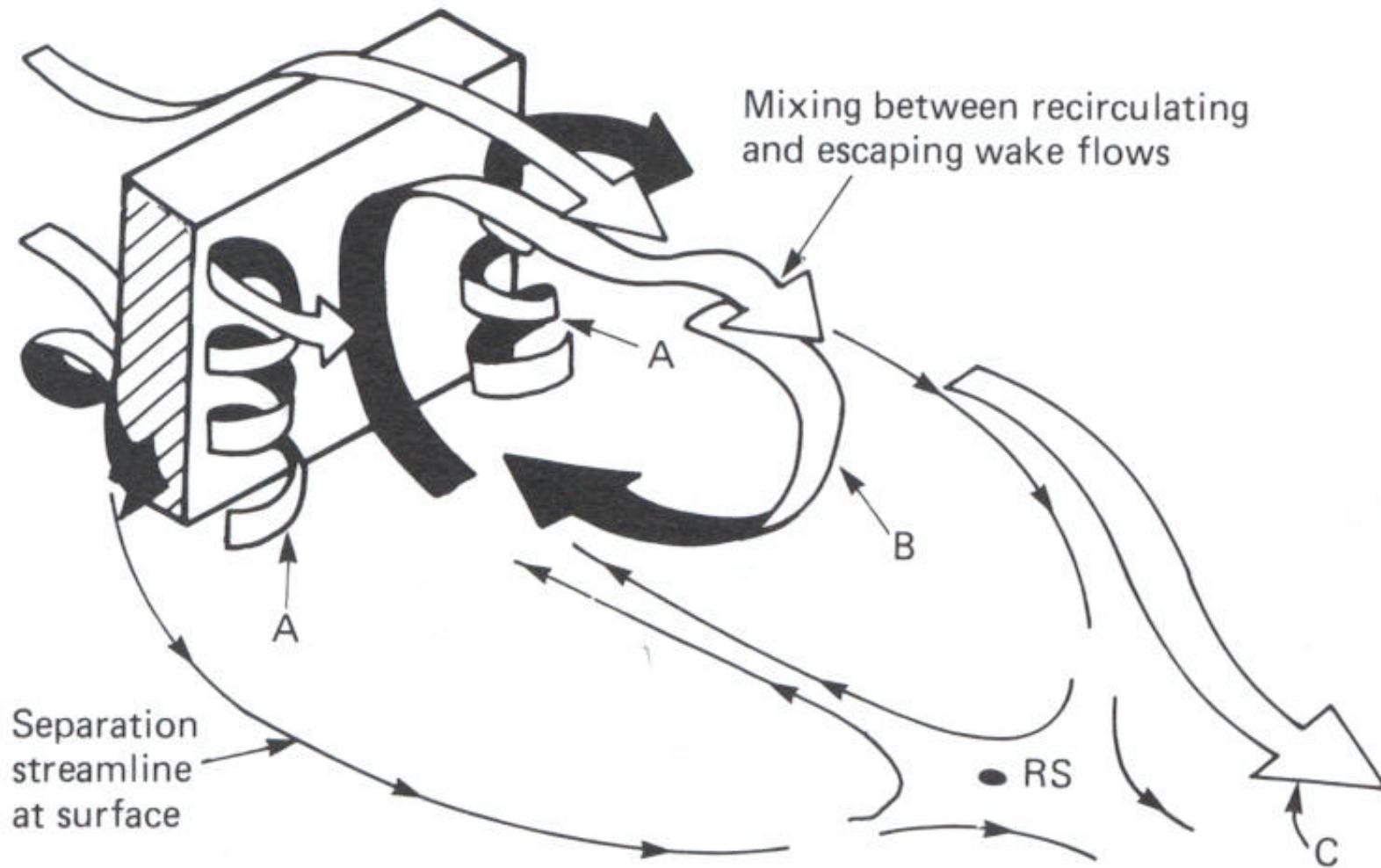


# 3-D WIND-EXCITED RESPONSE OF THREE-DIMENSIONAL BLUFF-BODIES



# 3D RESPONSE OF 3D STRUCTURES

Wind tunnel tests

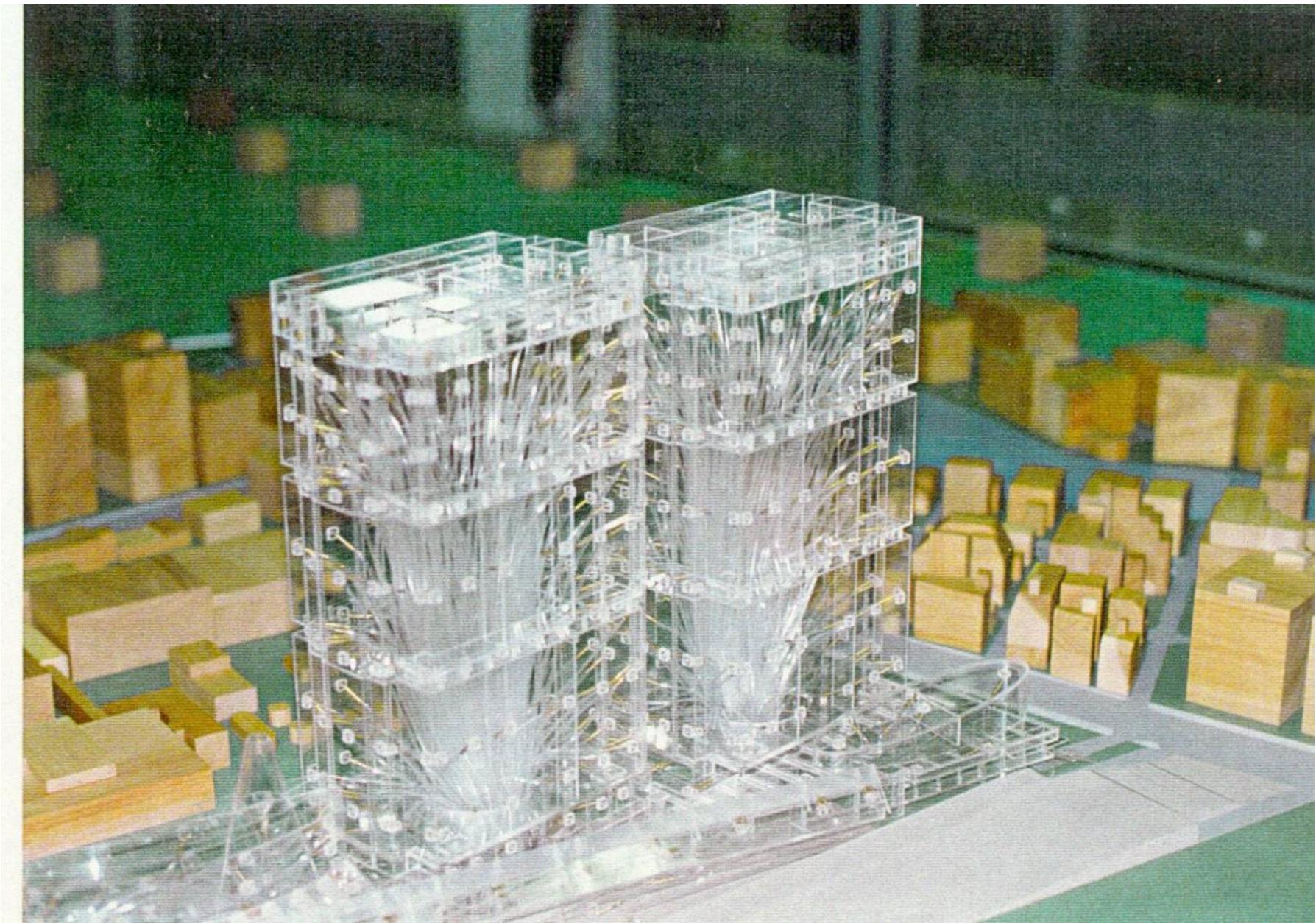
- pressure taps tests
- high-frequency force balance tests
- flexible balance aeroelastic tests
- fully aeroelastic tests

Full-scale tests

CFD analyses

Electronic databases

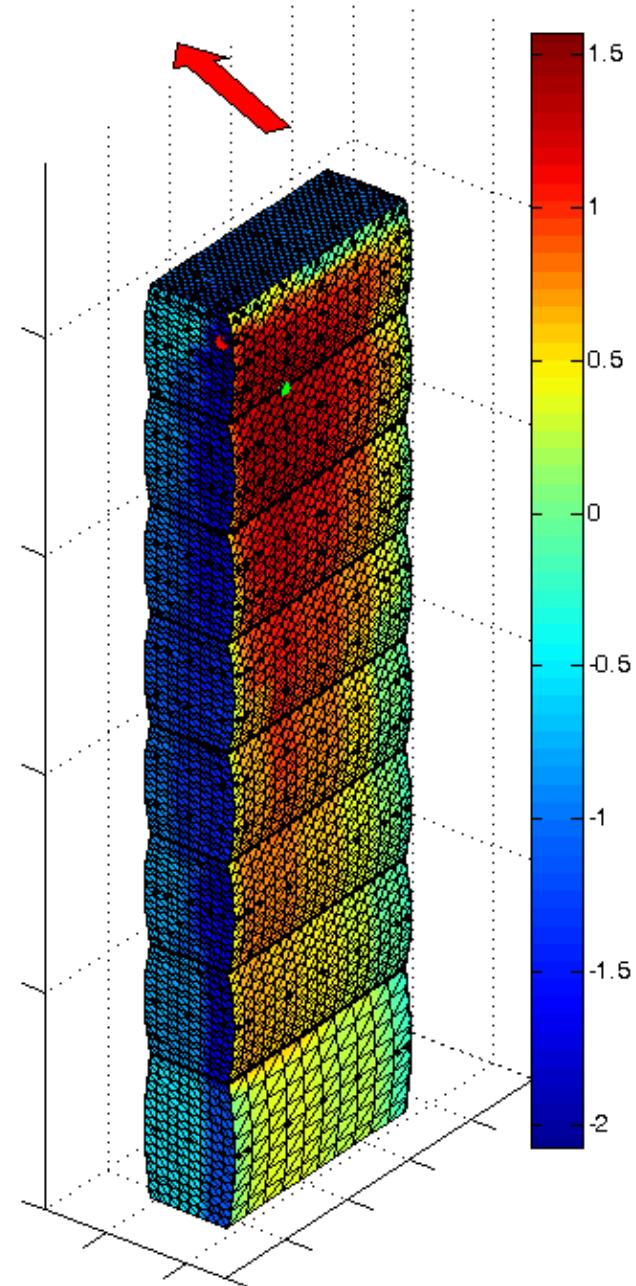
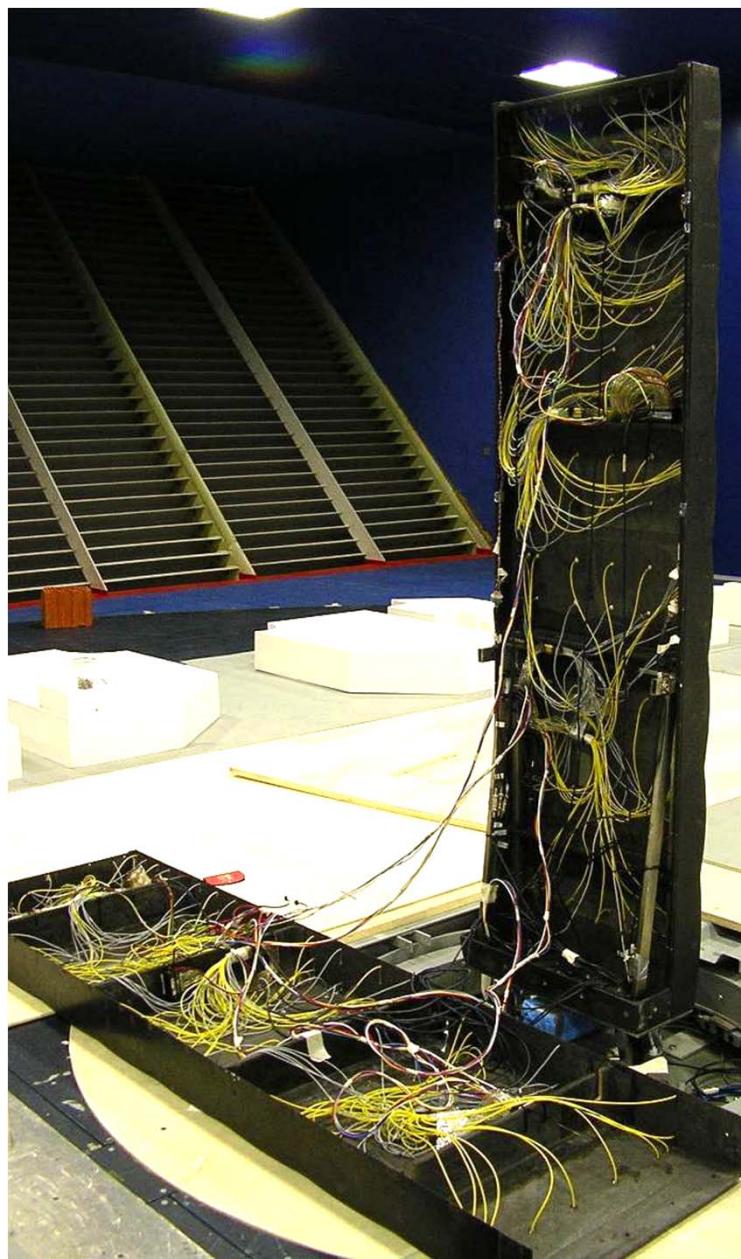
Analytical methods



