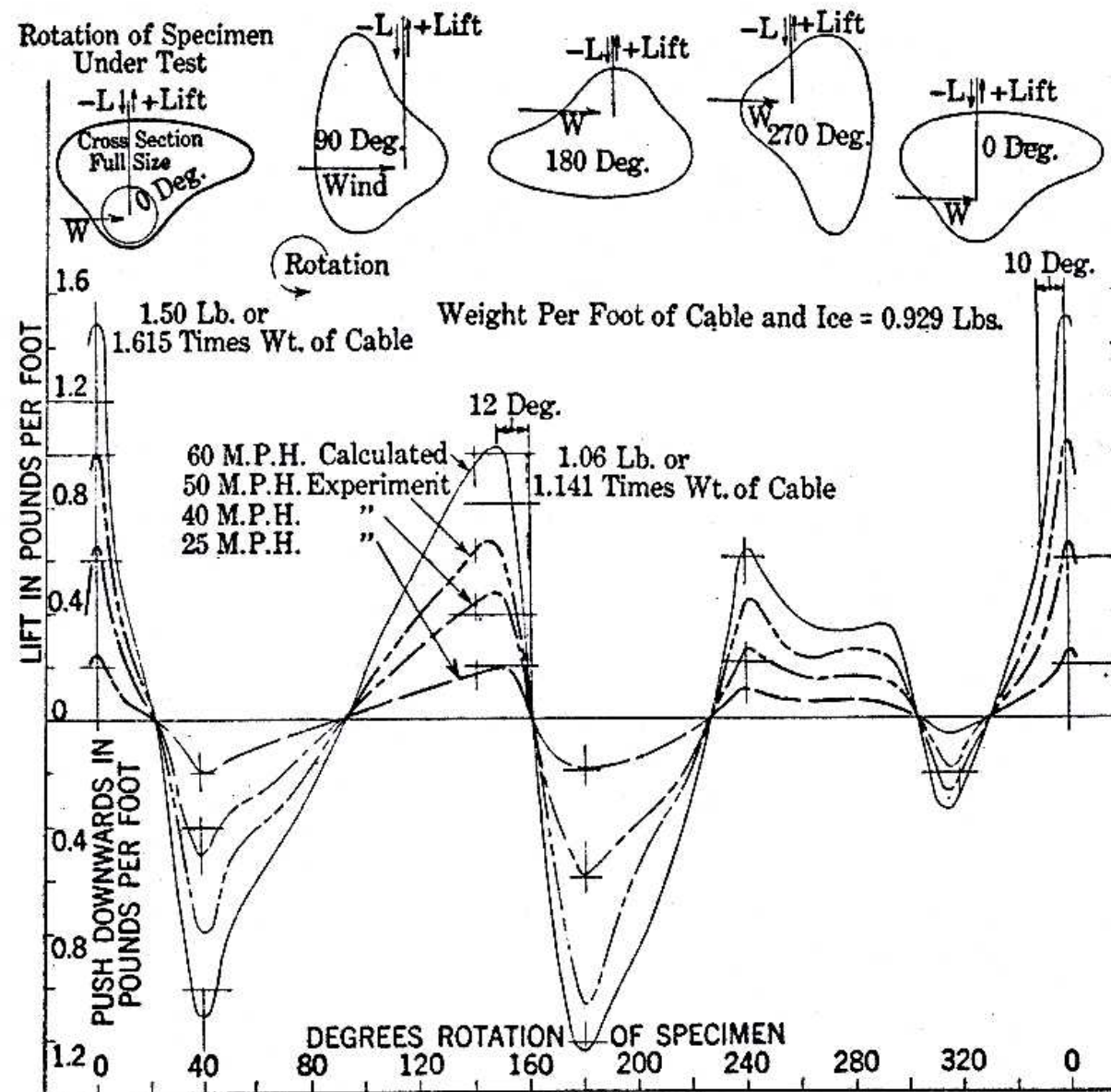


Iced cables



Iced cables





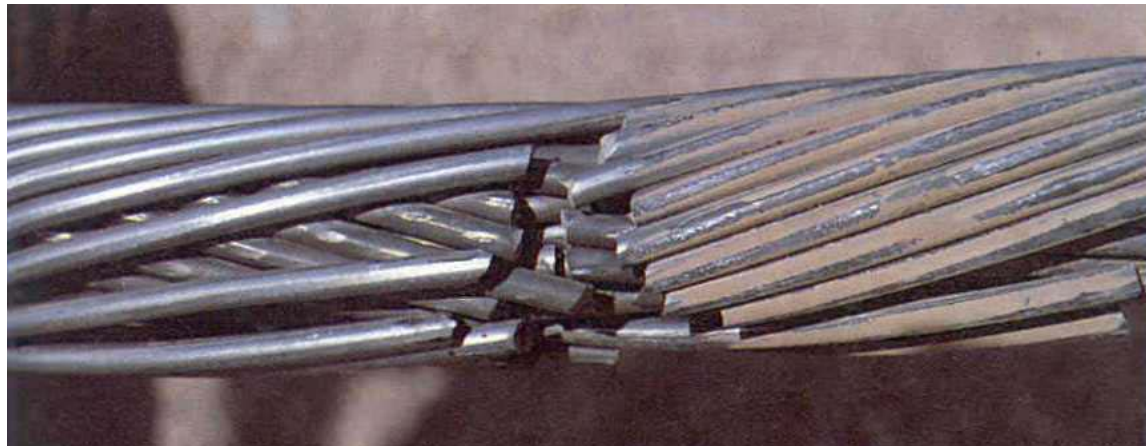
Iced cables



Conductor galloping



Conductor galloping



Fatigue collapse of conductors

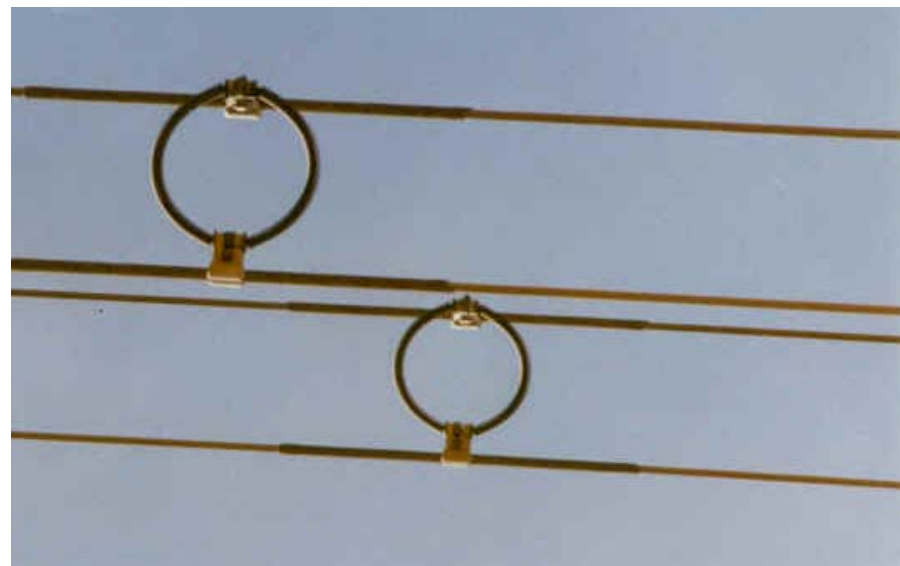


Collapse of towers for transmission lines

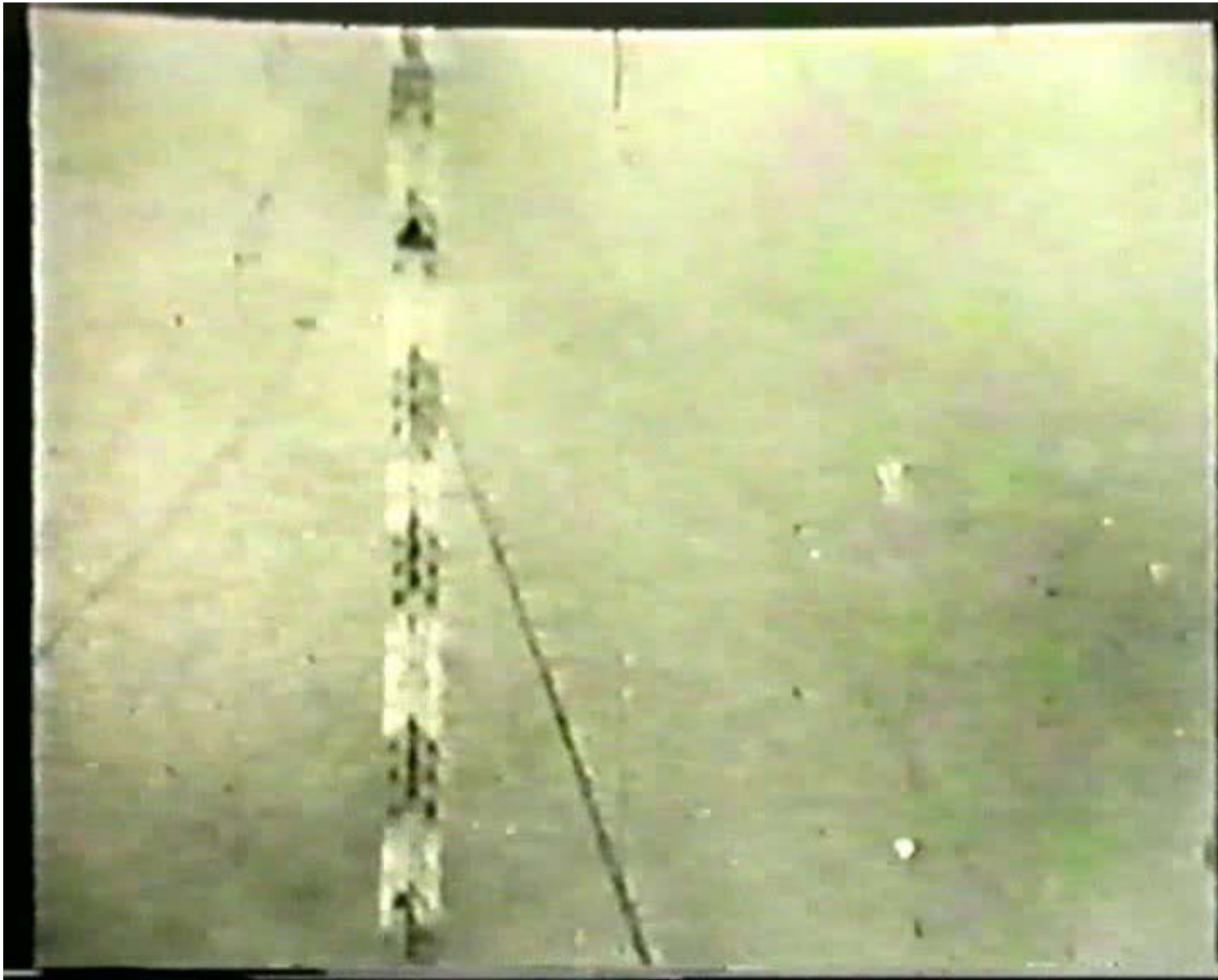




Collapse of towers for transmission lines



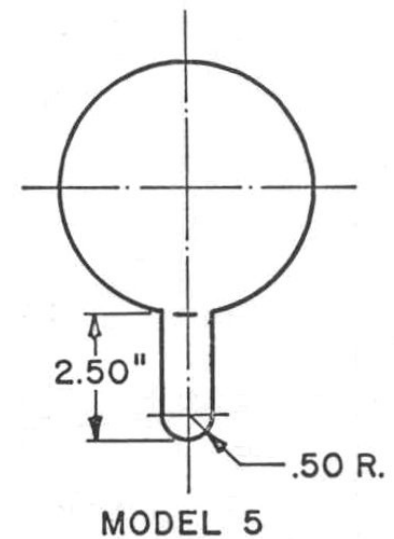
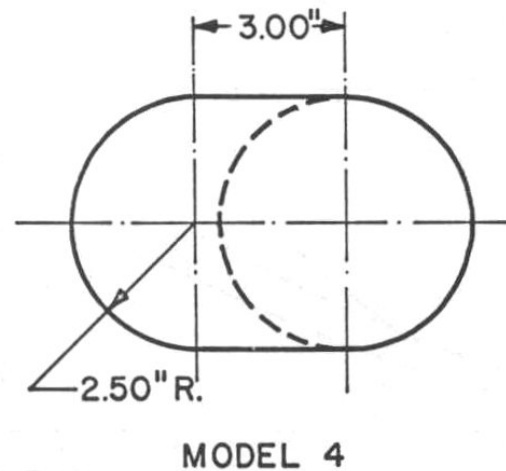