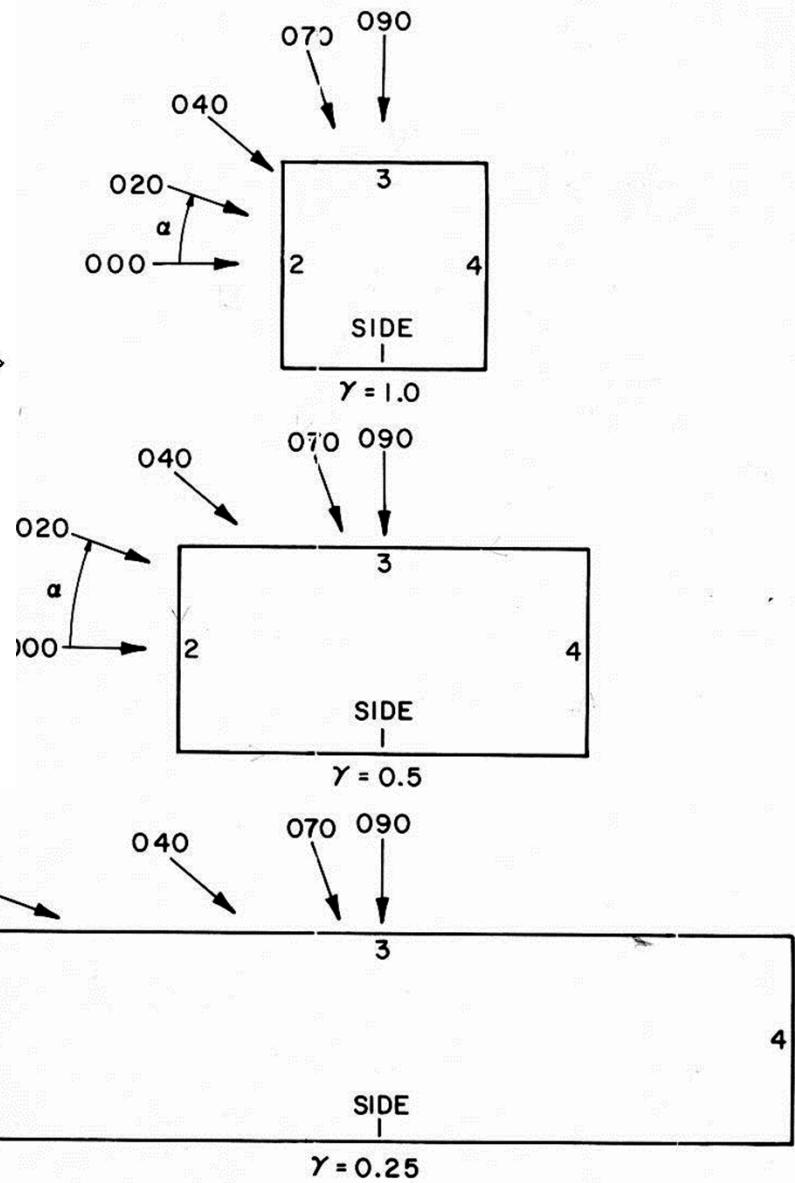
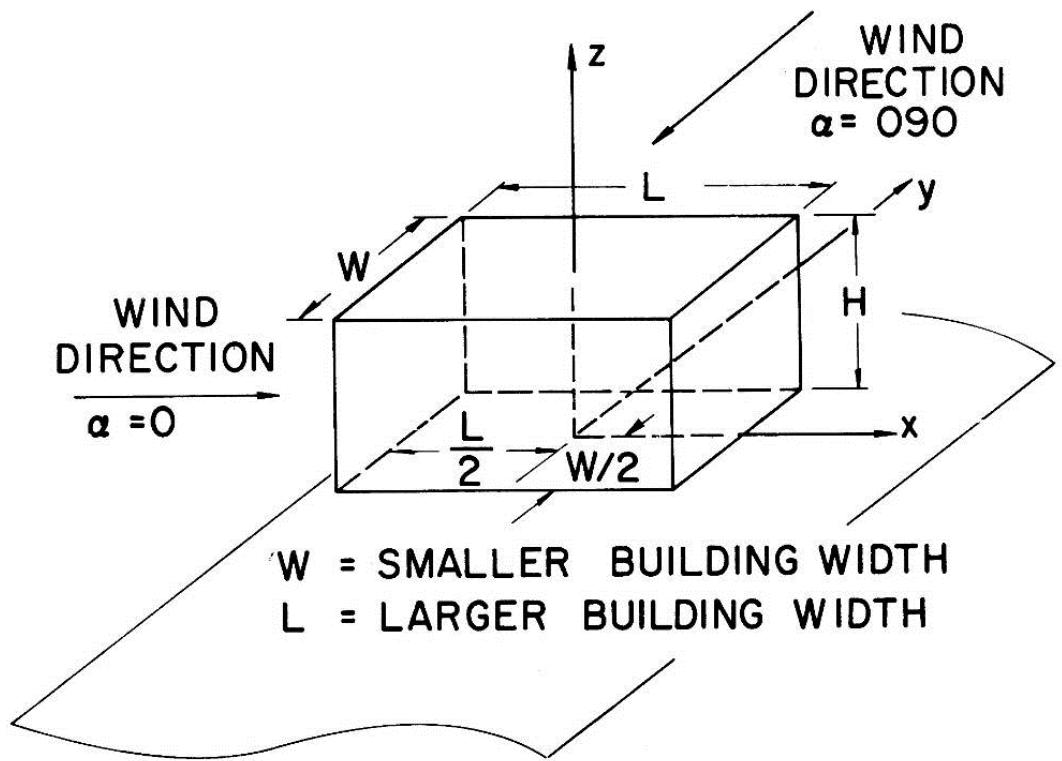
Pressure taps measurements



Pressure taps measurements



Pressure taps measurements



Akins and Paterka (1977)

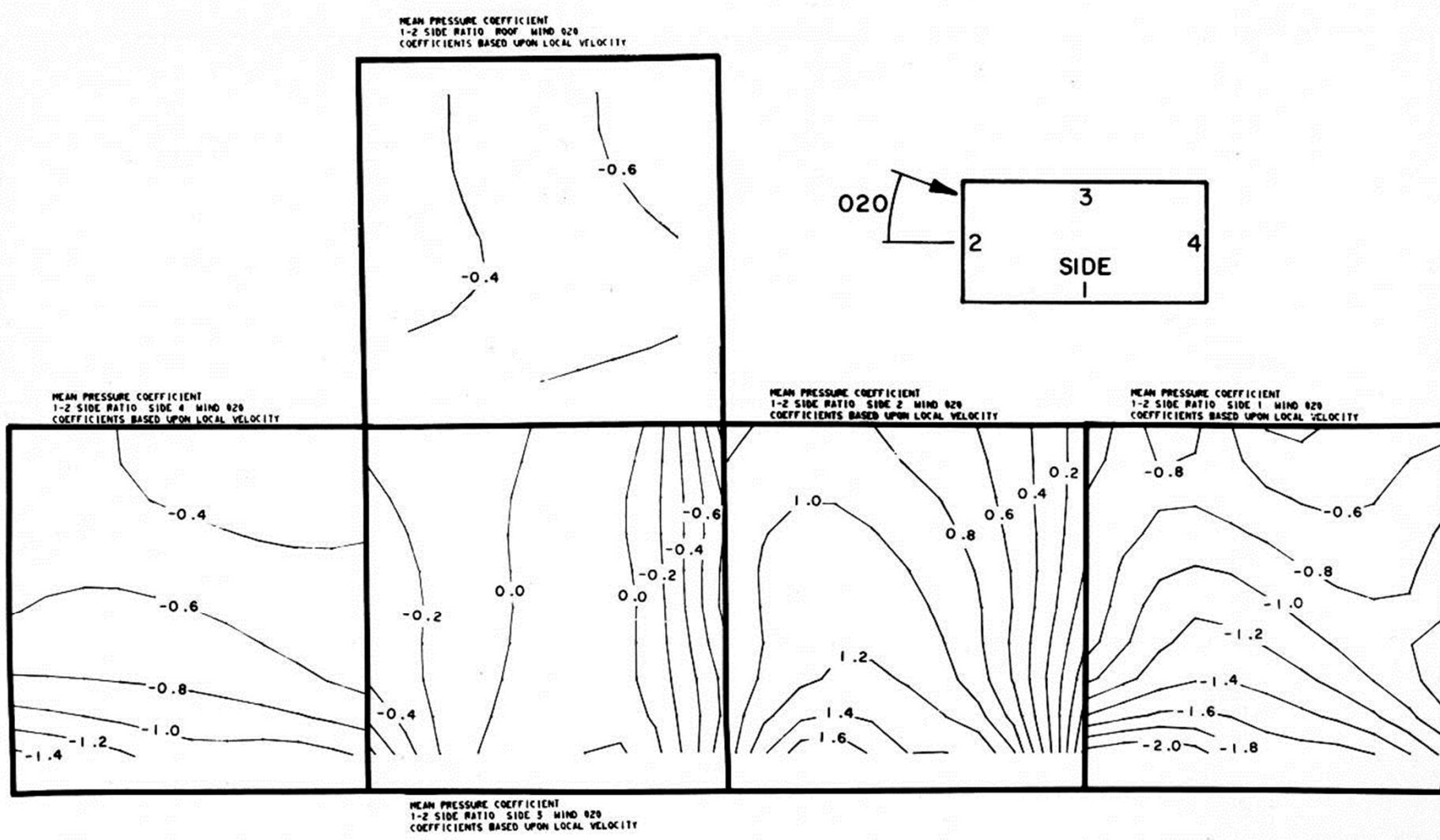
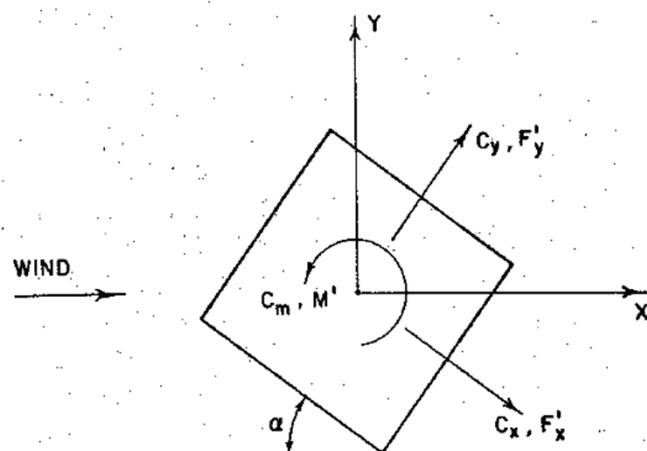
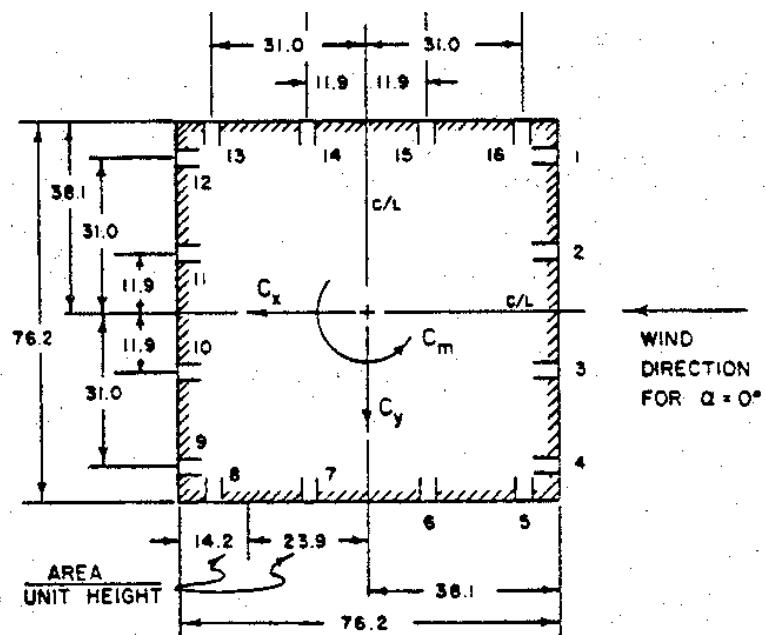
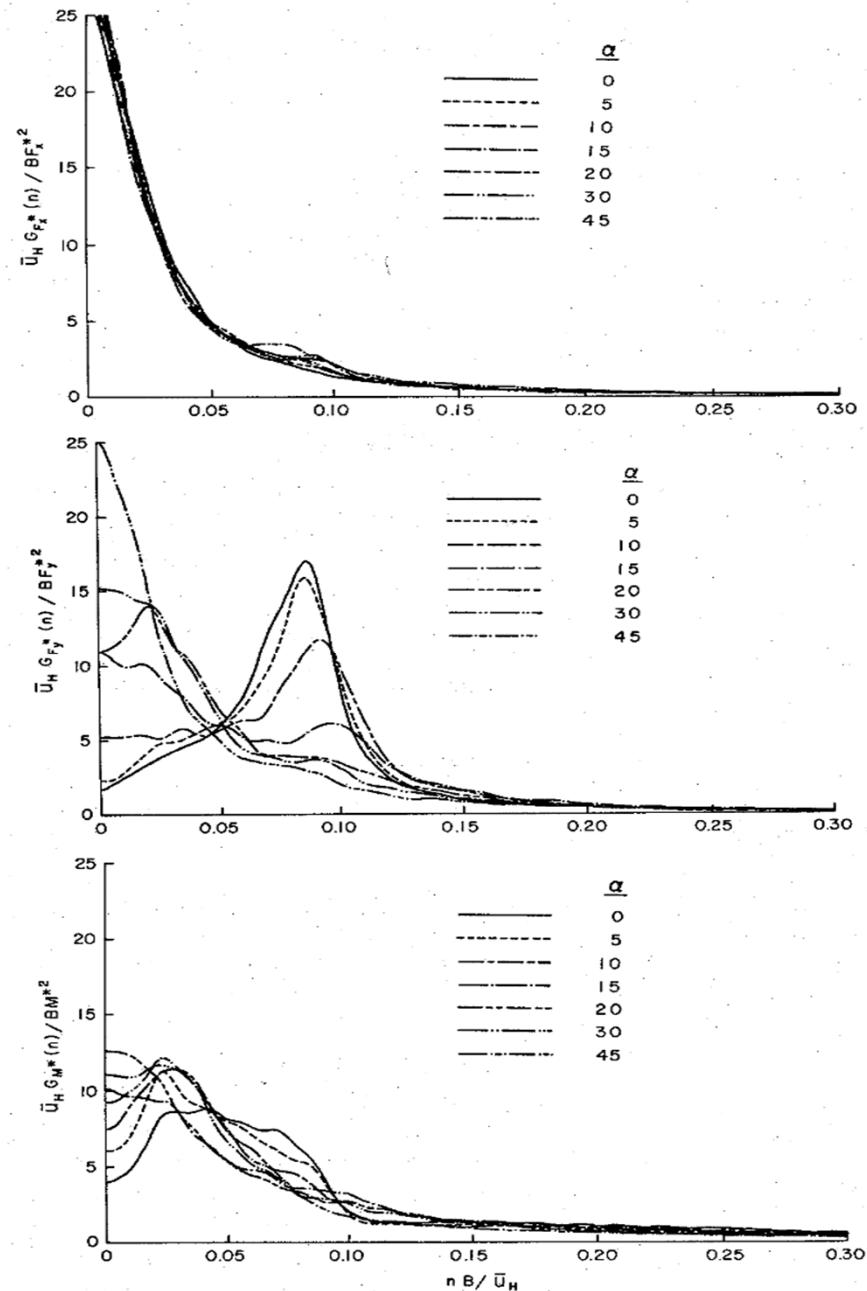


Figure B7.  $C_{p\text{mean}}$ ,  $\bar{\beta}$ ,  $\bar{p}$ ,  $\alpha = 20$ ,  $\gamma = 0.5$

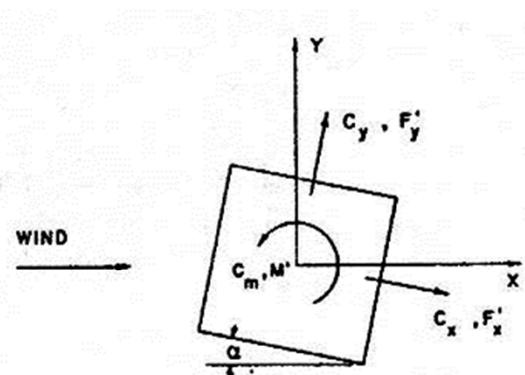
Akins and Paterka (1977)



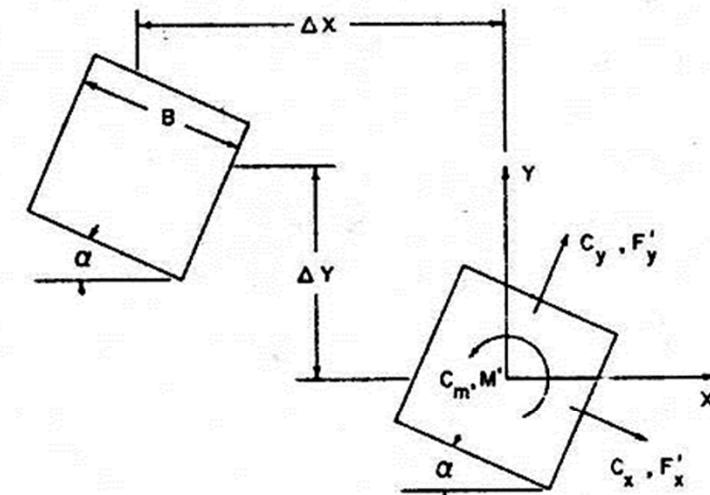
CONFIGURATION - (a)



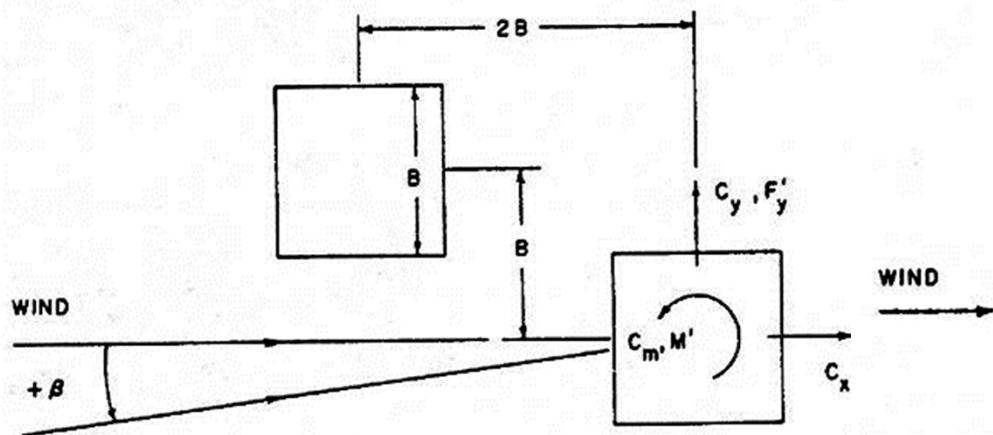
Reinhold and Sparks (1979)



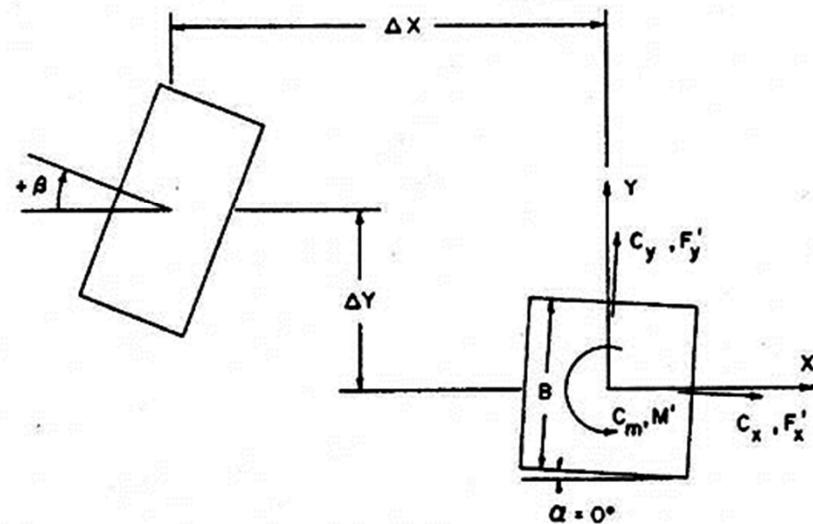
CLASS A , CONFIGURATION ( $\alpha$ )



CLASS B , CONFIGURATION ( $\alpha - \frac{\Delta X}{B} - \frac{\Delta Y}{B}$ )

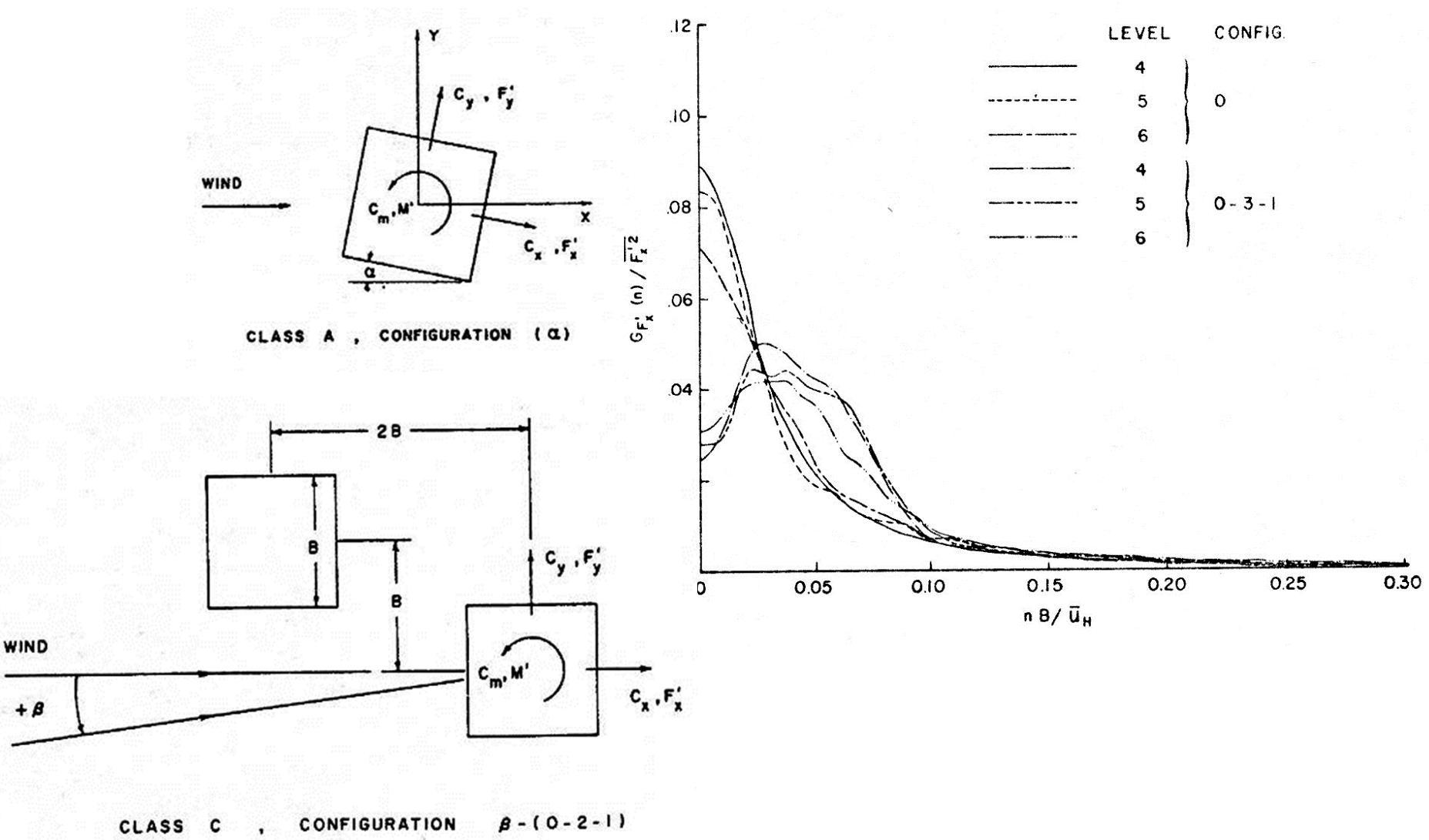


CLASS C , CONFIGURATION  $\beta - (0-2-1)$



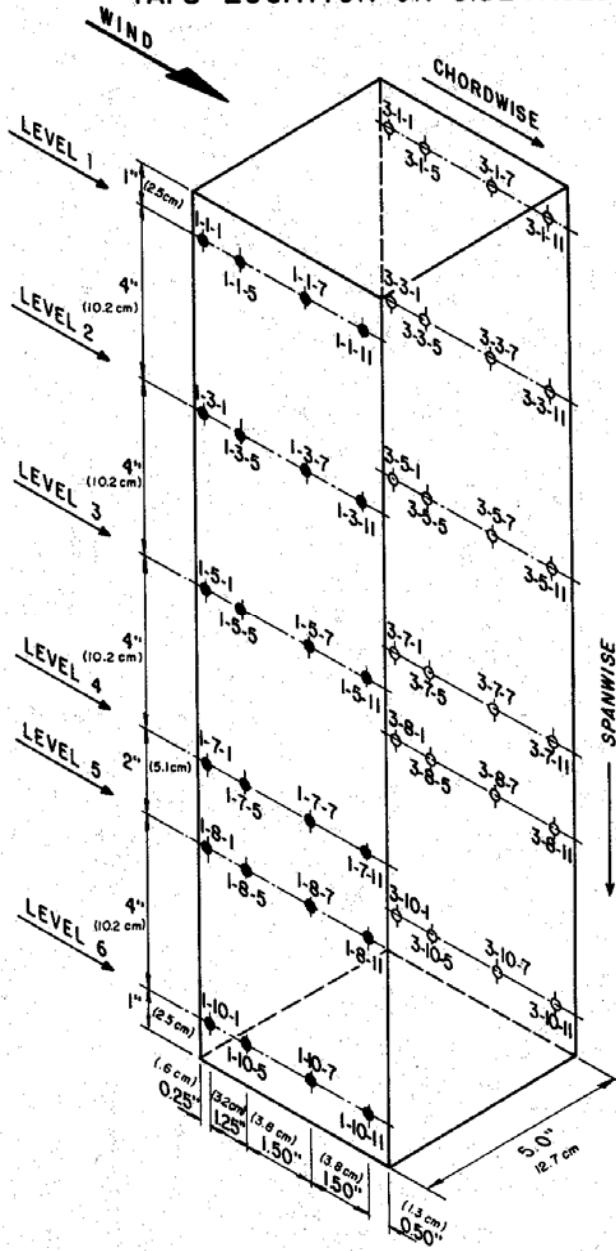
CLASS D , CONFIGURATION ( $\alpha - \beta - \frac{\Delta X}{B} - \frac{\Delta Y}{B}$ )

Reinhold and Sparks (1979)

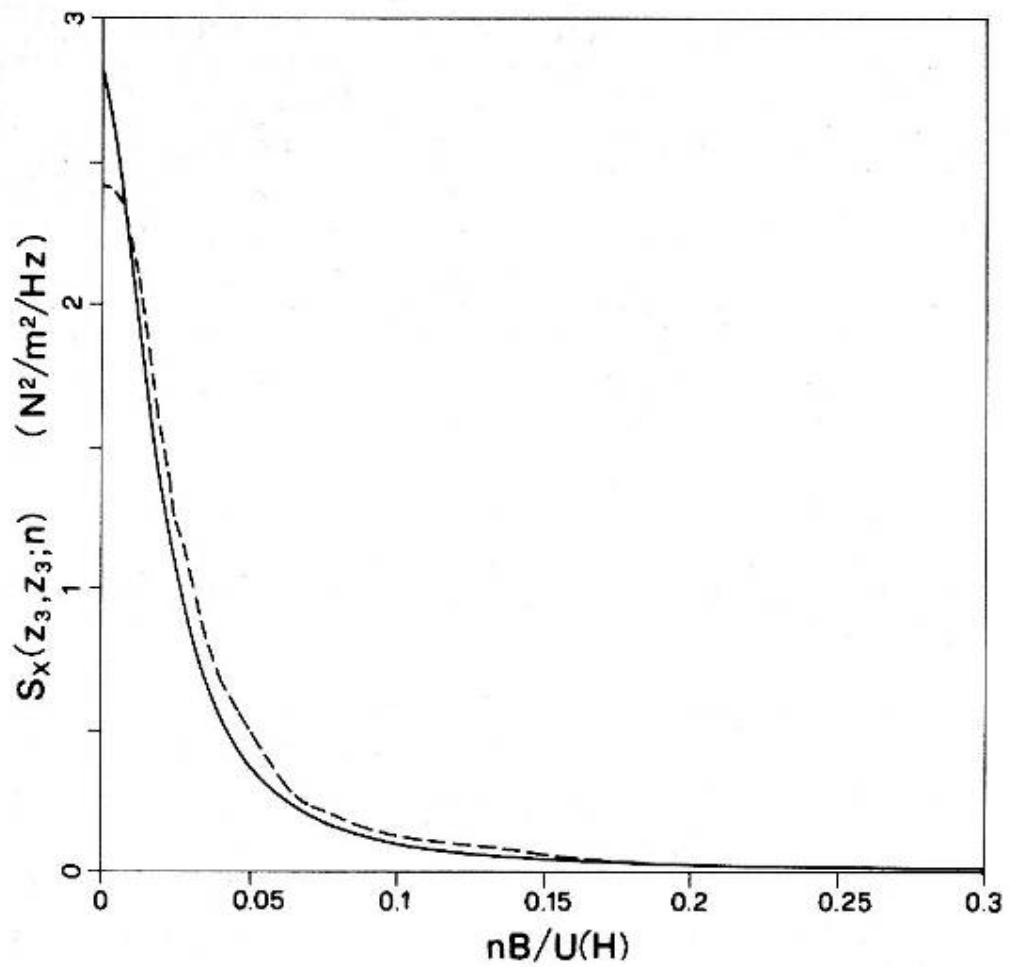
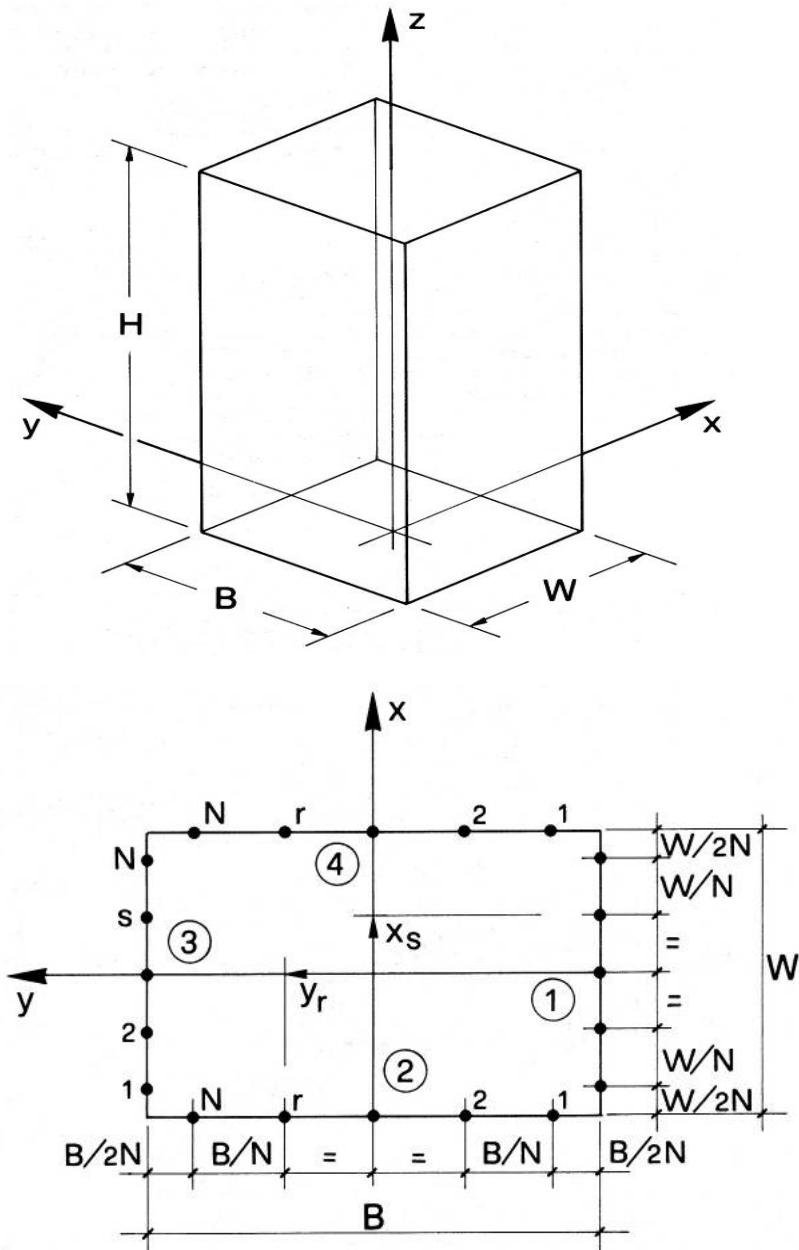


Reinhold and Sparks (1979)