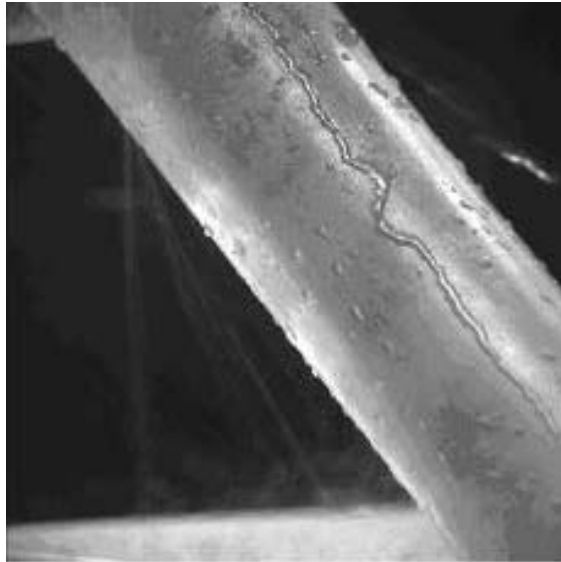
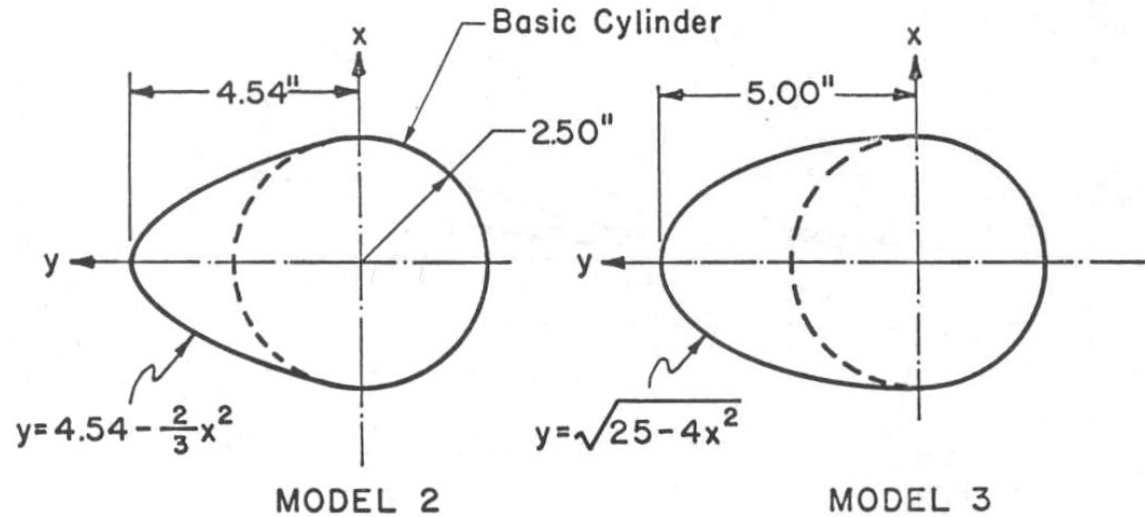
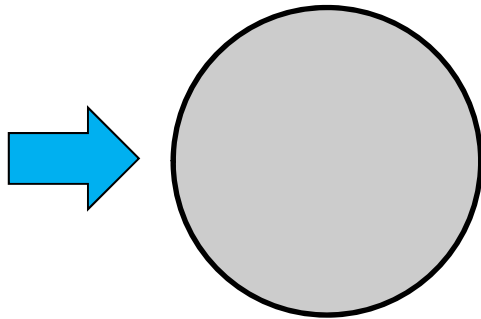
Devises to contrats galloping vibrations of transmission lines



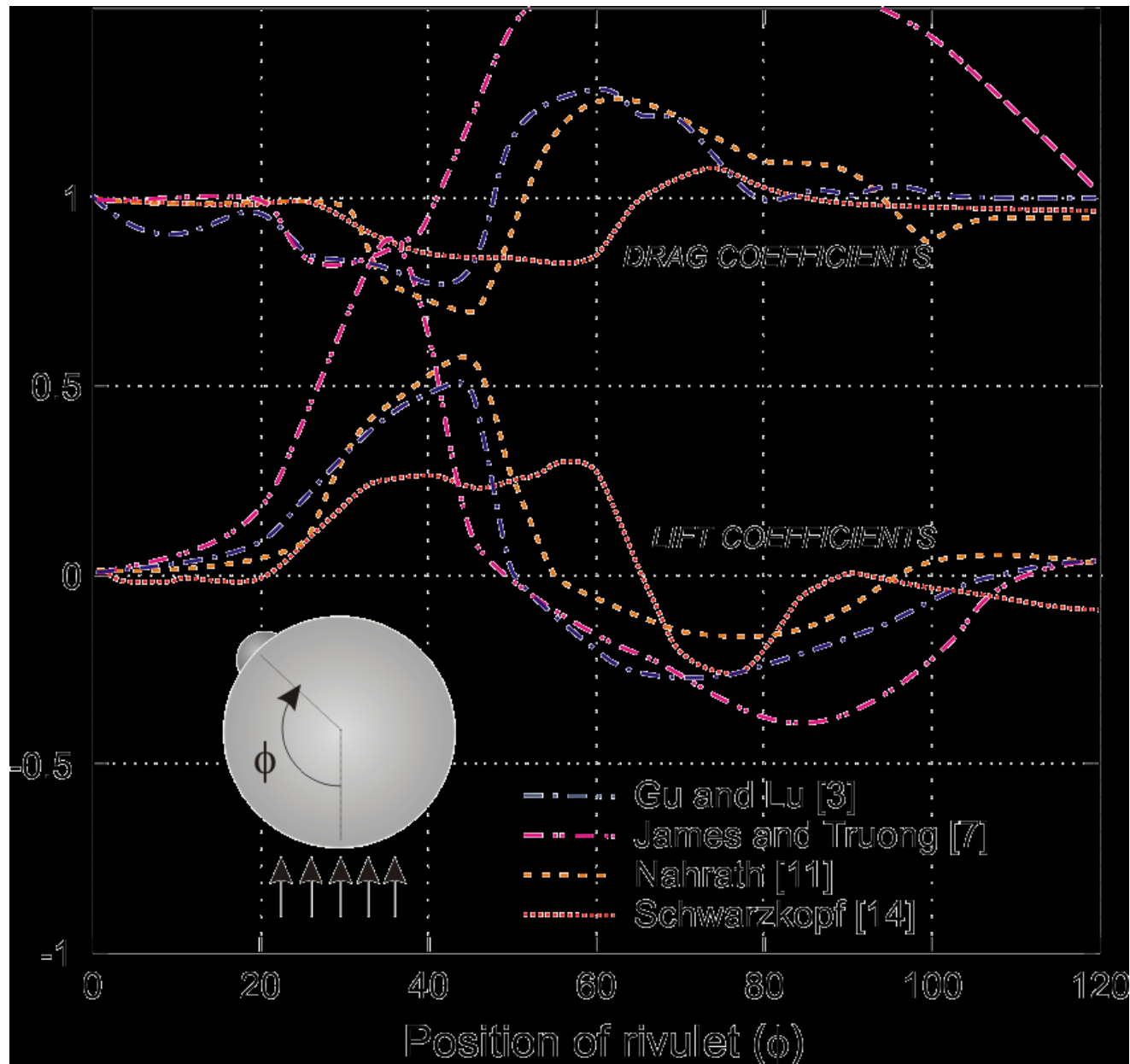
Cable galloping

## Necessary condition

$$c_d + c'_1 < 0$$



Water rivulet over cables



Water rivulet over cables



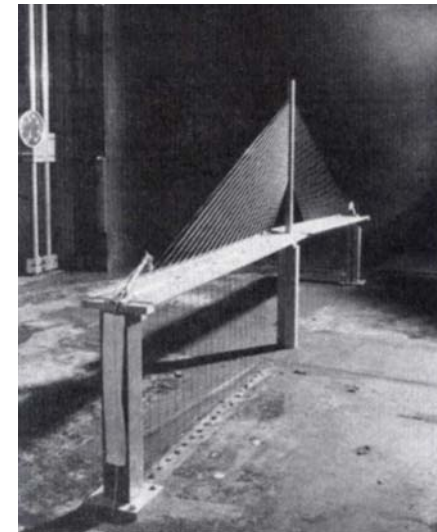
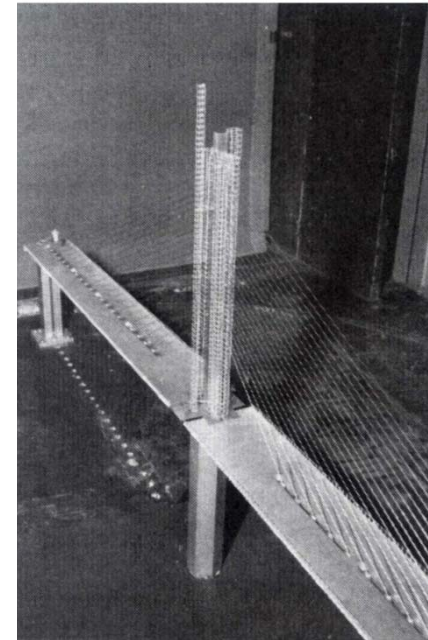
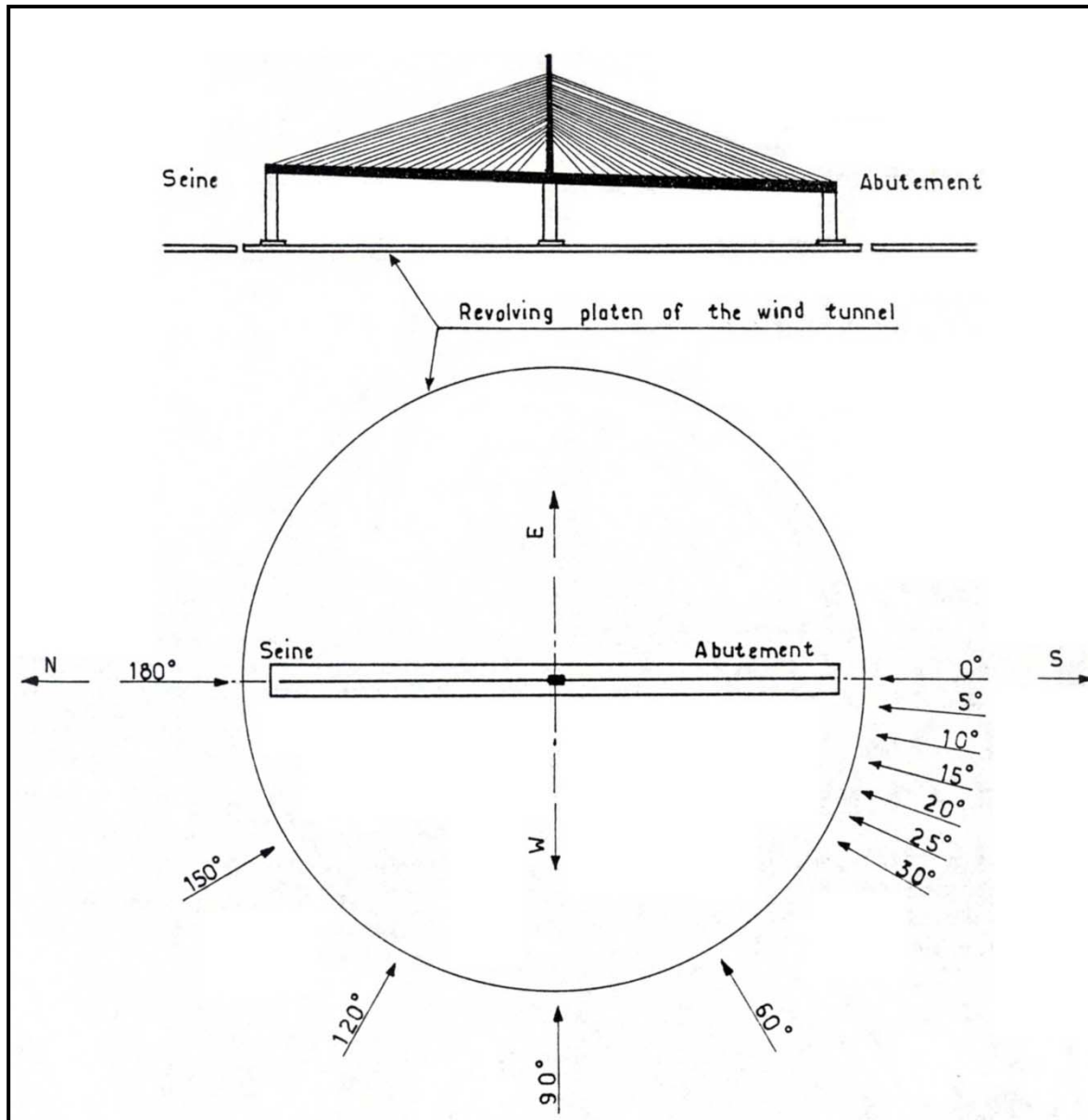