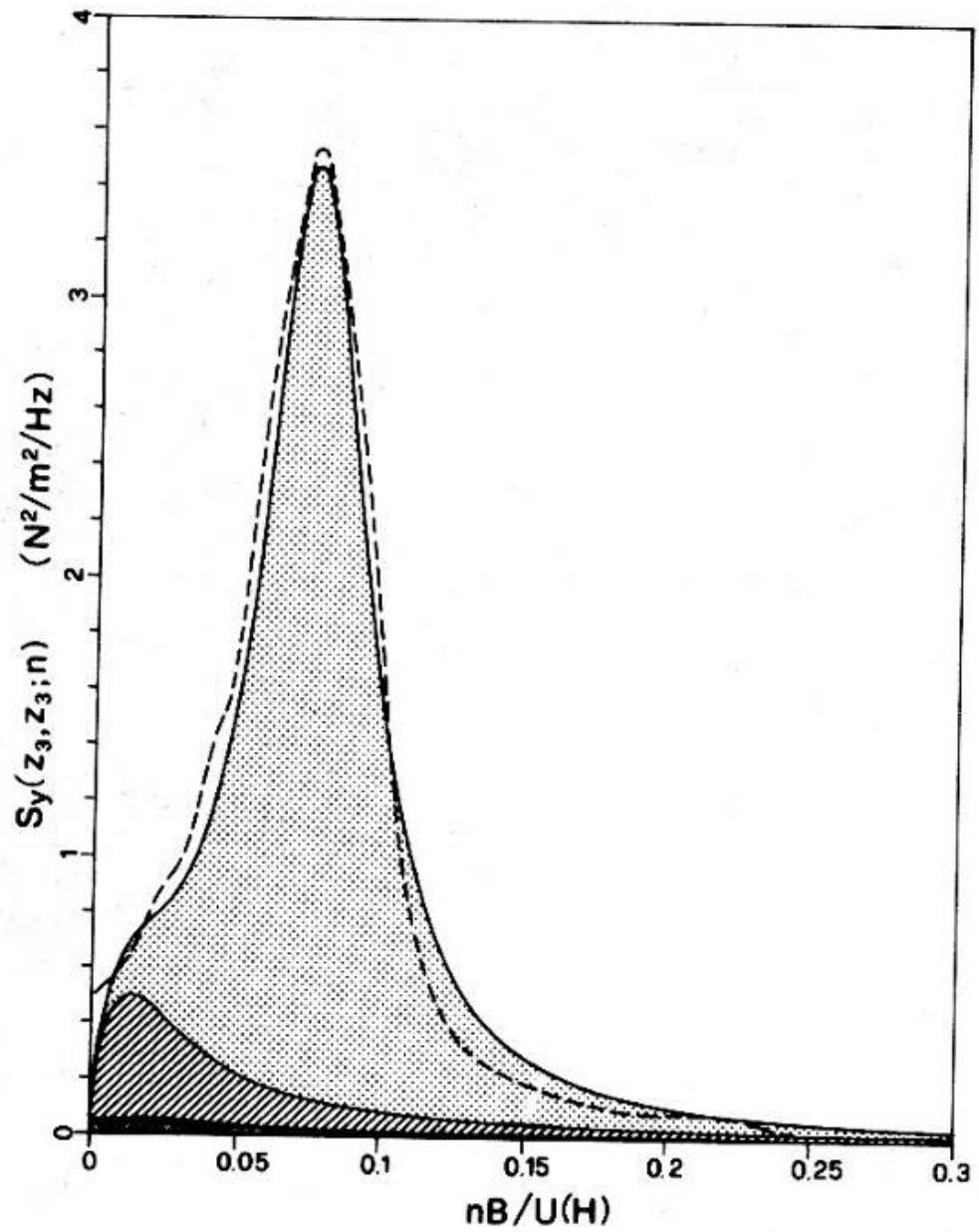
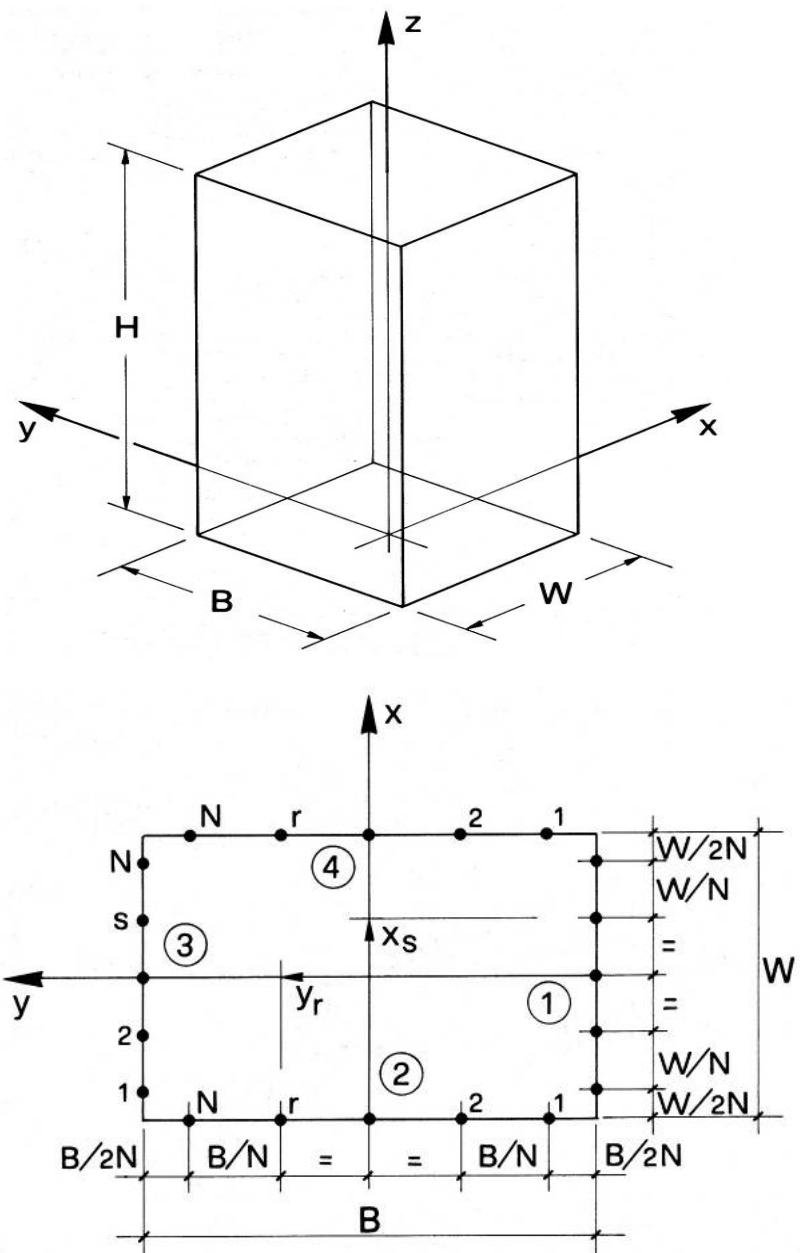
TAPS LOCATION ON SIDE FACES



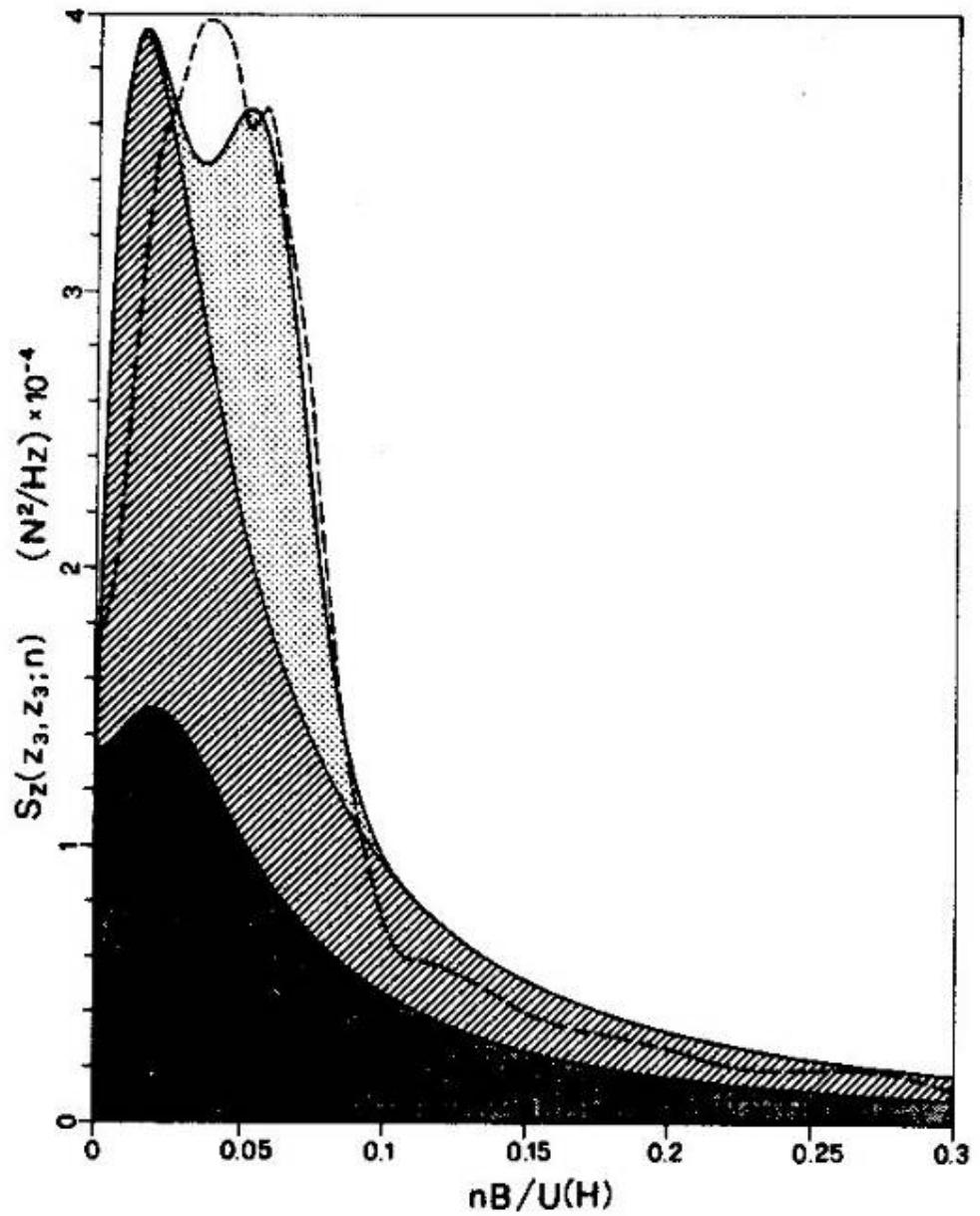
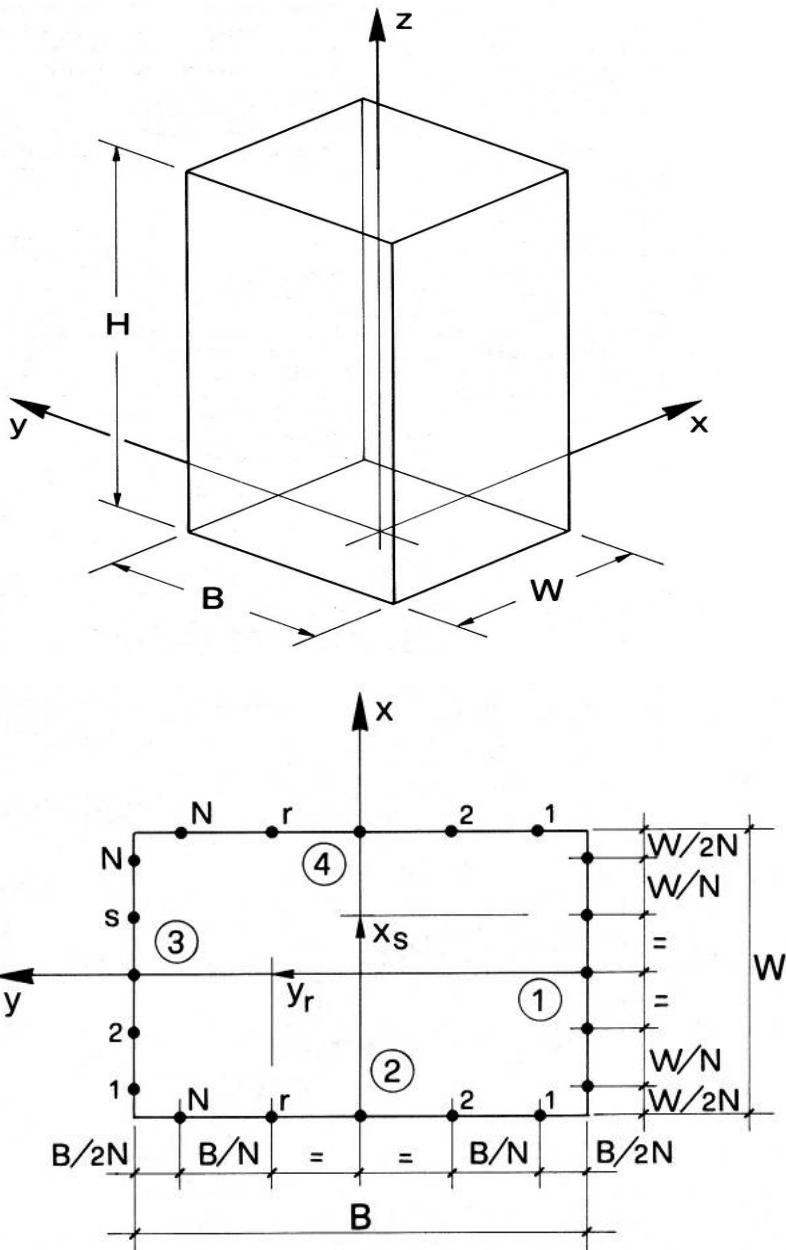
Kareem (1982)



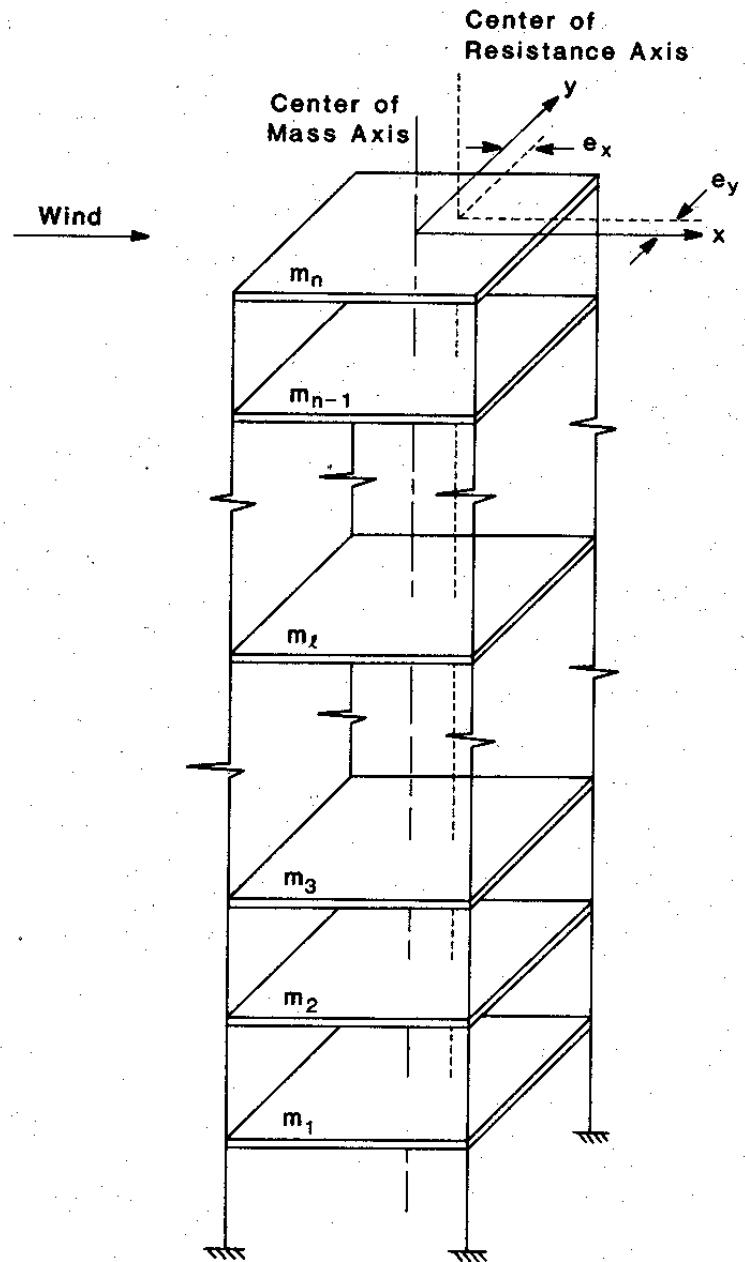
Solari (1985)



Solari (1985)



Solari (1985)



## Time Domain Solutions

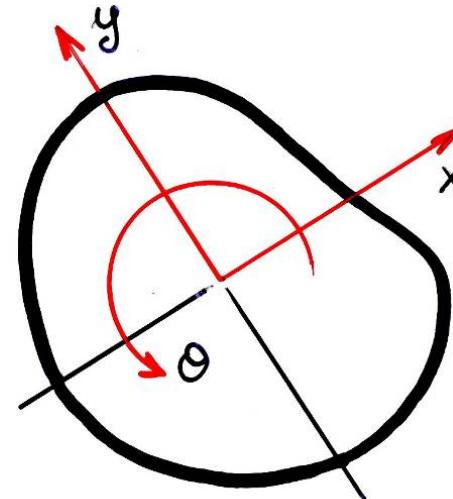
Patrickson & Friedman (1979)  
 Yang, Liu, Samali (1981)  
 Torkomani & Pramono (1985)