Brotonne Bridge, France, 1977



Brotonne Bridge, France, 1977

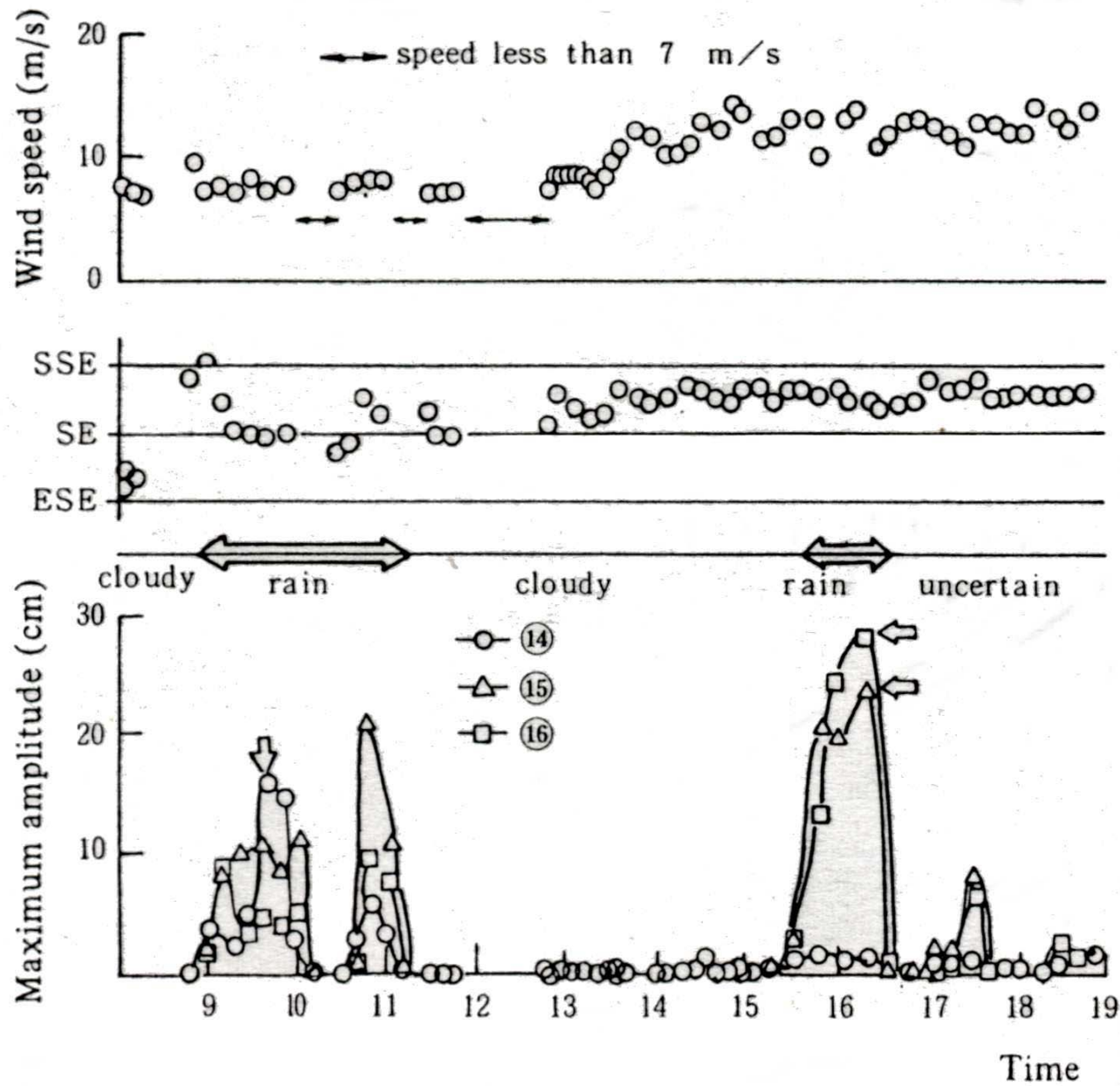




Brotonne Bridge, France, 1977

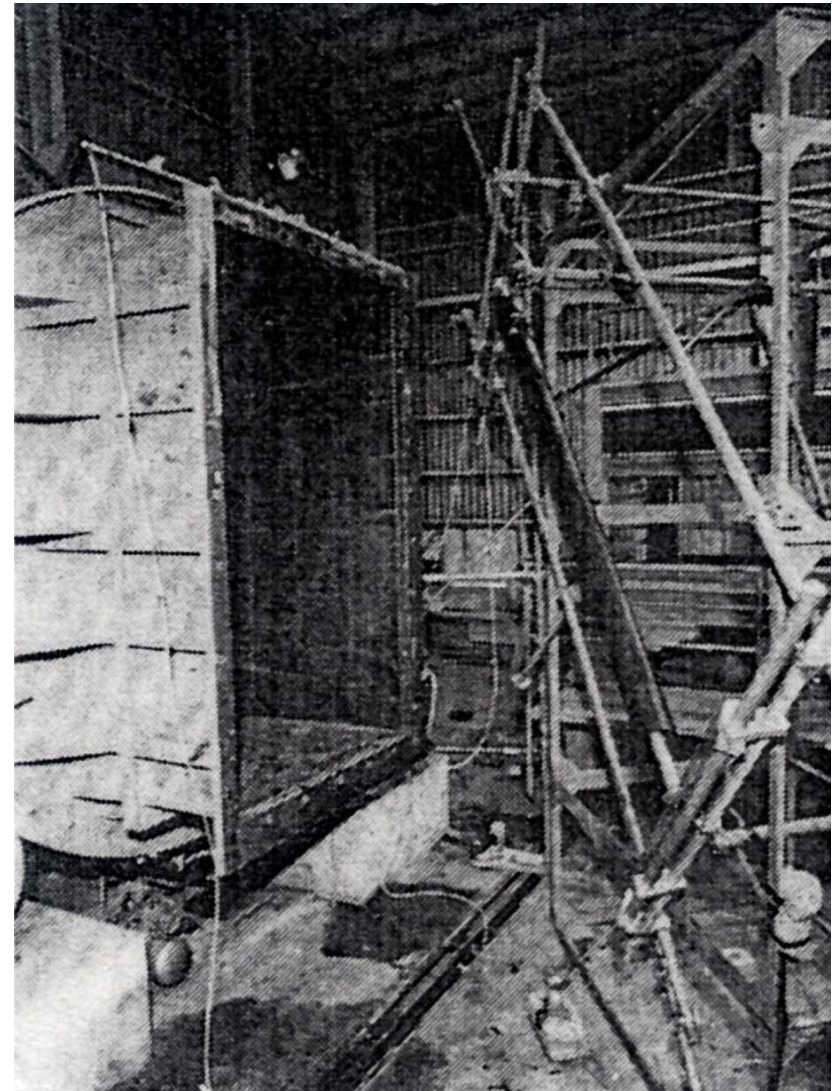
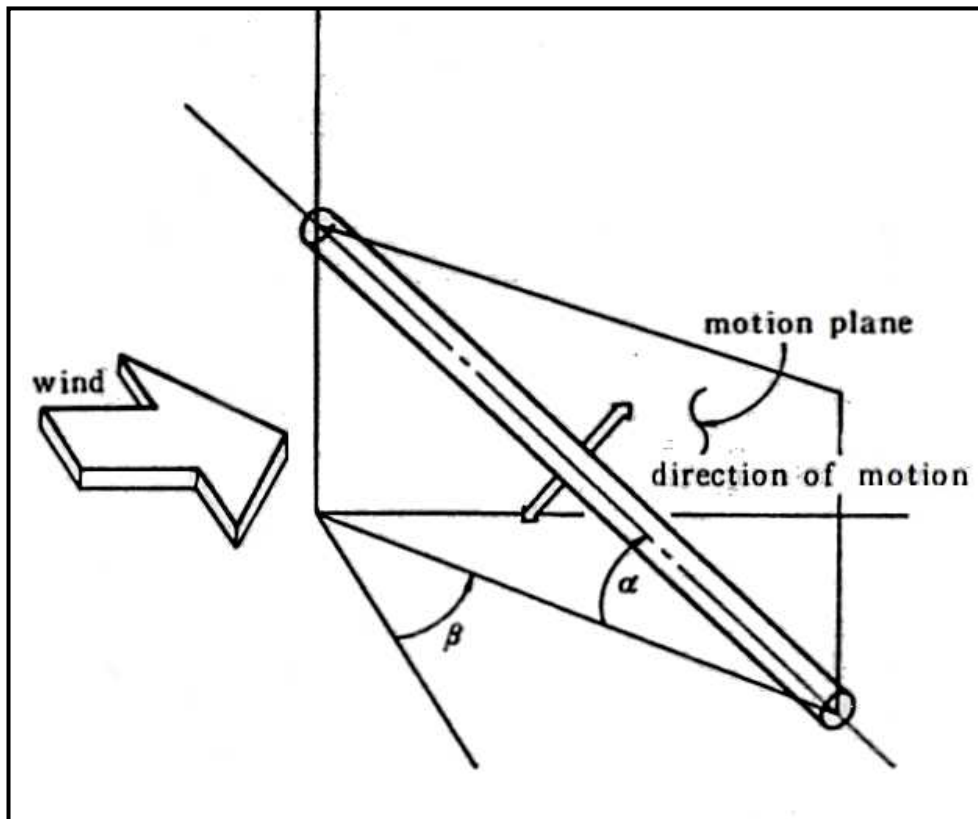


Meiko Nishi Bridge, Nagoya, Japan, 1985



Meiko Nishi Bridge, Nagoya, Japan, 1985





Meiko Nishi Bridge, Nagoya, Japan, 1985



Higashi-Kobe Bridge, Japan, 1992



Tsurumi-Tsubasa Bridge, Yokohama, Japan, 1994





Fred Hatman Bridge, U.S.A., 1995





Fred Hatman Bridge, U.S.A., 1995



Fred Hatman Bridge, U.S.A., 1995





Fred Hatman Bridge, U.S.A., 1995



Øresund Cable Stayed Bridge, 1999

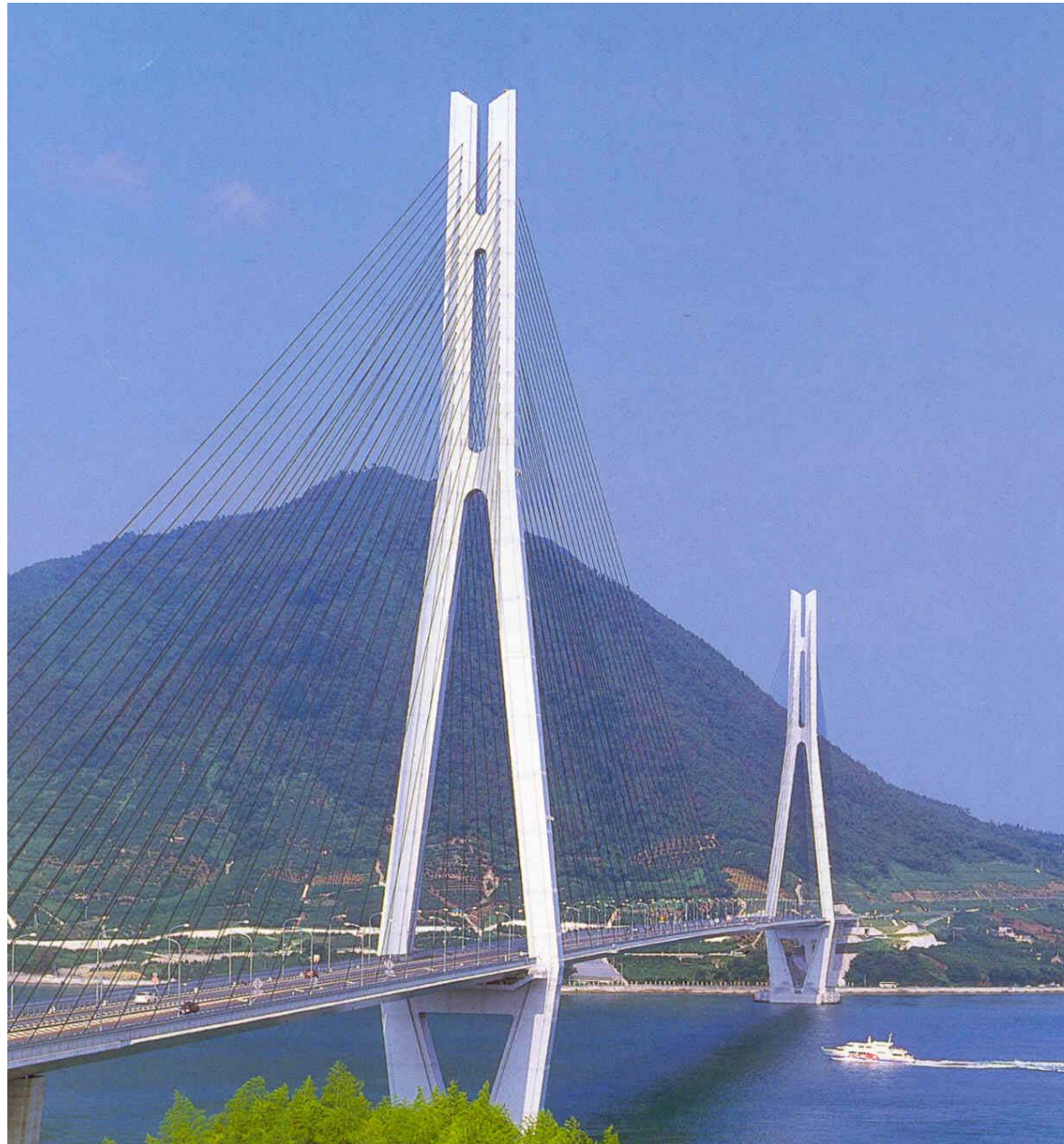


Øresund Cable Stayed Bridge, 1999

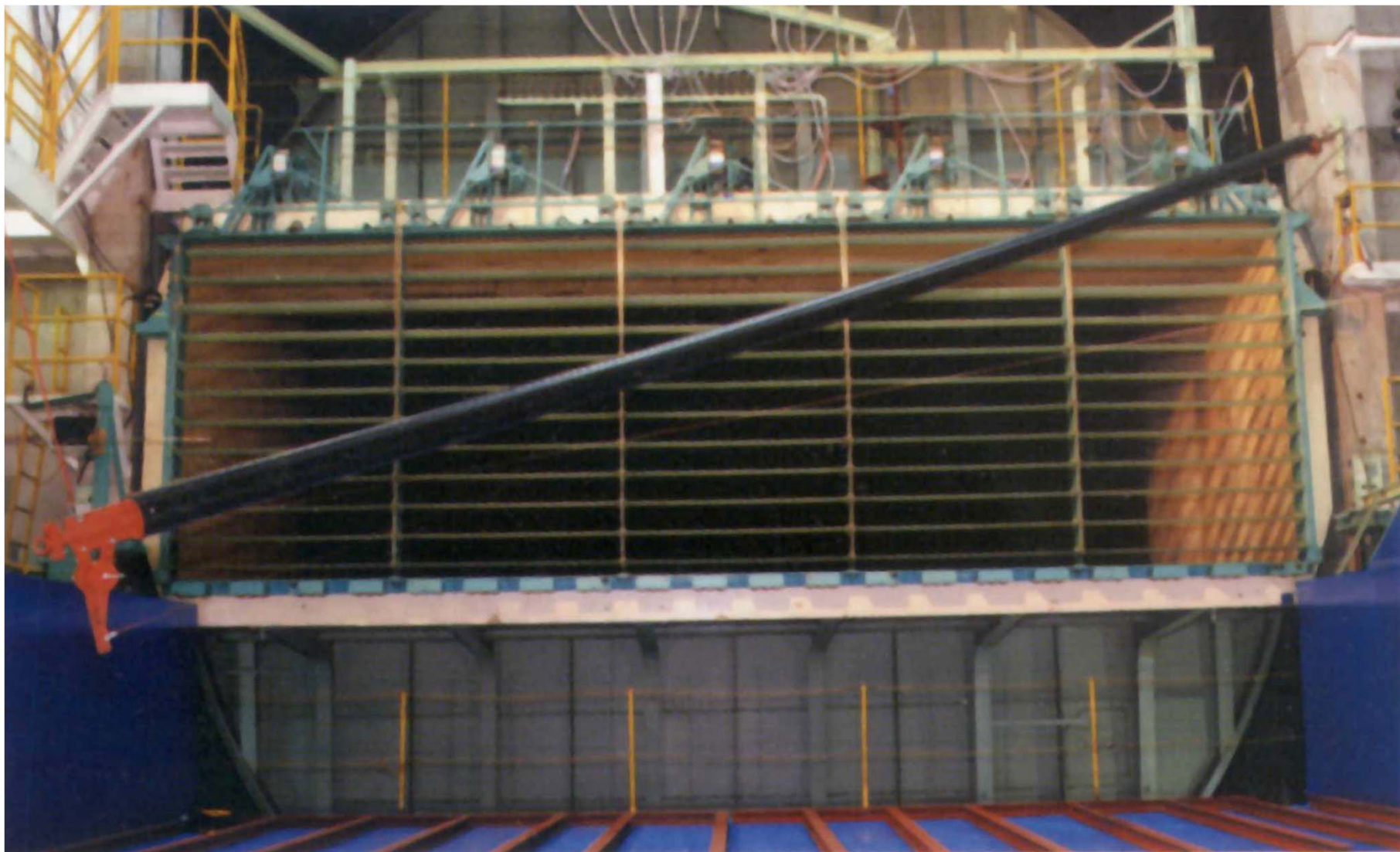


Dong Ting Bridge, China





Tatara Bridge, Japan, 1999

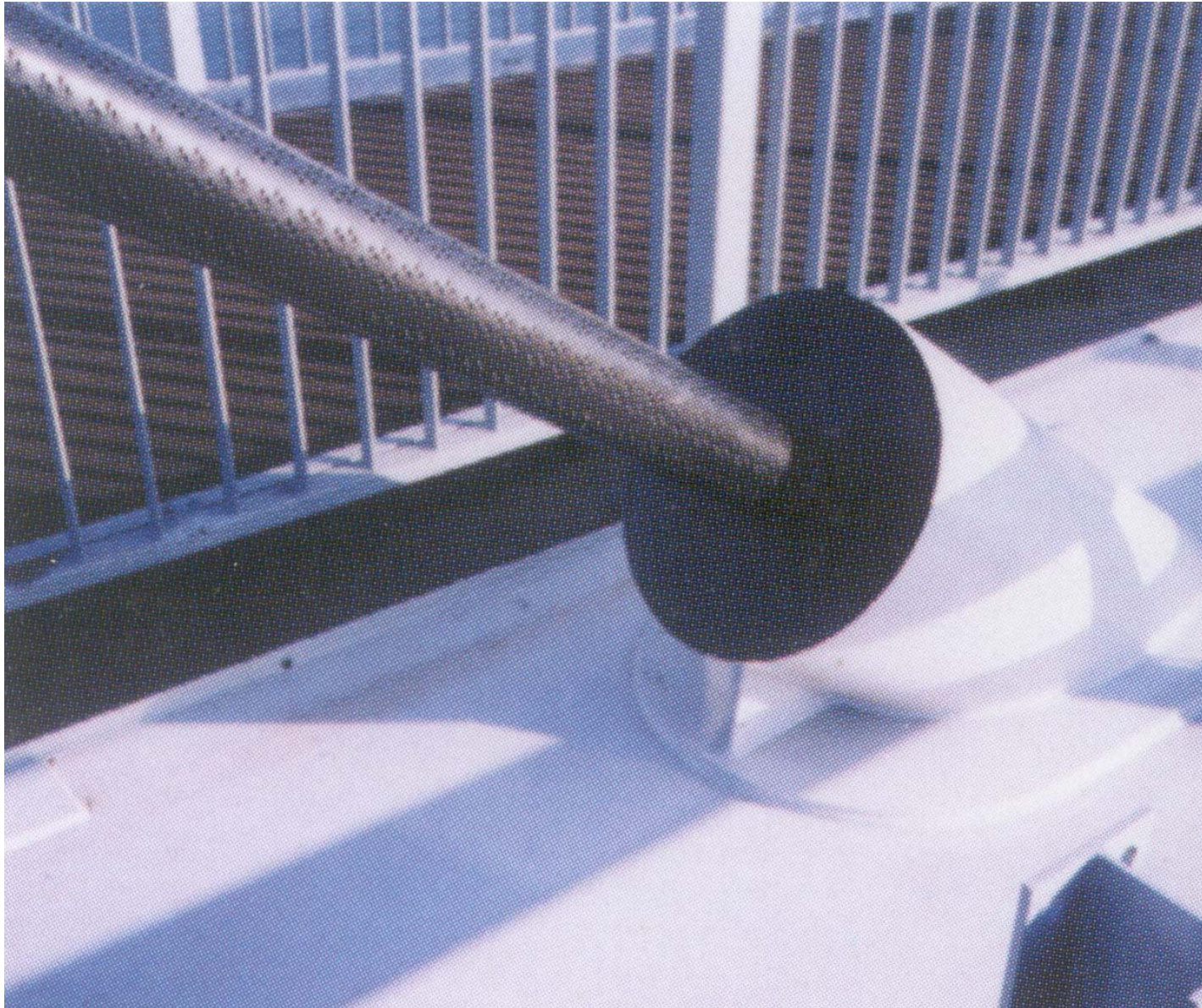


Tatara Bridge, Japan, 1999