## Frequency Domain Solutions

Sidarous & Vanderbilt (1979)  
 Foutch & Safak (1981, 1987)  
 Kareem (1981, 1985)  
 Reinhold (1983)  
 Tallin & Ellingwood (1984)  
 Solari (1986)

3D wind-excited response

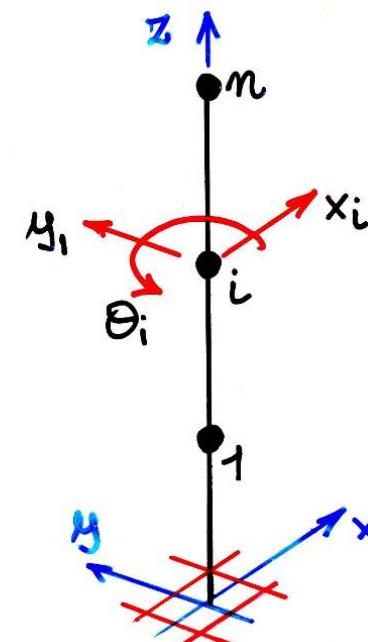
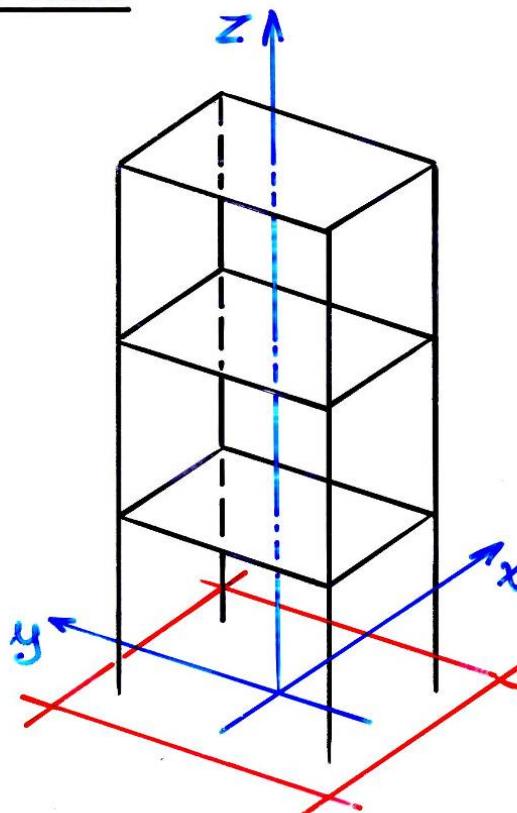
Rigid cylinder of infinite length in bi-dimensional flow



3 D.O.F.

$$\mathbf{q}_i = \begin{Bmatrix} x \\ y \\ \theta \end{Bmatrix}$$

3-D Building in the ABL



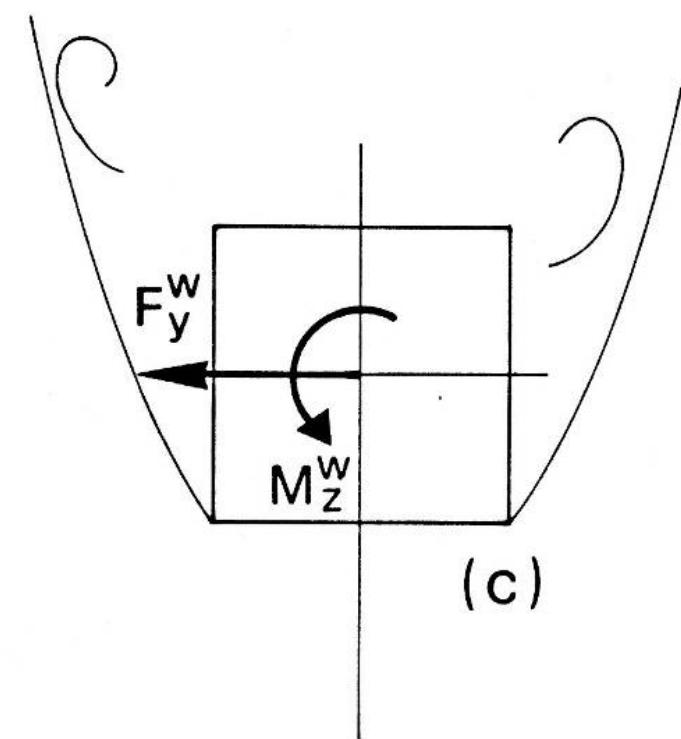
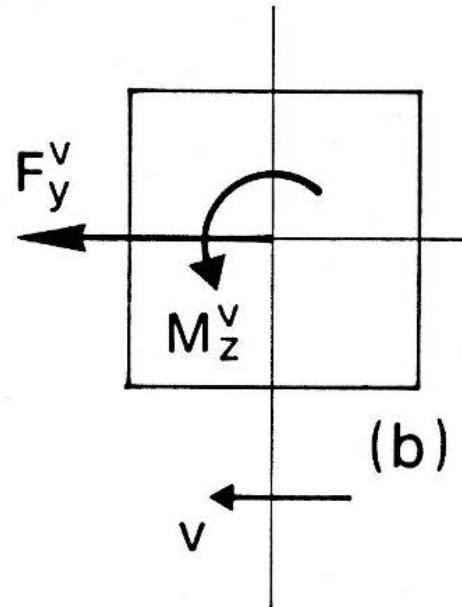
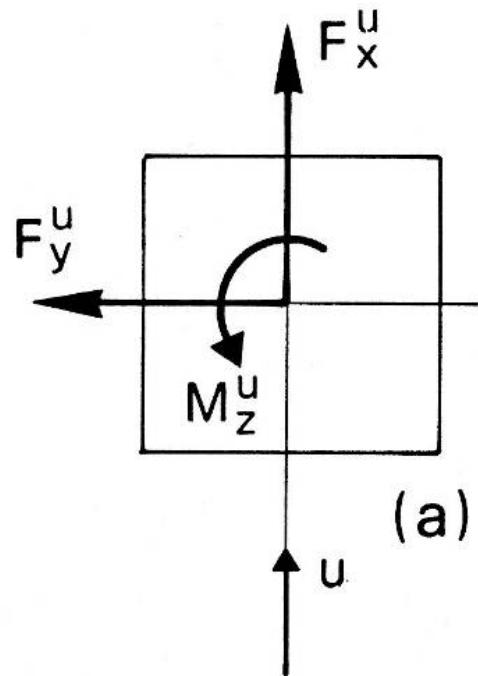
$N=3n$  D.O.F.

$$\mathbf{Q}_i = \begin{Bmatrix} x_1 & y_1 & \theta_1 \\ \vdots & \vdots & \vdots \\ x_i & y_i & \theta_i \\ \vdots & \vdots & \vdots \\ x_n & y_n & \theta_n \end{Bmatrix}$$

Computer program WL3D - Solari (1986)

FLUCTUATING WIND LOADS ARE CONSIDERED TO BE THE SUM OF THREE MAIN CONTRIBUTIONS ASSUMED AS STATISTICALLY INDEPENDENT:

- (a) FORCES DUE TO ALONG-WIND TURBULENCE;
- (b) FORCES DUE TO ACROSS-WIND TURBULENCE;
- (c) FORCES DUE TO WAKE EXCITATION



BUILDINGS SELECTED AS TEST CASES

DESCRIPTION	UNITS	BUILDING 1	BUILDING 2
HEIGHT OF BUILDING (H)	M	200	300
WIDTH OF BUILDING (B)	M	50	50
DEPTH OF BUILDING (W)	M	50	50
MASS PER UNIT LENGTH	KG/M	500 000	500 000
POLAR MASS MOMENT OF INERTIA PER UNIT LENGTH	KG M	22 500 000	22 500 000
ALONG-WIND NATURAL FREQUENCY	Hz	0.2	0.1
ACROSS-WIND NATURAL FREQUENCY	Hz	0.2	0.1
TORSIONAL NATURAL FREQUENCY	Hz	0.25	0.125
DAMPING RATIO	%	1	1

GEOMETRIC, ELASTIC AND MASS CENTRES OF BUILDINGS ARE ASSUMED AS COINCIDENT

STANDARD DEVIATIONS OF TOP FLOOR DISPLACEMENTS (M,RAD)

	BUILDING 1			BUILDING 2		
	$\sigma_{x0}^{(0)}$	$\sigma_{y0}^{(0)}$	$\sigma_{\vartheta 0}^{(0)}$	$\sigma_{x0}^{(0)}$	$\sigma_{y0}^{(0)}$	$\sigma_{\vartheta 0}^{(0)}$
u	0.029	0.019	0.00049	0.170	0.091	0.0024
u + v	0.029	0.049	0.00091	0.170	0.250	0.0047
u + v + w	0.029	0.073	0.00093	0.170	0.718	0.0048

STANDARD DEVIATIONS OF TOP FLOOR ACCELERATIONS (M/S<sup>2</sup>,RAD/S<sup>2</sup>)

	BUILDING 1			BUILDING 2		
	$\sigma_{x0}^{(2)}$	$\sigma_{y0}^{(2)}$	$\sigma_{\vartheta 0}^{(2)}$	$\sigma_{x0}^{(2)}$	$\sigma_{y0}^{(2)}$	$\sigma_{\vartheta 0}^{(2)}$
u	0.036	0.028	0.00110	0.061	0.035	0.00140
u + v	0.036	0.074	0.00210	0.061	0.096	0.00280
u + v + w	0.036	0.102	0.00210	0.061	0.273	0.00280

Computer program WL3D - Solari (1986)

RATIOS BETWEEN CORNER (C) AND CENTRE (O) DISPLACEMENT STANDARD DEVIATIONS

	BUILDING 1		BUILDING 2	
	$\sigma_{xc}^{(0)} / \sigma_{xo}^{(0)}$	$\sigma_{yc}^{(0)} / \sigma_{yo}^{(0)}$	$\sigma_{xc}^{(0)} / \sigma_{xo}^{(0)}$	$\sigma_{yc}^{(0)} / \sigma_{yo}^{(0)}$
u	1.08	1.19	1.06	1.20
u + v	1.27	1.12	1.22	1.11
u + v + w	1.28	1.07	1.23	1.02

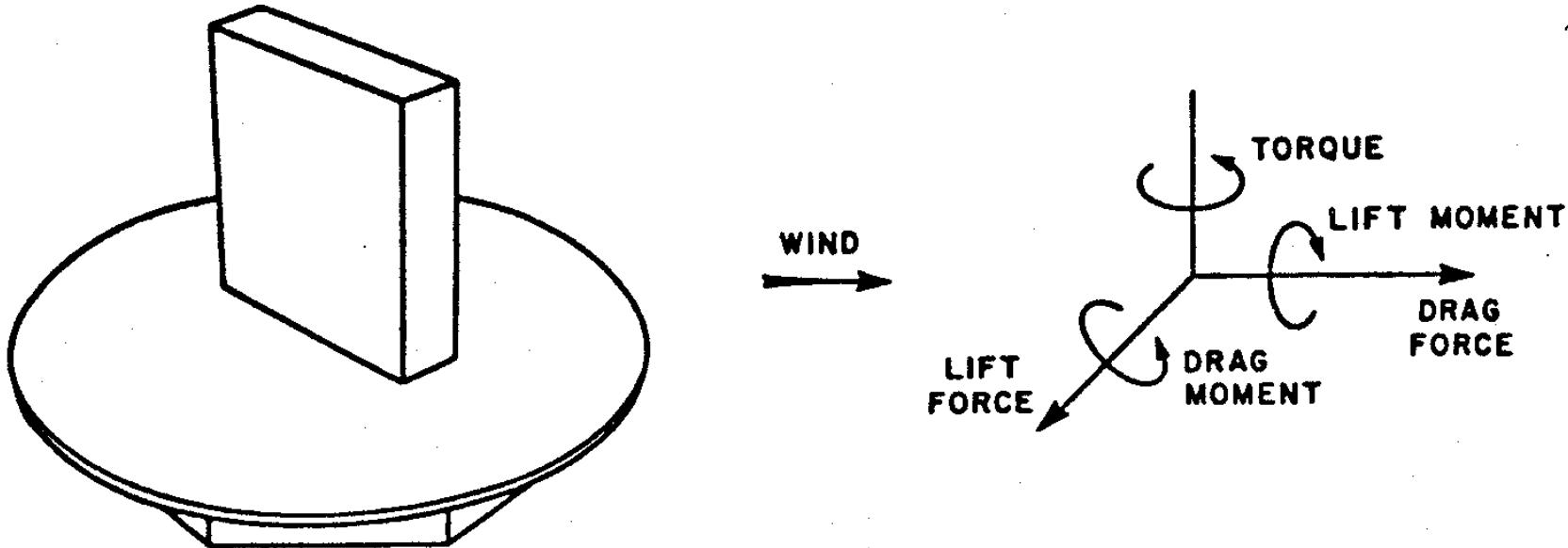
RATIOS BETWEEN CORNER (C) AND CENTRE (O) ACCELERATION STANDARD DEVIATIONS

	BUILDING 1		BUILDING 2	
	$\sigma_{xc}^{(2)} / \sigma_{xo}^{(2)}$	$\sigma_{yc}^{(2)} / \sigma_{yo}^{(2)}$	$\sigma_{xc}^{(2)} / \sigma_{xo}^{(2)}$	$\sigma_{yc}^{(2)} / \sigma_{yo}^{(2)}$
u	1.27	1.44	1.16	1.45
u + v	1.77	1.24	1.53	1.25
u + v + w	1.77	1.13	1.53	1.04

Computer program WL3D - Solari (1986)



High-frequency force balance measurements



## Base overturning moment

$$M(t) = \int_0^H f(z, t) z dz$$

$$\bar{M} = \int_0^H \bar{f}(z) z dz$$

$$S_M(n) = \int_0^H \int_0^H S_f(z, z'; n) z z' dz dz'$$

coincides with the modal force for a linear mode shape

Davenport and Tschanz (1981, 1983)

## High-frequency force-balance wind-tunnel tests

$$\bar{C}_M = \frac{2\bar{M}}{\rho \bar{u}^2 B H^2}; \quad \tilde{C}_M = \frac{2\sigma_M}{\rho \bar{u}^2 B H^2}; \quad \frac{n S_M(n)}{\sigma_M^2} = f\left(\frac{nB}{\bar{u}}\right)$$

Alongwind response • linear mode shape  $\Psi_1(z) = z$

$$X(z; t) = z \cdot P_1(t); \quad P_1(t) = \bar{P}_1 + P'_1(t)$$

$$\bar{P}_1 = \frac{\bar{F}_1}{m_1(2\pi n_1)^2}; \quad m_1 = \int_0^H \mu(z) z^2 dz$$