Tatara Bridge, Japan, 1999



Tatara Bridge, Japan, 1999





Sutong Bridge, Yangtze River, China, 2007



Sutong Bridge, Yangtze River, China, 2007





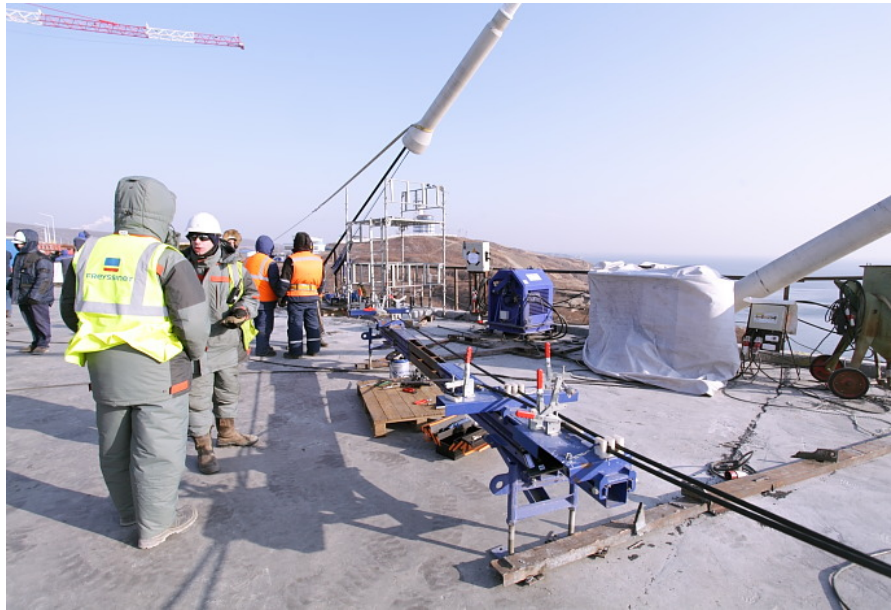
Rusky Island Bridge, Vladivostok, Siberia, 2012



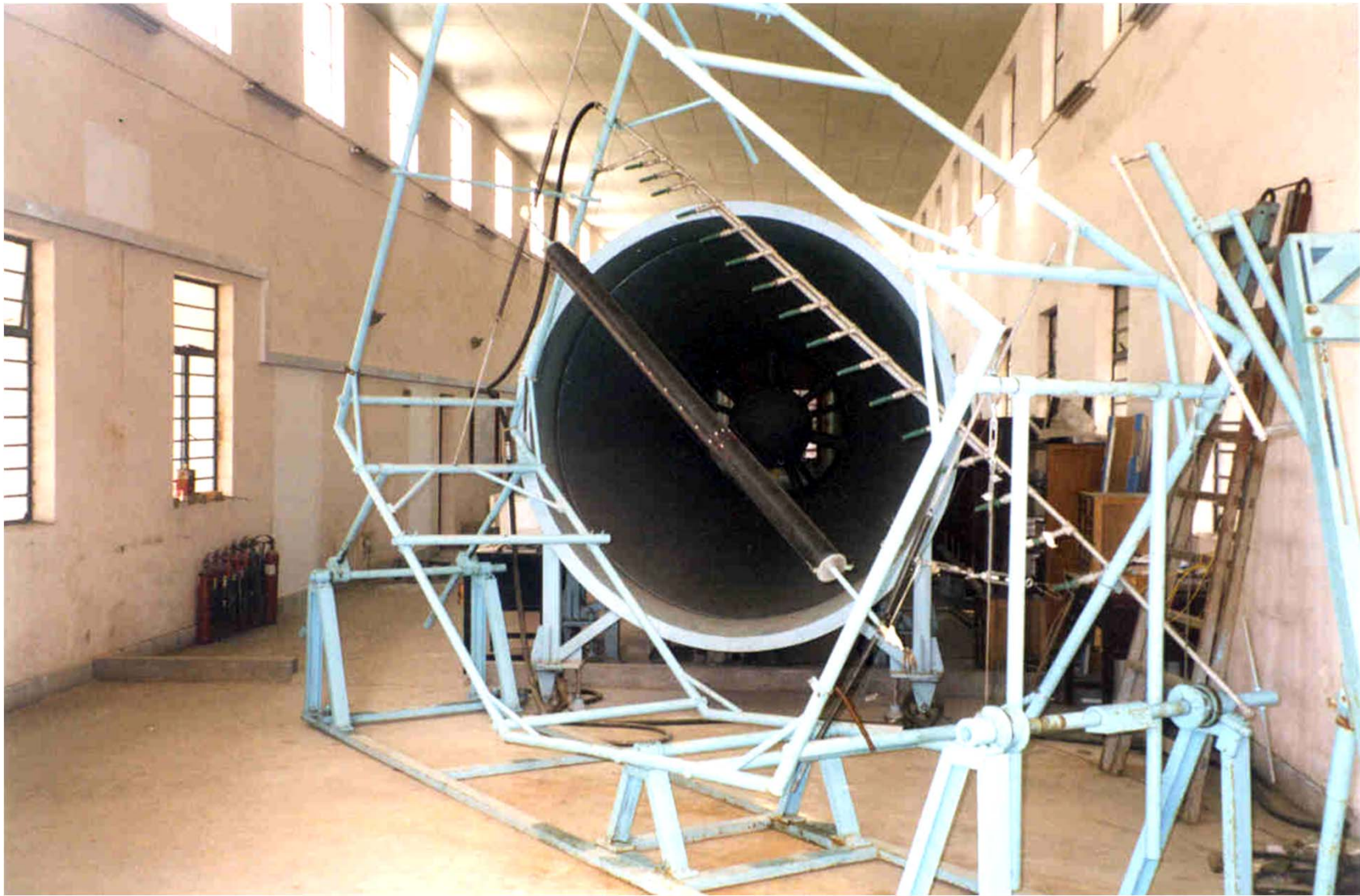


Russky Island Bridge, Vladivostok, Siberia, 2012





Rusky Island Bridge, Vladivostok, Siberia, 2012



Rain-wind-induced vibrations

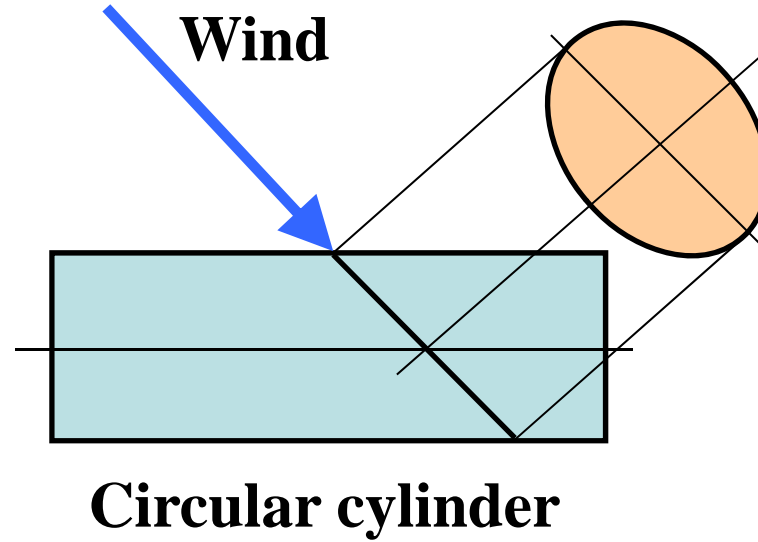
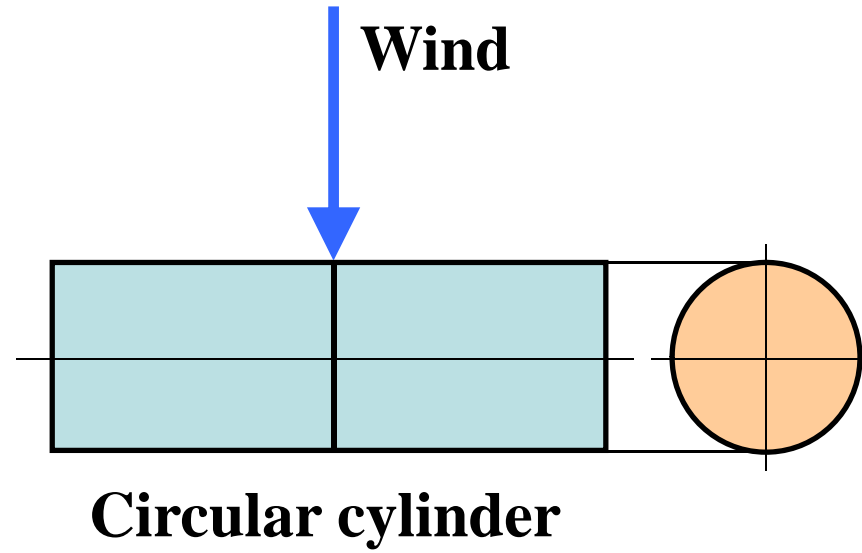


Rain-wind-induced vibrations

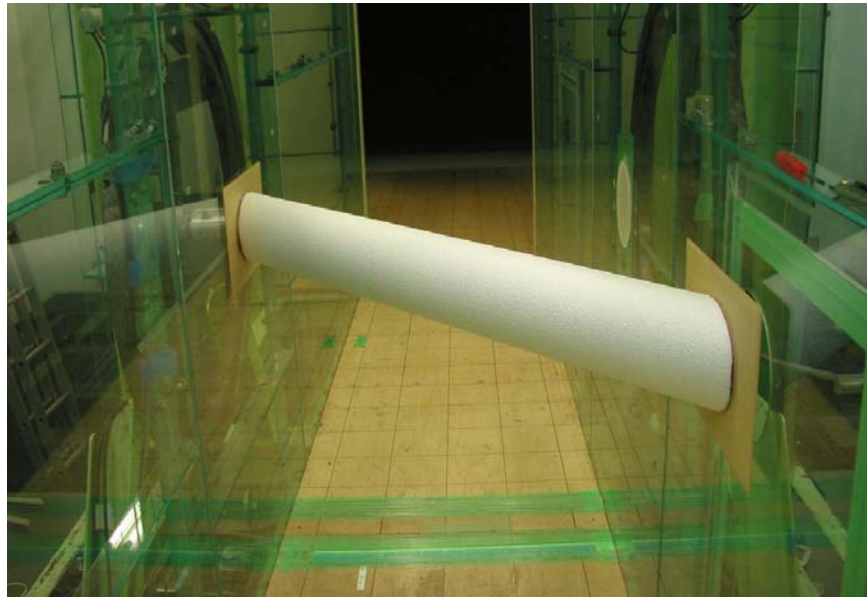
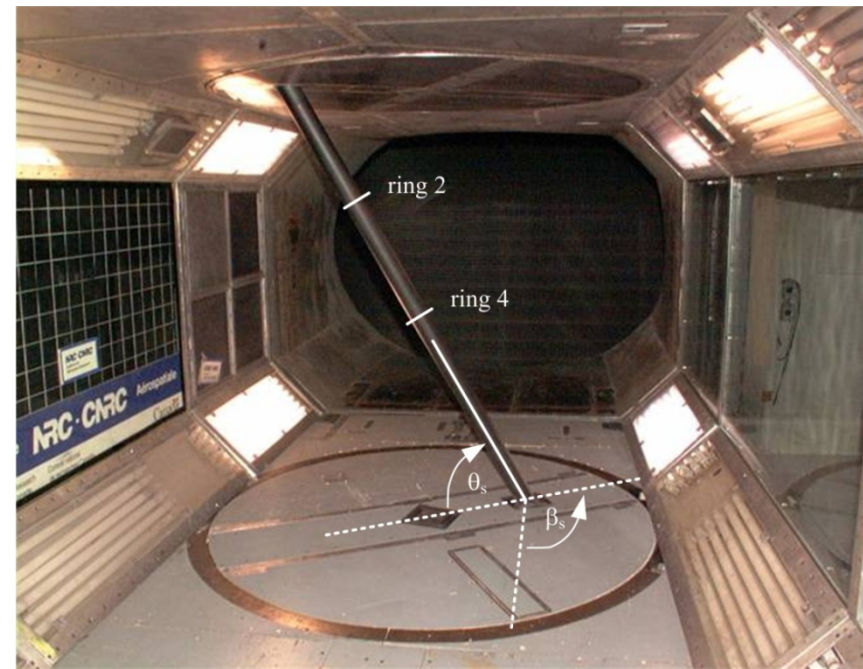
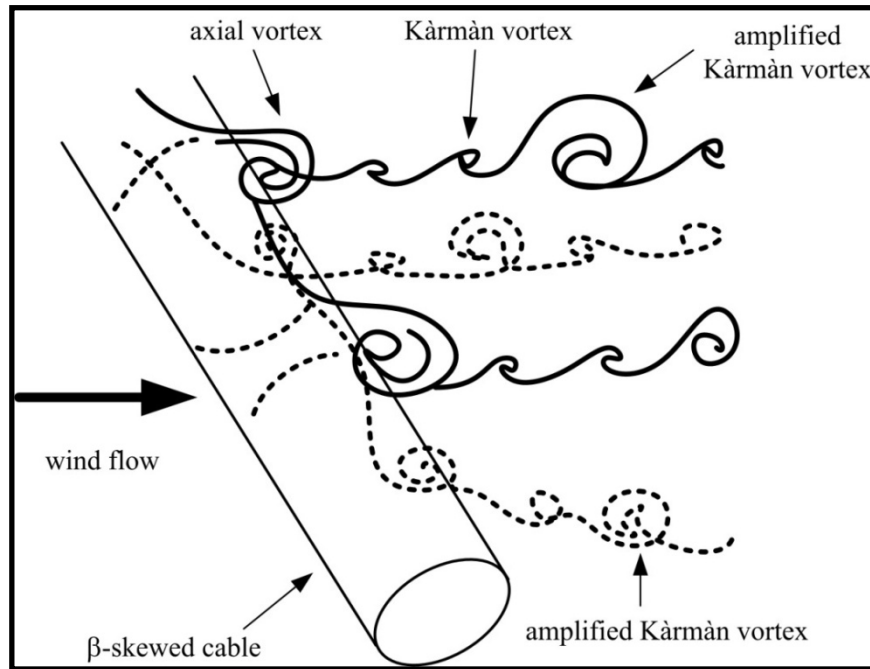




Rain-wind-induced vibrations



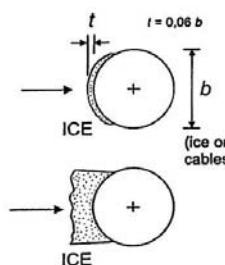
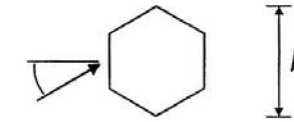
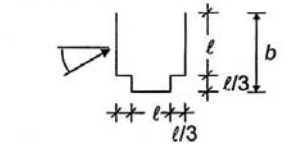
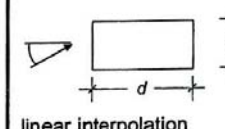
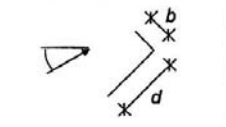
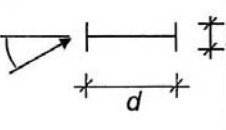
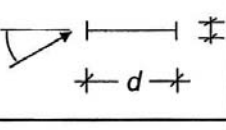
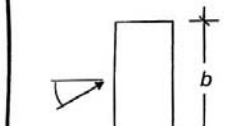
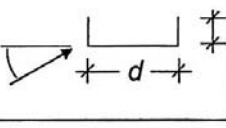
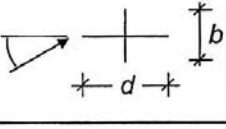
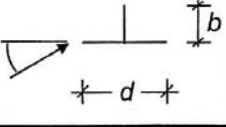
Aeroelastic instability of yawed dry circular cylinder



Aeroelastic instability of yawed dry circular cylinder

# Galloping coefficient

$$a_G = -(c_d + c'_1)$$

Cross-section	Factor of galloping instability $a_G$	Cross-section	Factor of galloping instability $a_G$		
	1,0		1,0		
			4		
 linear interpolation	$d/b=2$	2		$d/b=2$	0,7
	$d/b=1,5$	1,7		$d/b=2,7$	5
	$d/b=1$	1,2		$d/b=5$	7
 linear interpolation	$d/b=2/3$	1		$d/b=3$	7,5
	$d/b=1/2$	0,7		$d/b=3/4$	3,2
	$d/b=1/3$	0,4		$d/b=2$	1

Crosswind galloping



## Megaframe beams

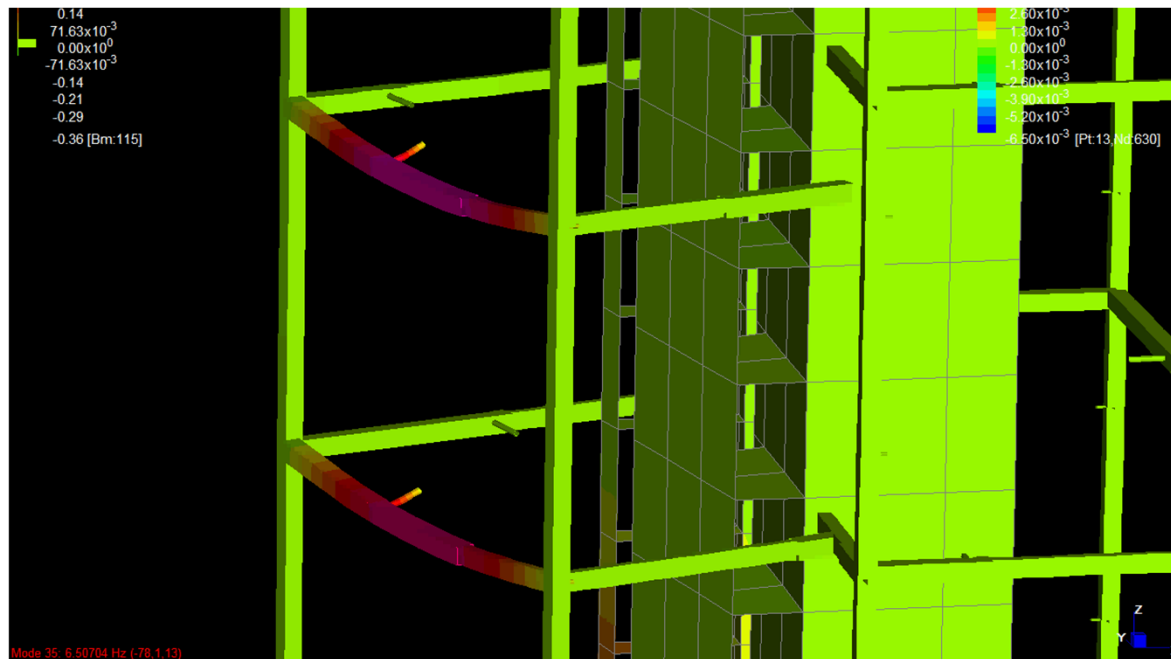
Length  $L = 11,2$  m

Square side  $b = 600$  mm

Mass per unit length  $m = 148,7$  kg/m

Fundamental frequency  $n = 6,51$  Hz

Damping coefficient  $\zeta = 0,002$





## Megaframe beams

Length  $L = 11,2$  m

Square side  $b = 600$  mm

Mass per unit length  $m = 148,7$  kg/m

Fundamental frequency  $n = 6,51$  Hz

Damping coefficient  $\zeta = 0,002$

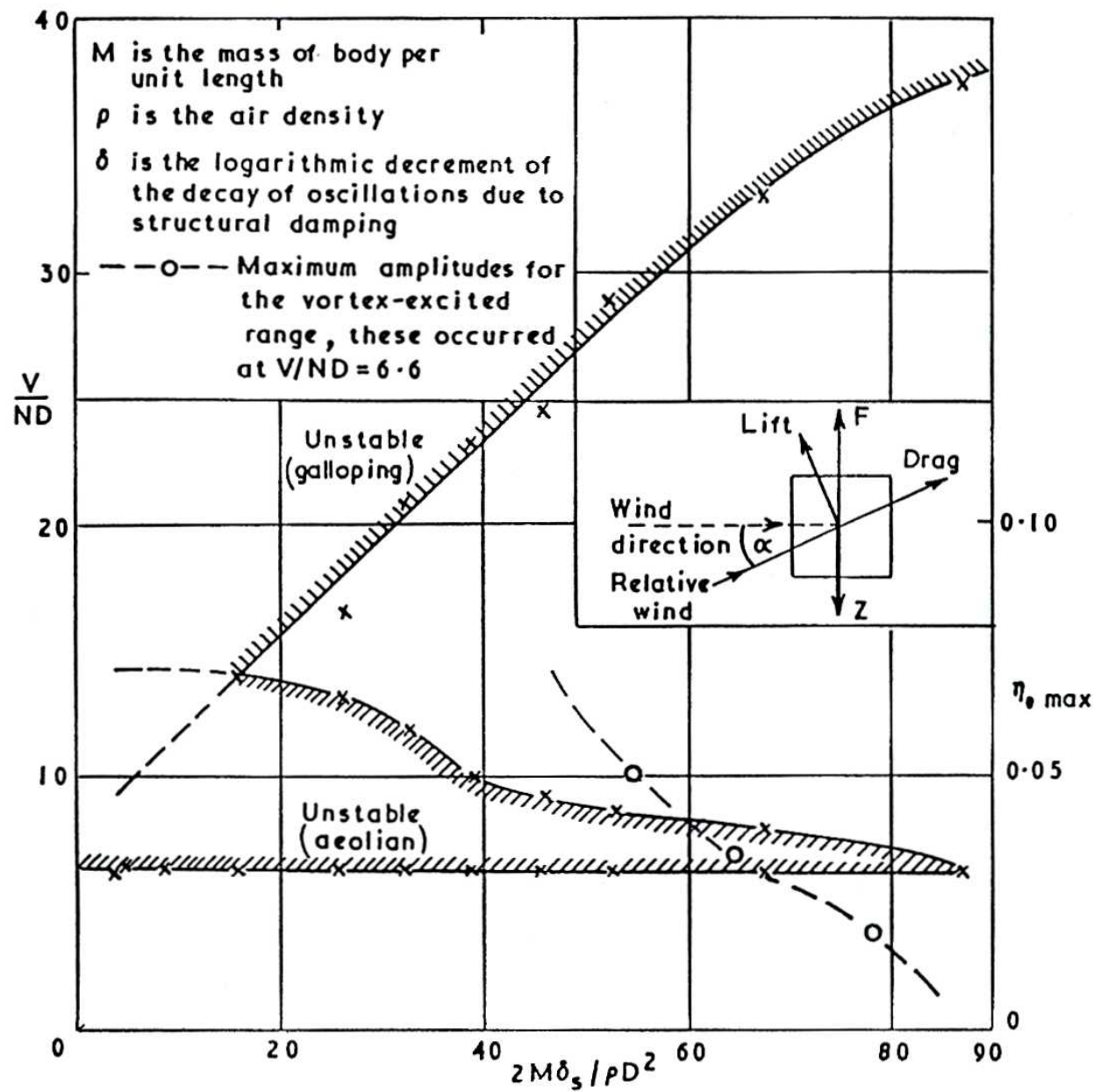
Scruton number

$$Sc = \frac{4\pi m \xi_s}{\rho b^2} = \frac{4\pi \times 148,7 \times 0,002}{1,25 \times 0,60^2} = 8,30$$