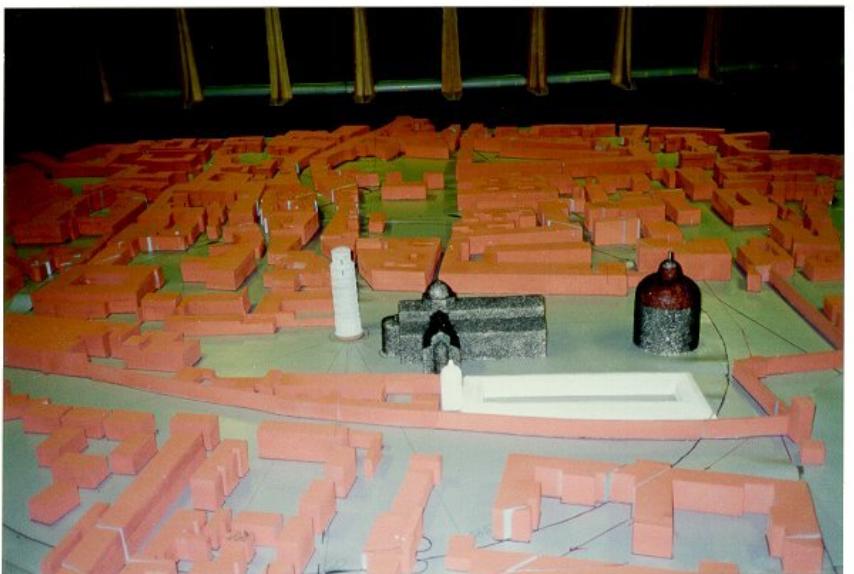
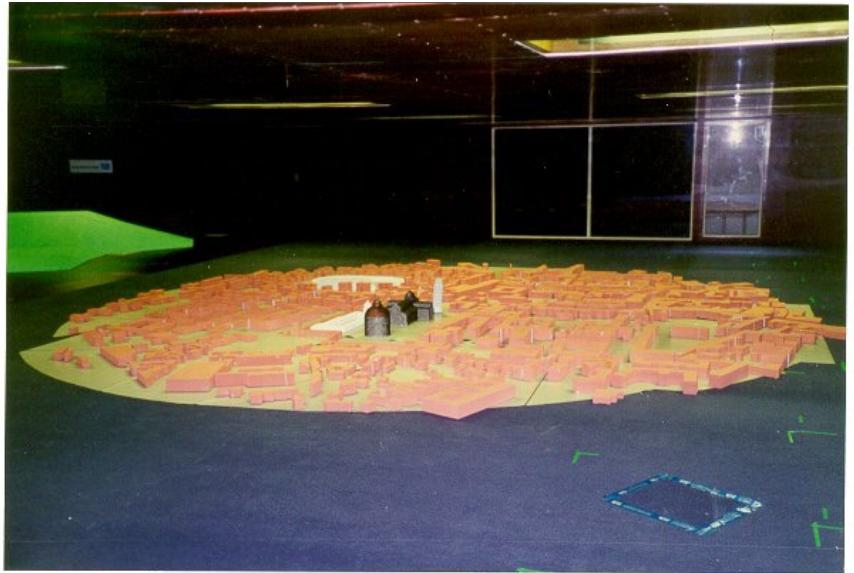
$$\bar{F}_1 = \int_0^H \bar{F}(z) z dz = \bar{M} = \frac{1}{2} \rho \bar{u}^2 B H^2 \bar{C}_M$$

$$\sigma_{P_1}^2 = \sigma_{QP_1}^2 + \sigma_{DP_1}^2$$

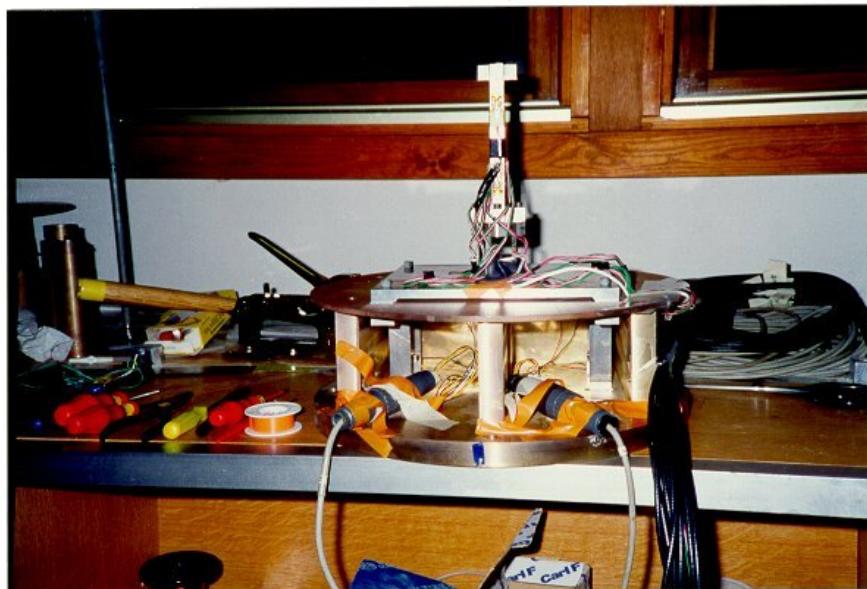
$$\sigma_{QP_1}^2 = \frac{\sigma_{F_1}^2}{m_1^2 (2\pi n_1)^4}; \quad \sigma_{F_1} = \sigma_M = \frac{1}{2} \rho \bar{u}^2 B H^2 \tilde{C}_M$$

$$\sigma_{DP_1}^2 = \frac{1}{m_1^2 (2\pi n_1)^4} \frac{\pi m_1}{4\xi} S_{F_1}(n_1)$$

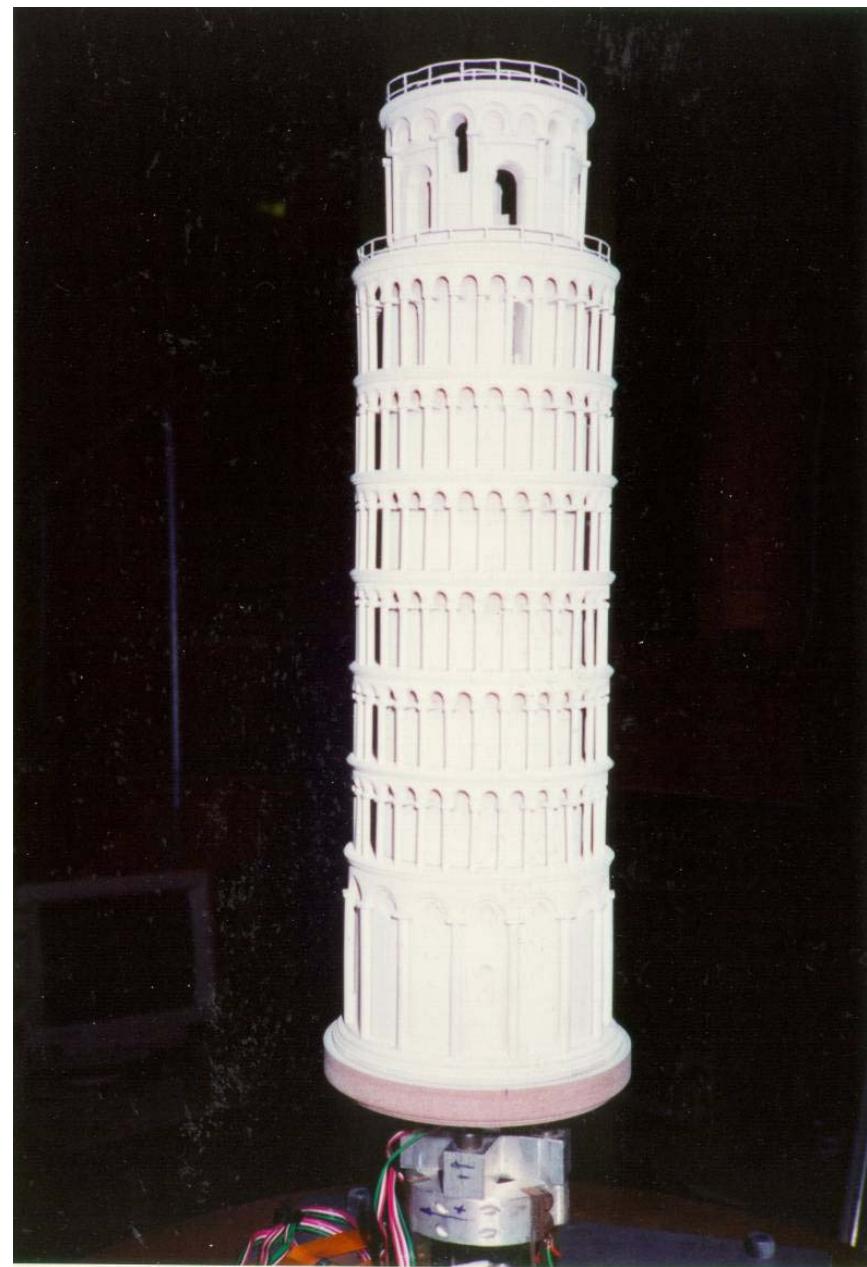
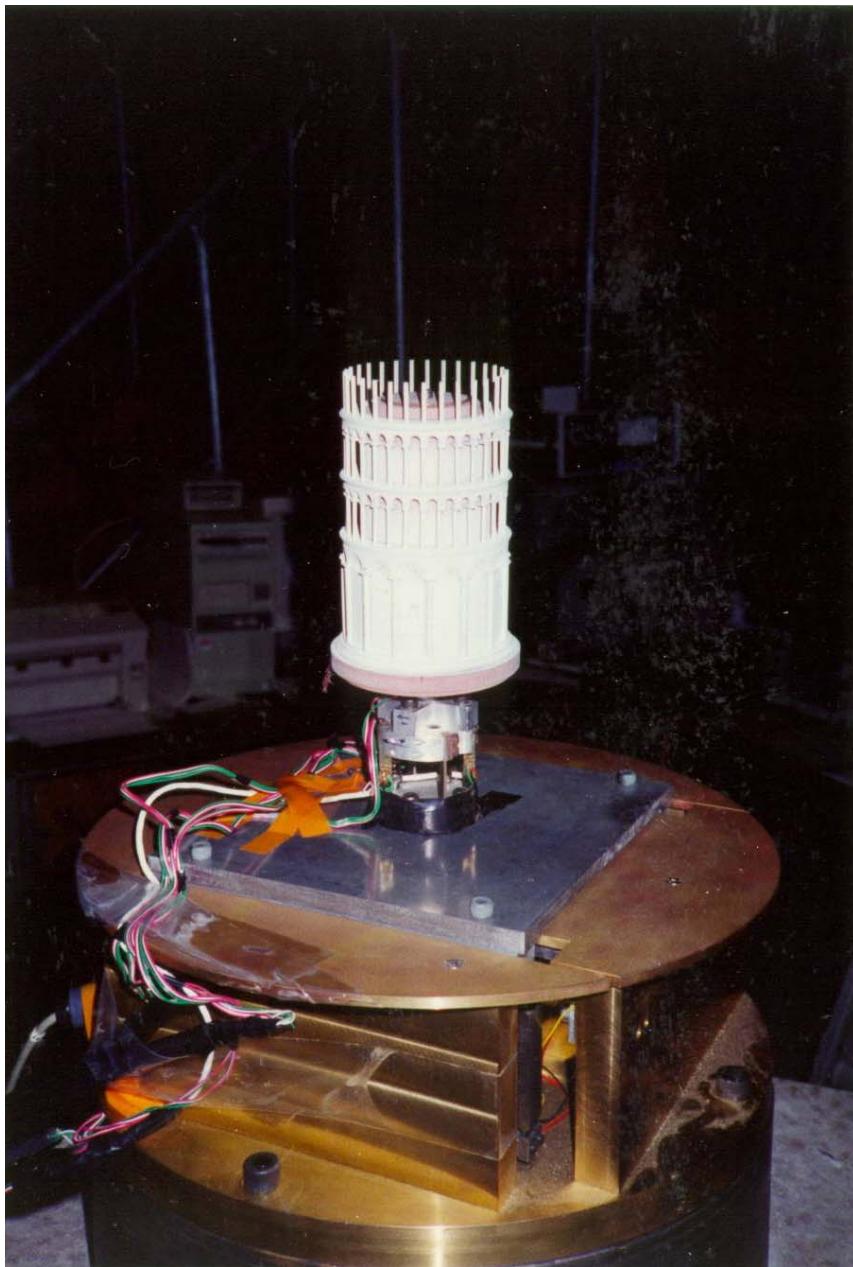
$$S_{F_1}(n) = \int_0^H \int_0^H S_{F'F'}(z, z'; n) z z' dz dz' = S_M(n) = \frac{\sigma_M^2}{n} f\left(\frac{nB}{\bar{u}}\right)$$



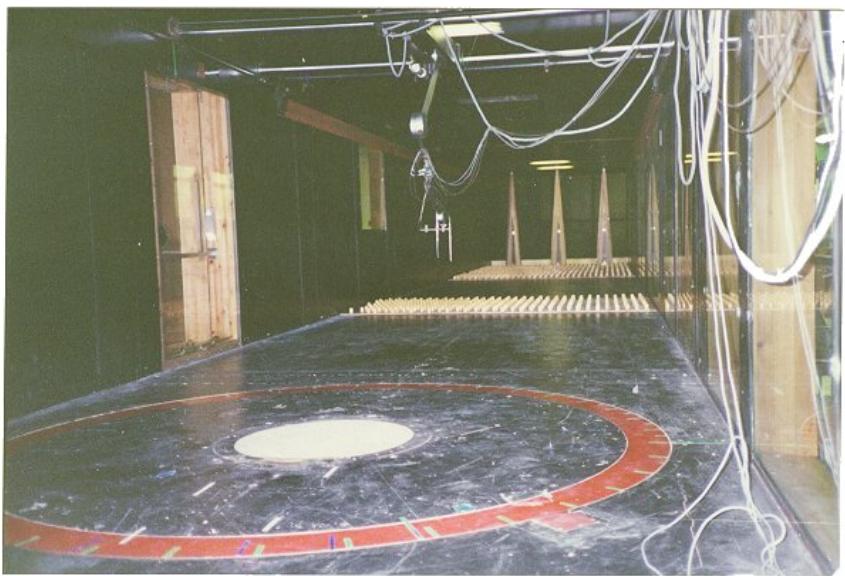
High-frequency force balance tests on the Leaning Tower of Pisa



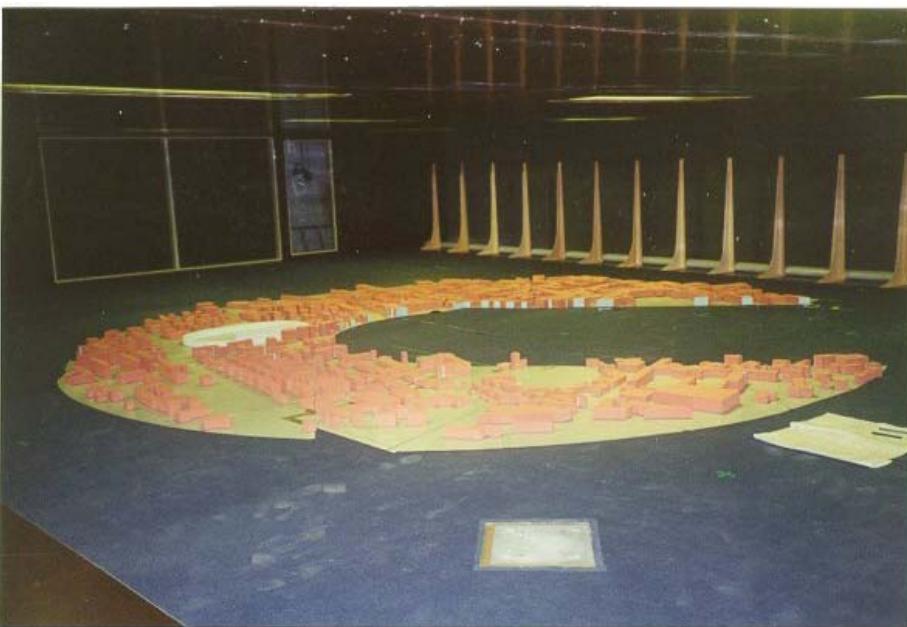
High-frequency force balance tests on the Leaning Tower of Pisa



High-frequency force balance tests on the Leaning Tower of Pisa



High-frequency force balance tests on the Leaning Tower of Pisa

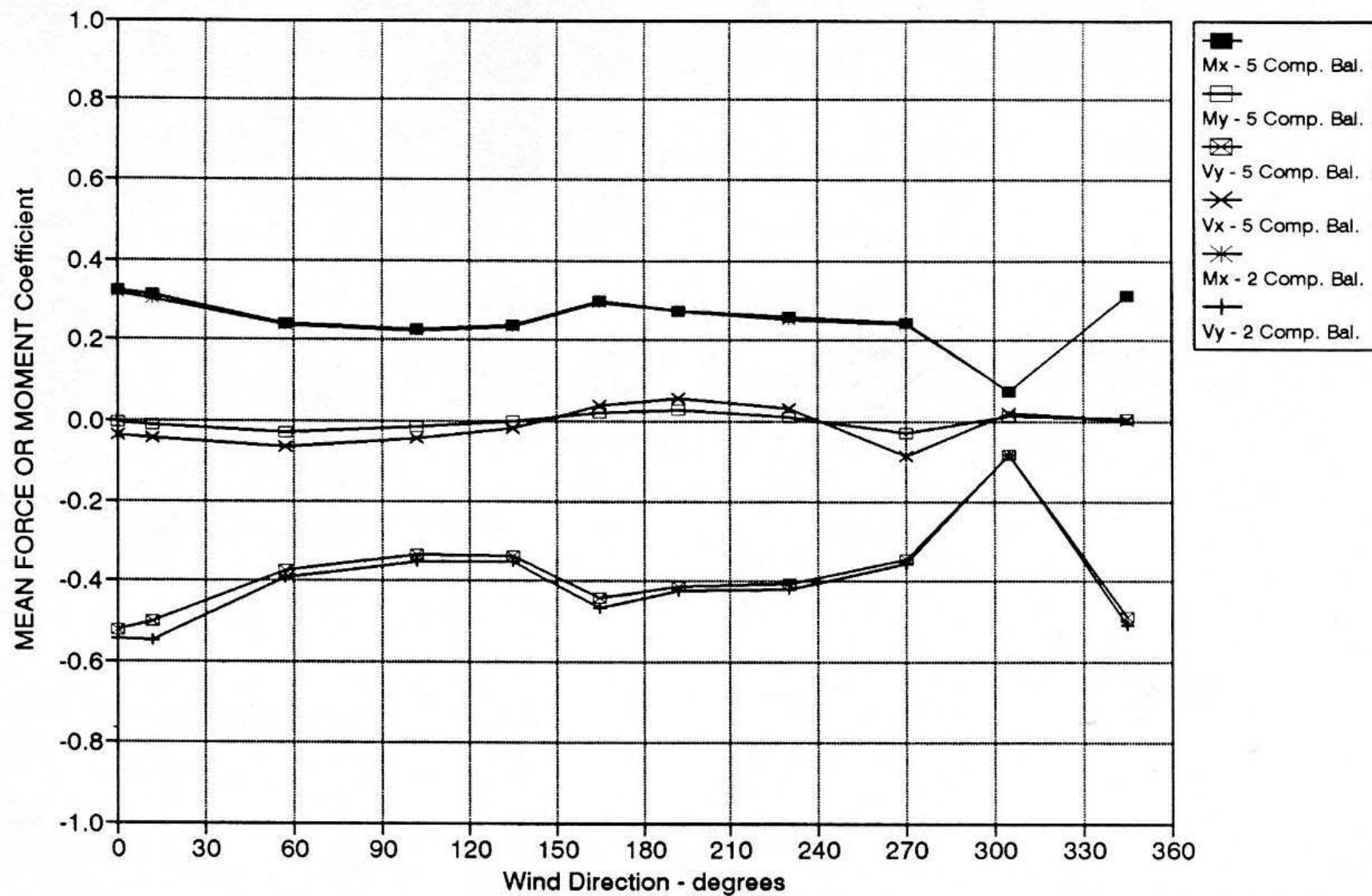


High-frequency force balance tests on the Leaning Tower of Pisa



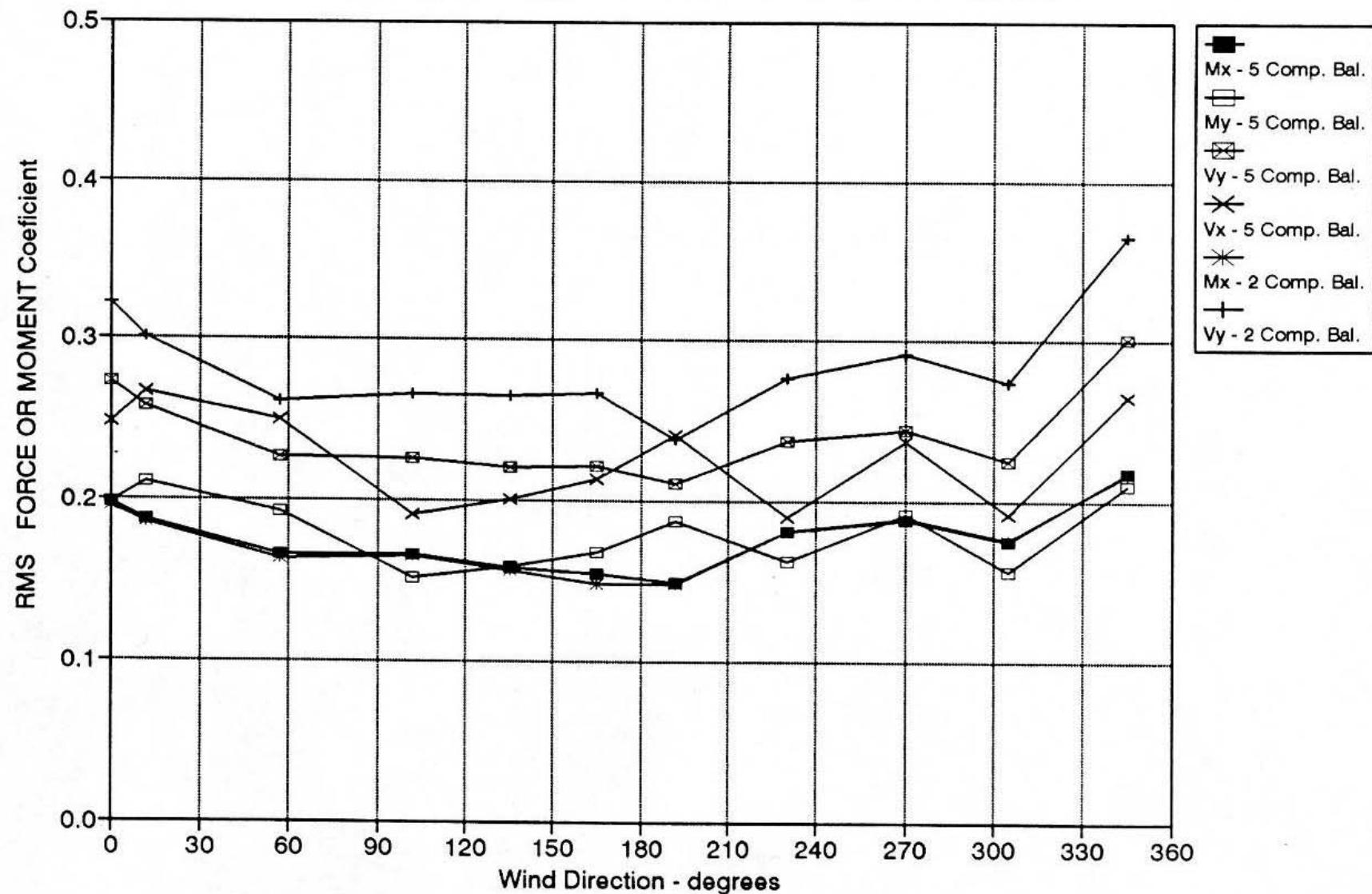
High-frequency force balance tests on the Leaning Tower of Pisa

## WIND TUNNEL TESTS OF PISA TOWER MEAN FORCE OR MOMENT COEFFICIENTS



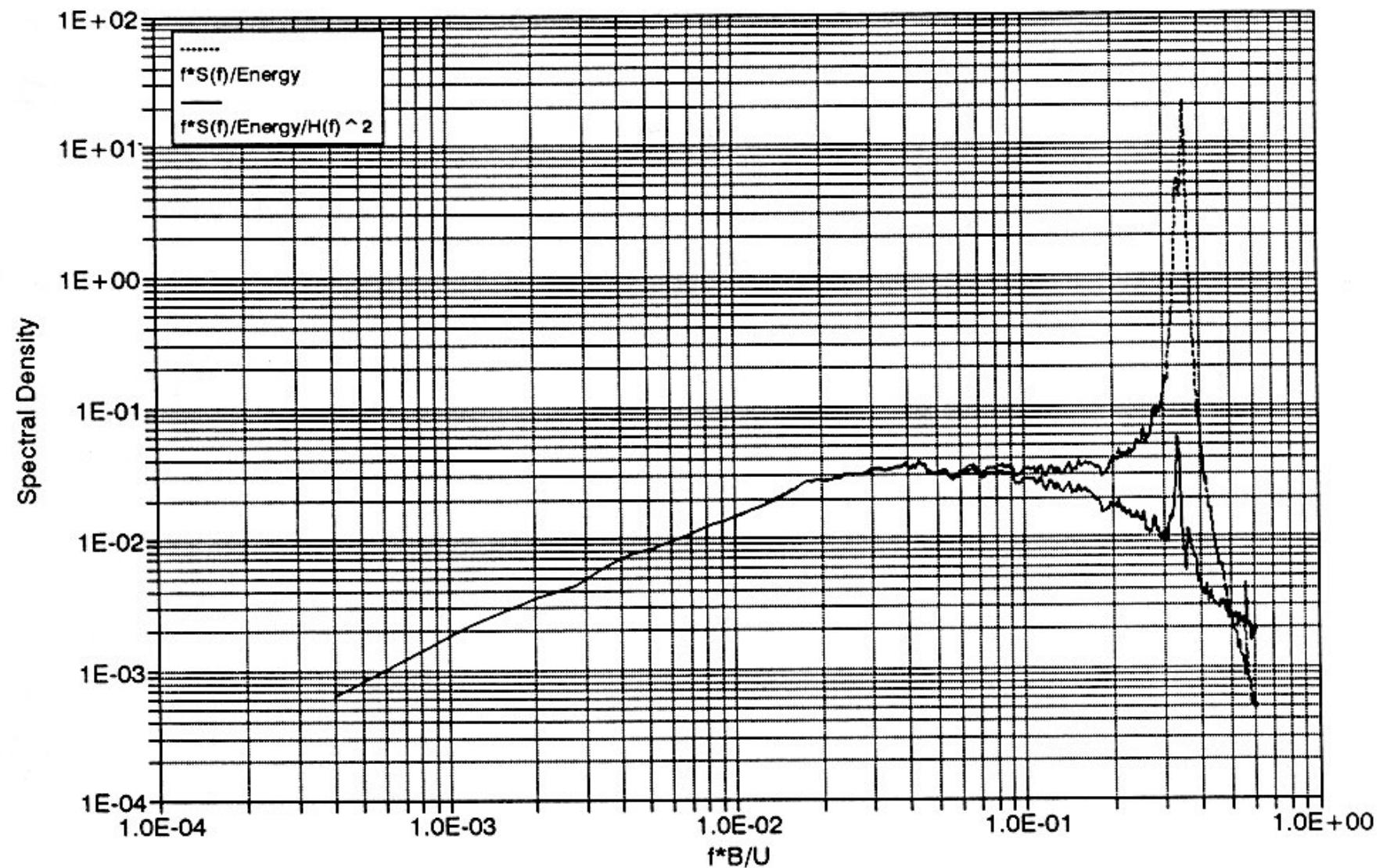
High-frequency force balance tests on the Leaning Tower of Pisa

## WIND TUNNEL TESTS OF PISA TOWER ROOT-MEAN-SQUARE FORCE OR MOMENT COEFF.



High-frequency force balance tests on the Leaning Tower of Pisa

82097JM0.308 [0], Mx Lower  
With Spike Removal, 7 pt. Smoothing



High-frequency force balance tests on the Leaning Tower of Pisa

## Correction procedures for nonlinear mode shapes

Kwok (1982)

Kareem (1984)

Vickery et al (1985)

Holmes (1987)

Boggs & Poterka (1989)

Xu & Kwok (1993)

## Procedures for determining the modal torque

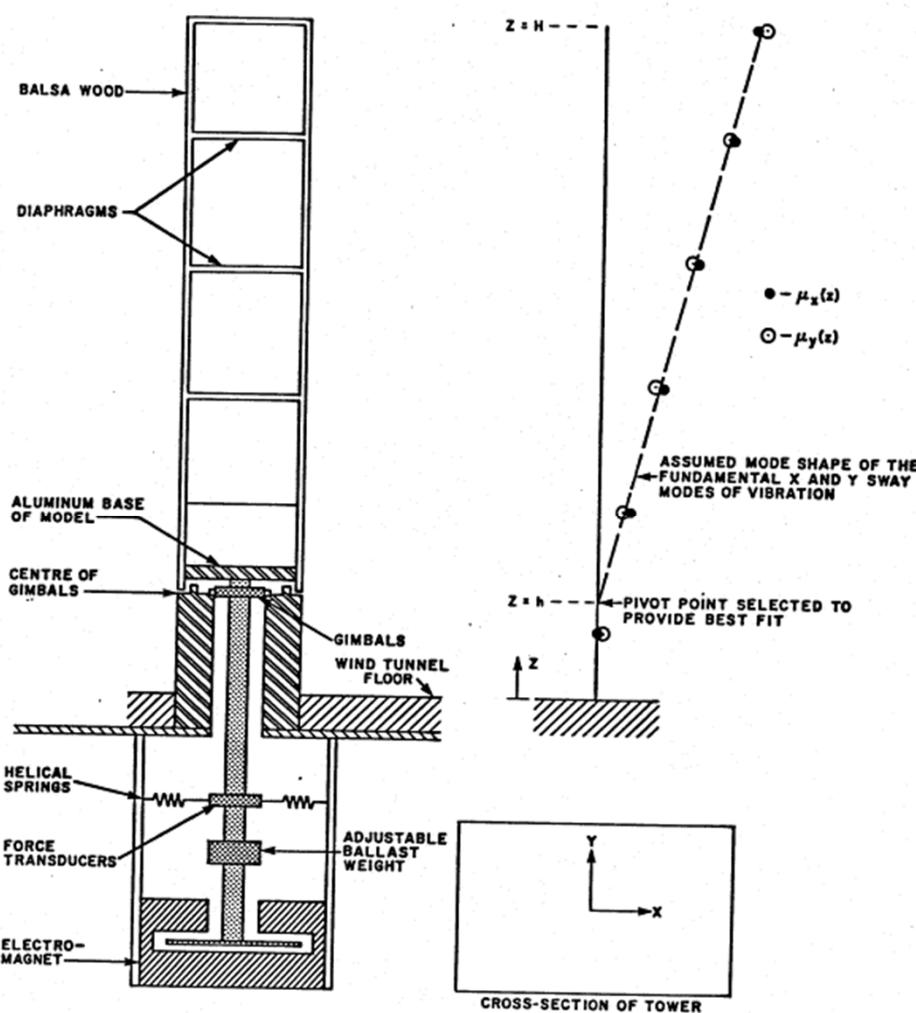
Tschanz & Davenport (1983)

Tallin & Ellingwood (1985)