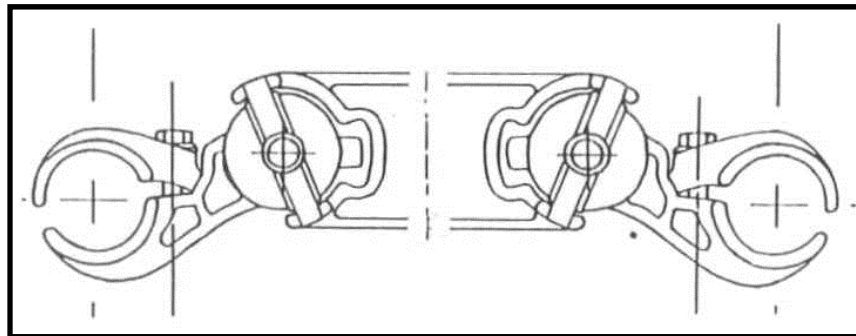
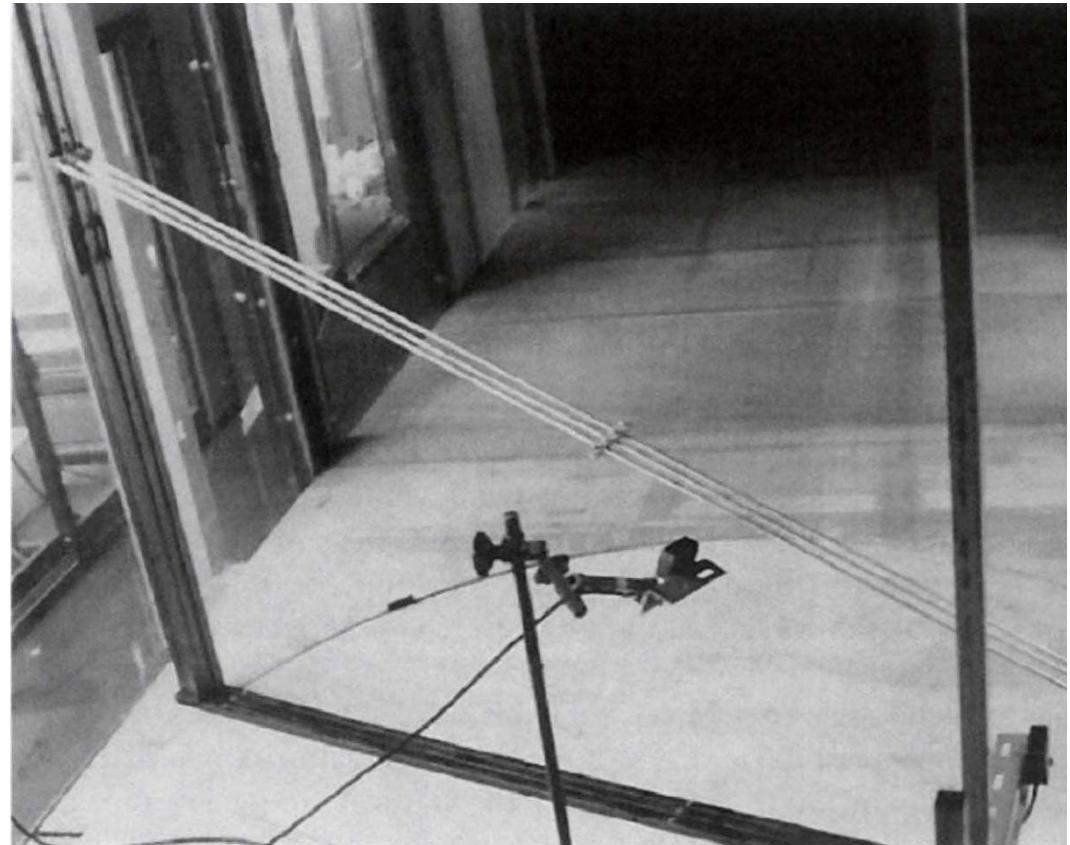
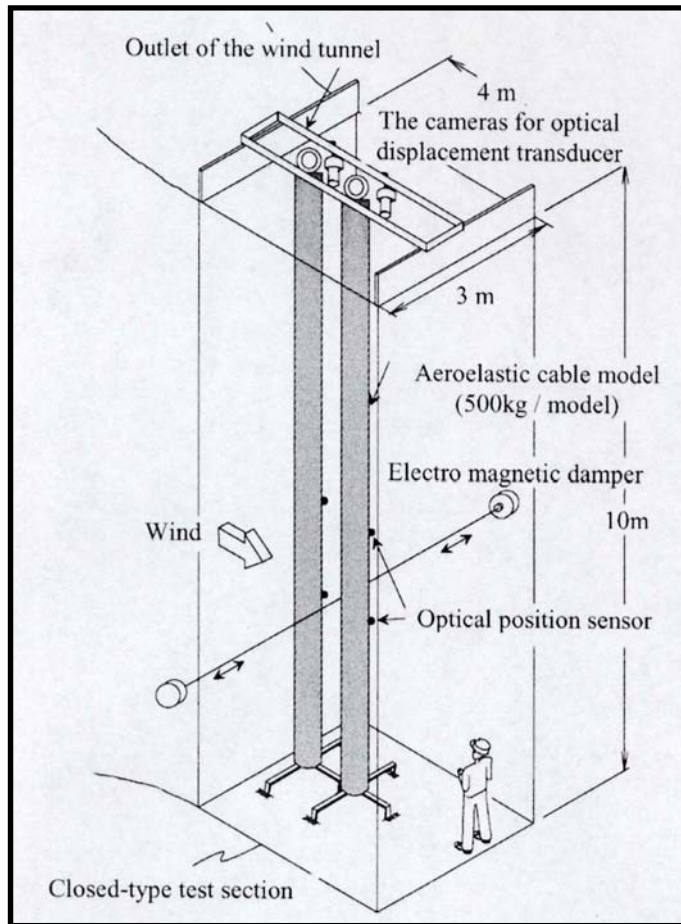
Gallop coefficient  $a_G = 1,2$

Gallop critical velocity

$$\bar{u}_{cr} = \frac{2nb}{a_G} \cdot Sc = \frac{2 \times 6,51 \times 0,60}{1,2} \cdot 8,30 = 54,0 \text{ m / s}$$



Galloping and vortex shedding critical interaction domains



Wake galloping

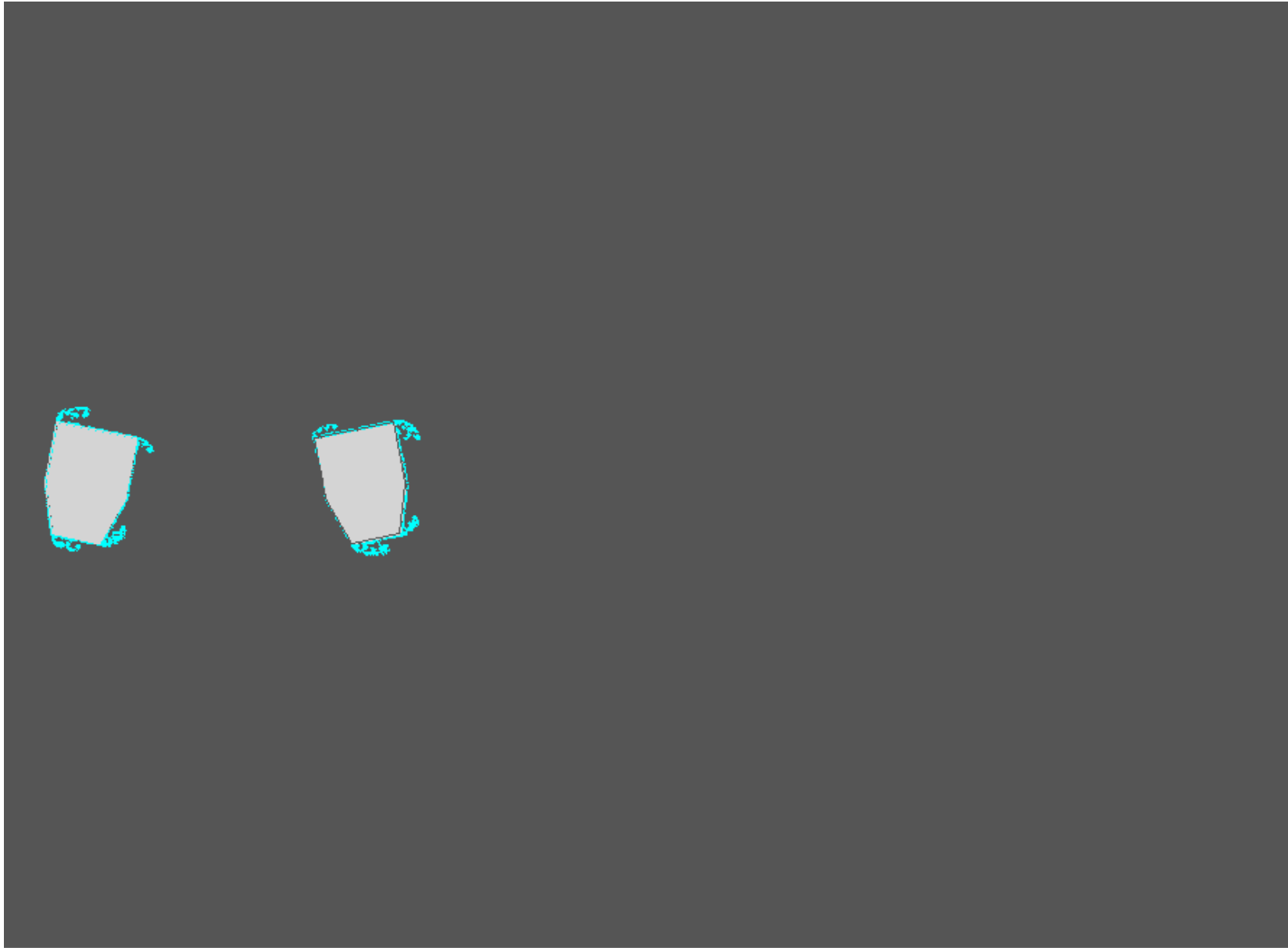


Dong Ping Bridge, China

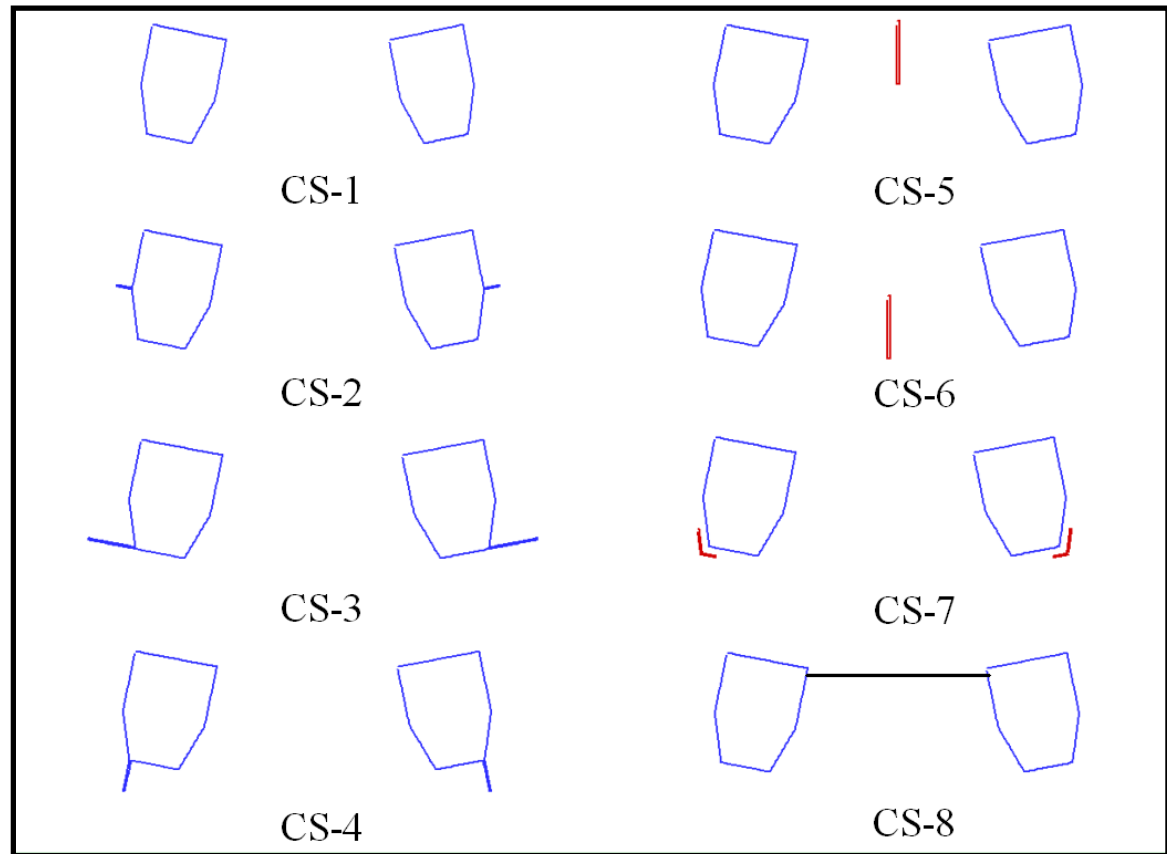
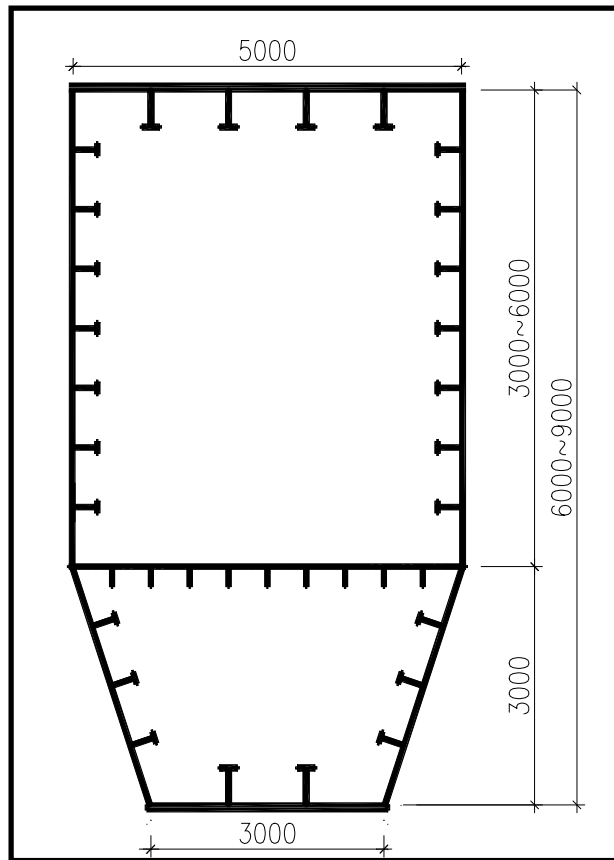




Lupu Bridge, Shanghai, China, 2003

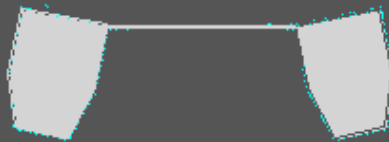


Lupu Bridge, Shanghai, China, 2003



Lupu Bridge, Shanghai, China, 2003

## *Lupu Bridge Section*



*the State Key Laboratory  
for Disaster reduction in Civil Engineering*

Lupu Bridge, Shanghai, China, 2003





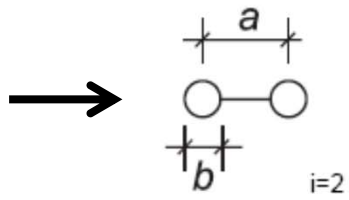
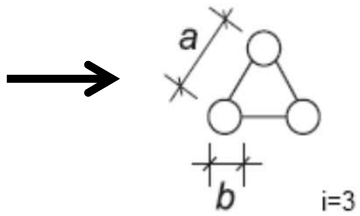
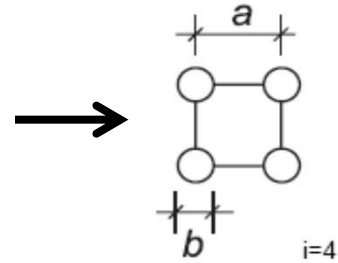
Lupu Bridge, Shanghai, China, 2003

## Necessary condition

$$a_G > 0$$

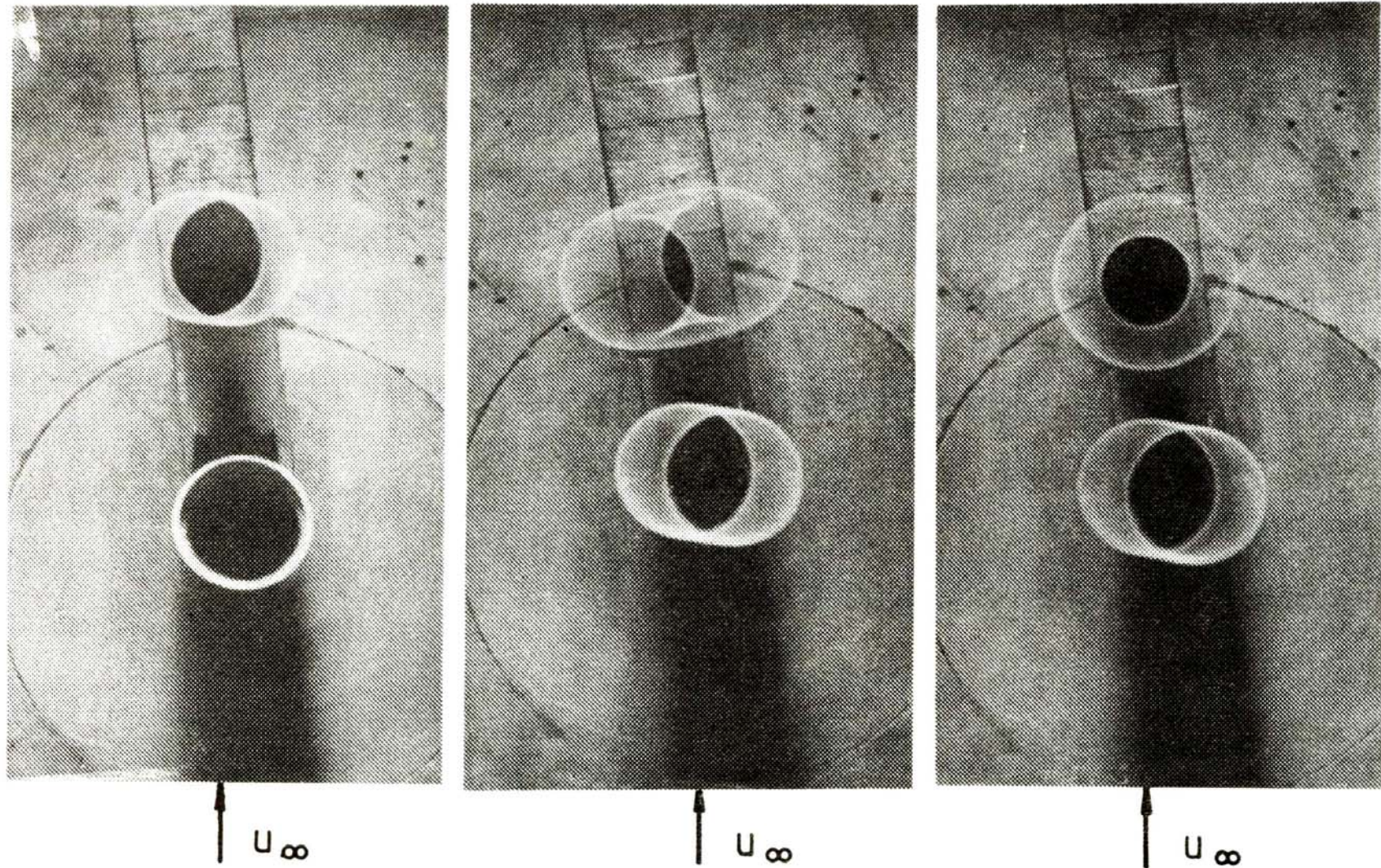
## Critical velocity

$$\bar{u}_{cr} = \frac{4m\omega_0\xi_s}{\rho b a_G} = \frac{2n_0 b}{a_G} \cdot Sc$$

Number of coupled cylinders	$a_G$	
	$a/b \leq 1,5$	$a/b \geq 2,5$
	1,5	3,0
	6,0	3,0
	1,0	2,0

Classical galloping for structurally connected circular cylinder





Interference galloping for non-structurally connected circular cylinder

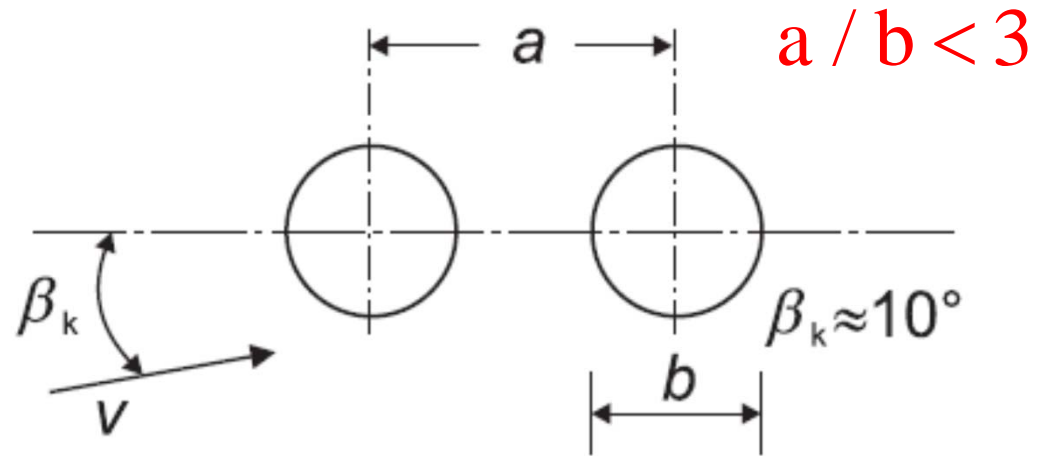


## Necessary condition

$$a_{IG} > 0$$

## Critical velocity

$$v_{IG} = 3,5 \cdot n_1 \cdot \sqrt{\frac{a \cdot b}{a_{IG}} \cdot Sc}$$



$a_{IG}$  = Interference Galloping factor

In the lack of more accurate assessments,

$a_{IG}$  can be taken as equal to 3

Interference galloping for non-structurally connected  
circular cylinder





Thermoelectric Power Plant, Priolo Gargallo, Siracusa

## Coupled chimneys with Tuned Mass Damper (TMD)

$$h = 90 \text{ m}; d = 6,4 \text{ m}; a = 8,4 \text{ m} \Rightarrow a / d = 1,31$$

$$n_1 = 0,80 \text{ Hz}; \xi = 0,08; m = 1.683 \text{ kg / m}$$

$$S_c = \frac{4\pi \cdot m \cdot \xi}{\rho \cdot d^2} = \frac{4\pi \cdot 1.683 \cdot 0,08}{1,25 \cdot 6,4^2} = 33,05$$

## Classical galloping for structurally connected chimneys

$$a / d = 1,31 < 1,5 \Rightarrow a_G = 1,5$$

$$\bar{u}_{cr} = \frac{2n_1 b}{a_G} \cdot S_c = \frac{2 \times 0,80 \times 6,4}{1,5} \cdot 33,05 = 226 \text{ m / s}$$

## Interference galloping for non – structurally connected chimneys

$$v_{IG} = 3,5 \cdot n_1 \cdot \sqrt{\frac{a \cdot b}{a_{IG}}} \cdot S_c = 3,5 \cdot 0,8 \cdot \sqrt{\frac{8,4 \cdot 6,4}{3}} \cdot 33,05 = 68 \text{ m / s}$$