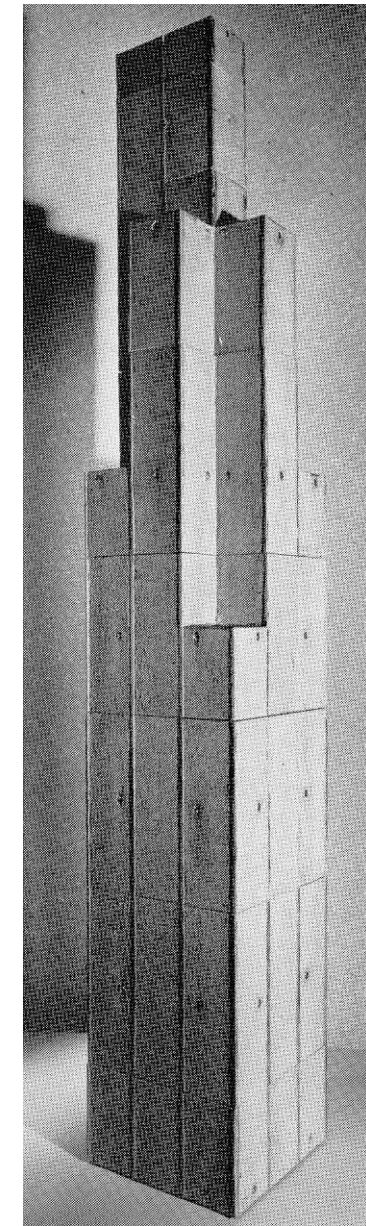
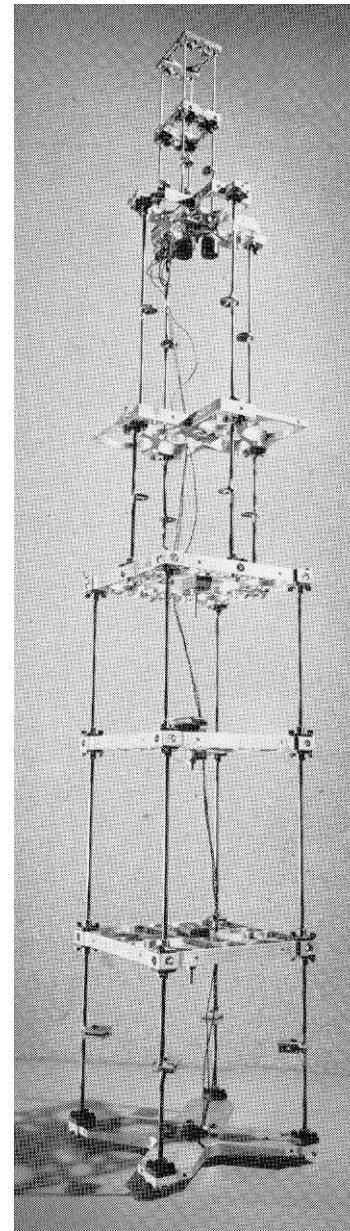
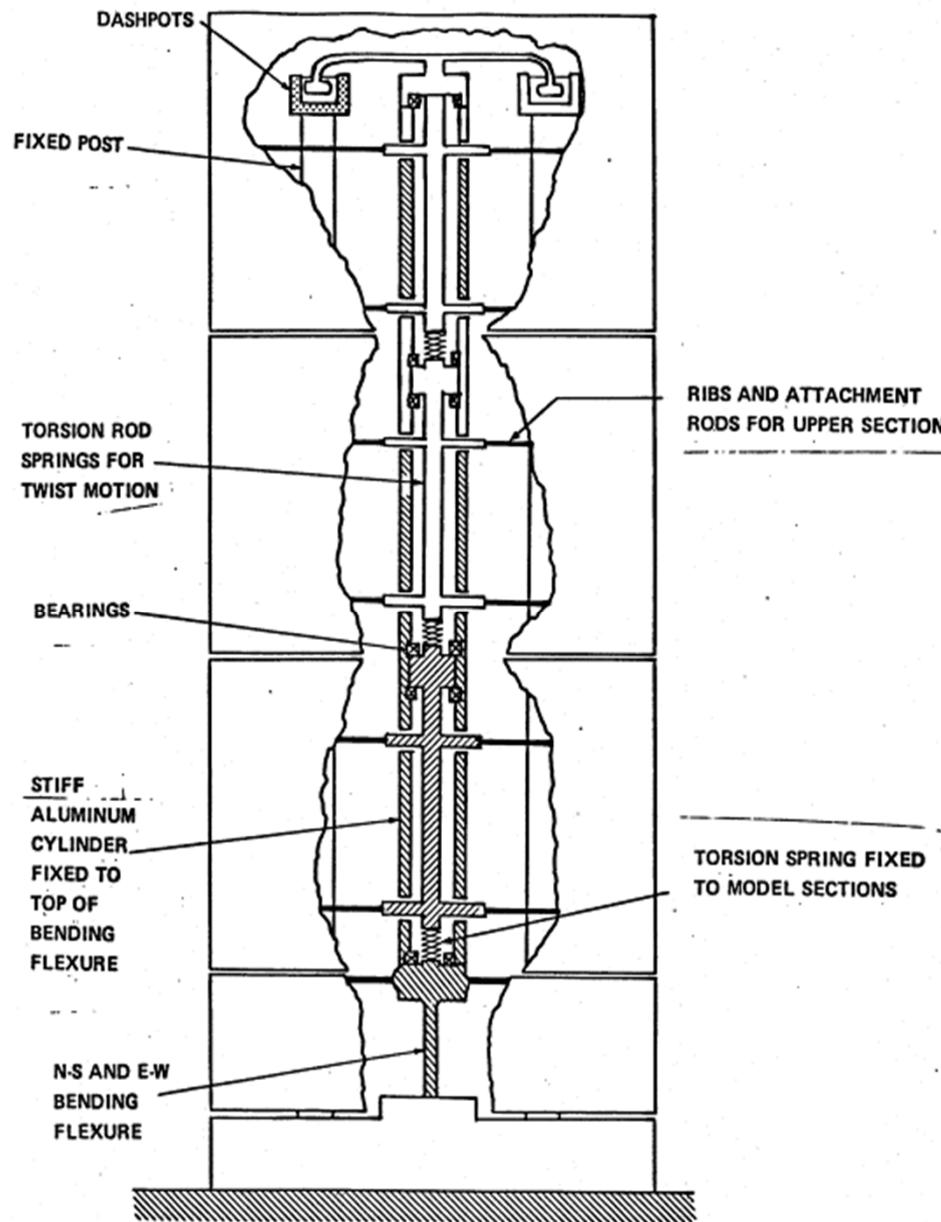
Marukawa et al (1985)

Xu & Kwok (1993)

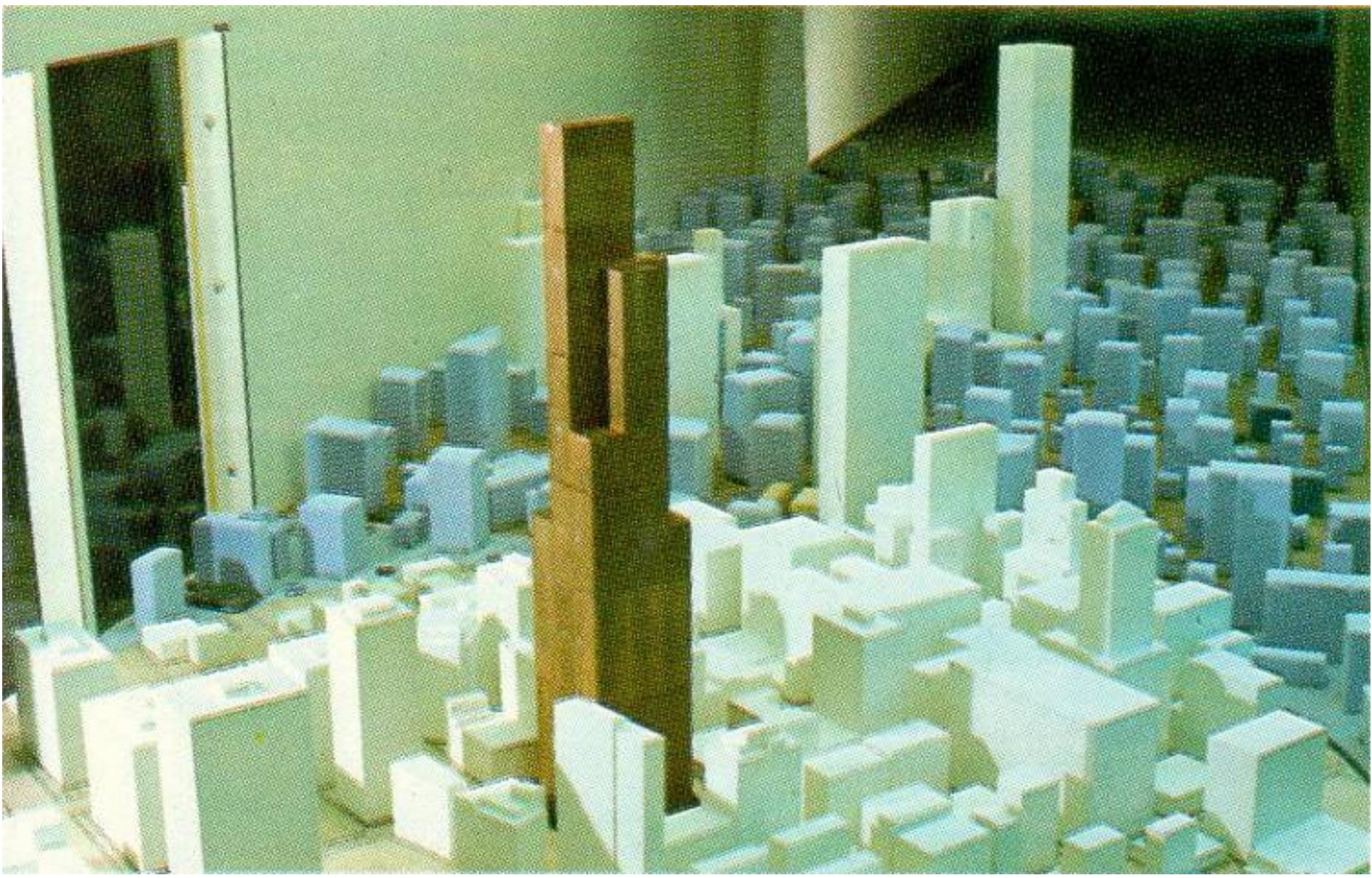
Correction techniques for non linear mode shapes



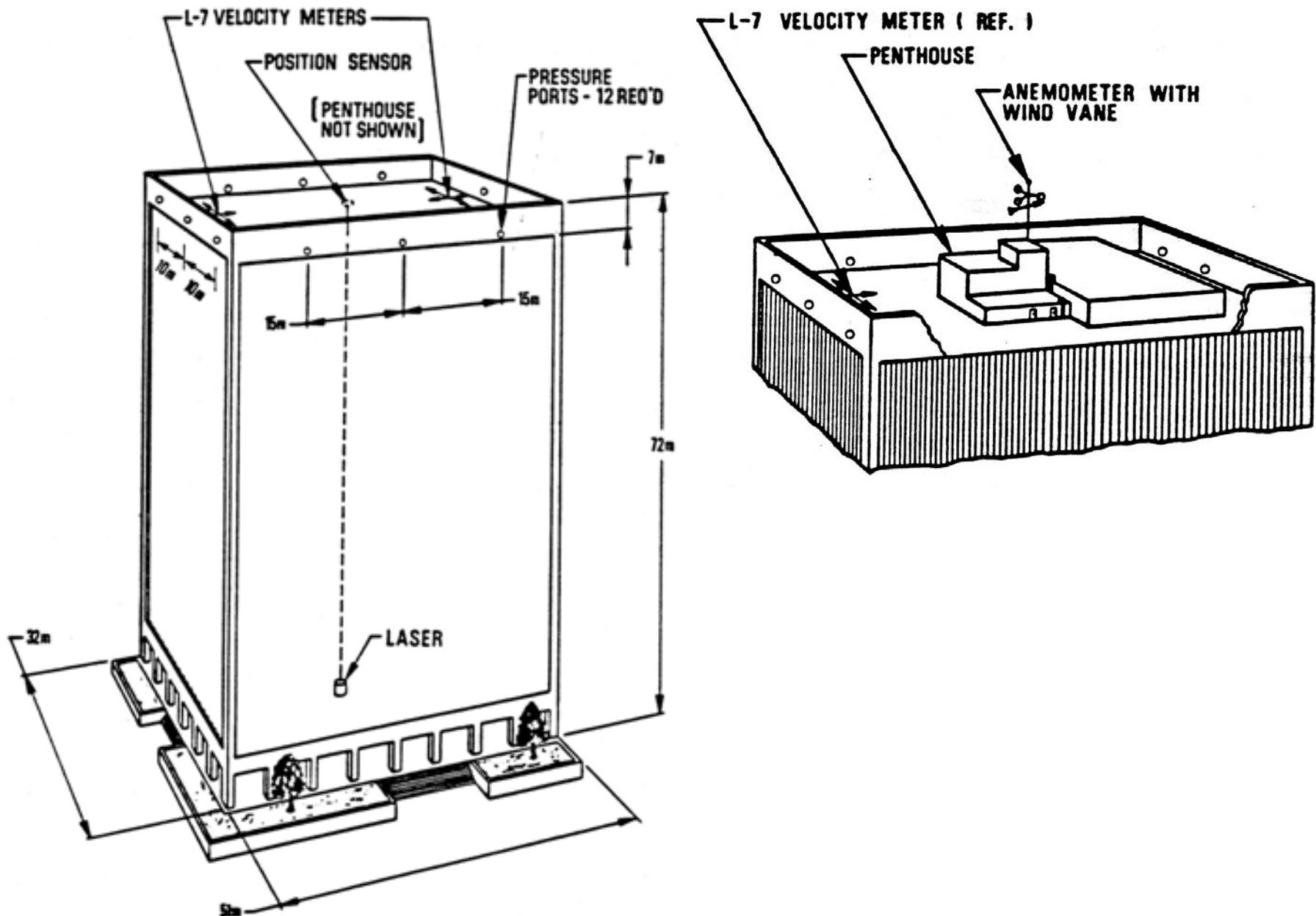
## Flexible balance aeroelastic measurements



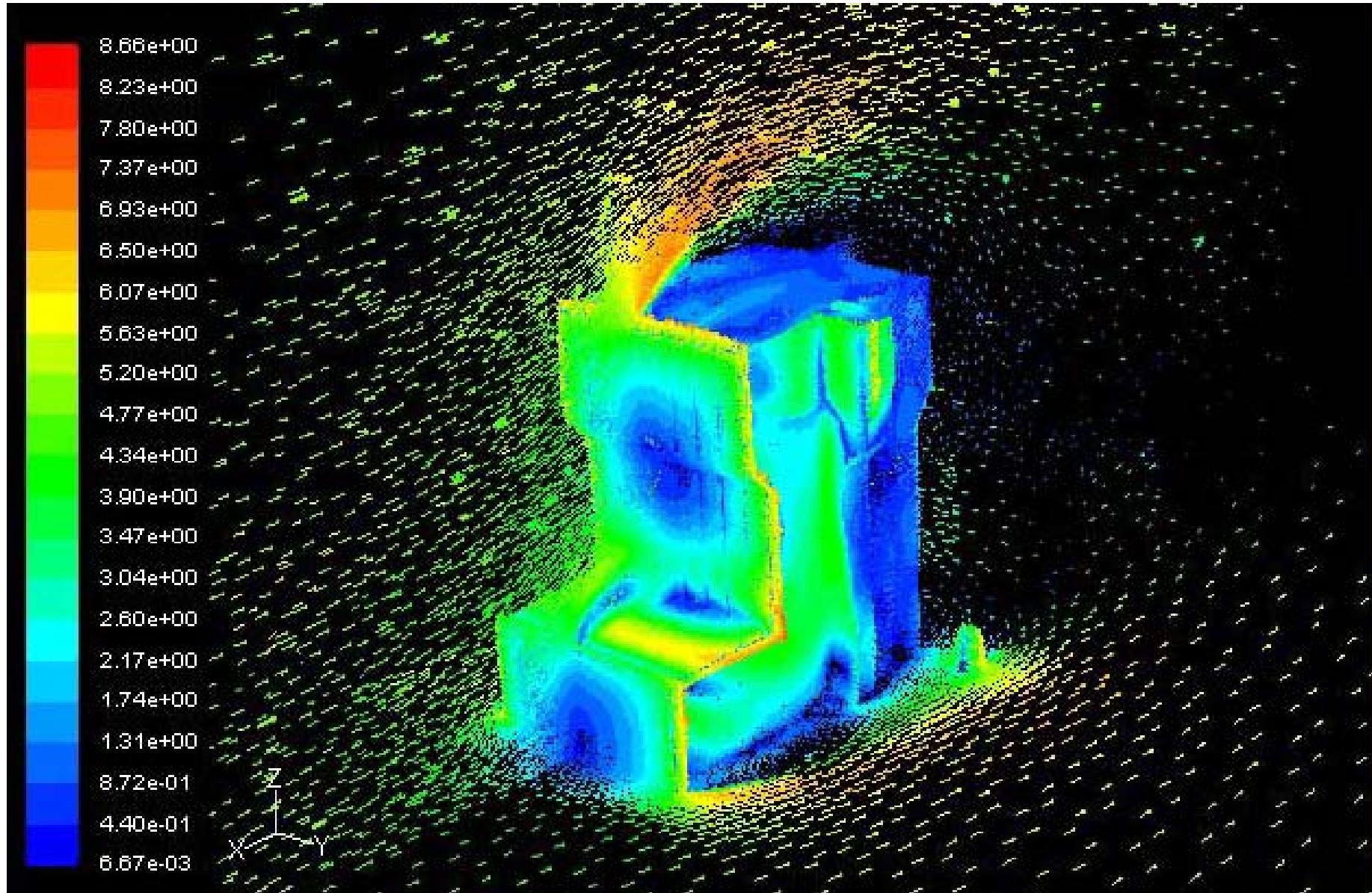
Fully aeroelastic measurements



Fully aeroelastic measurements

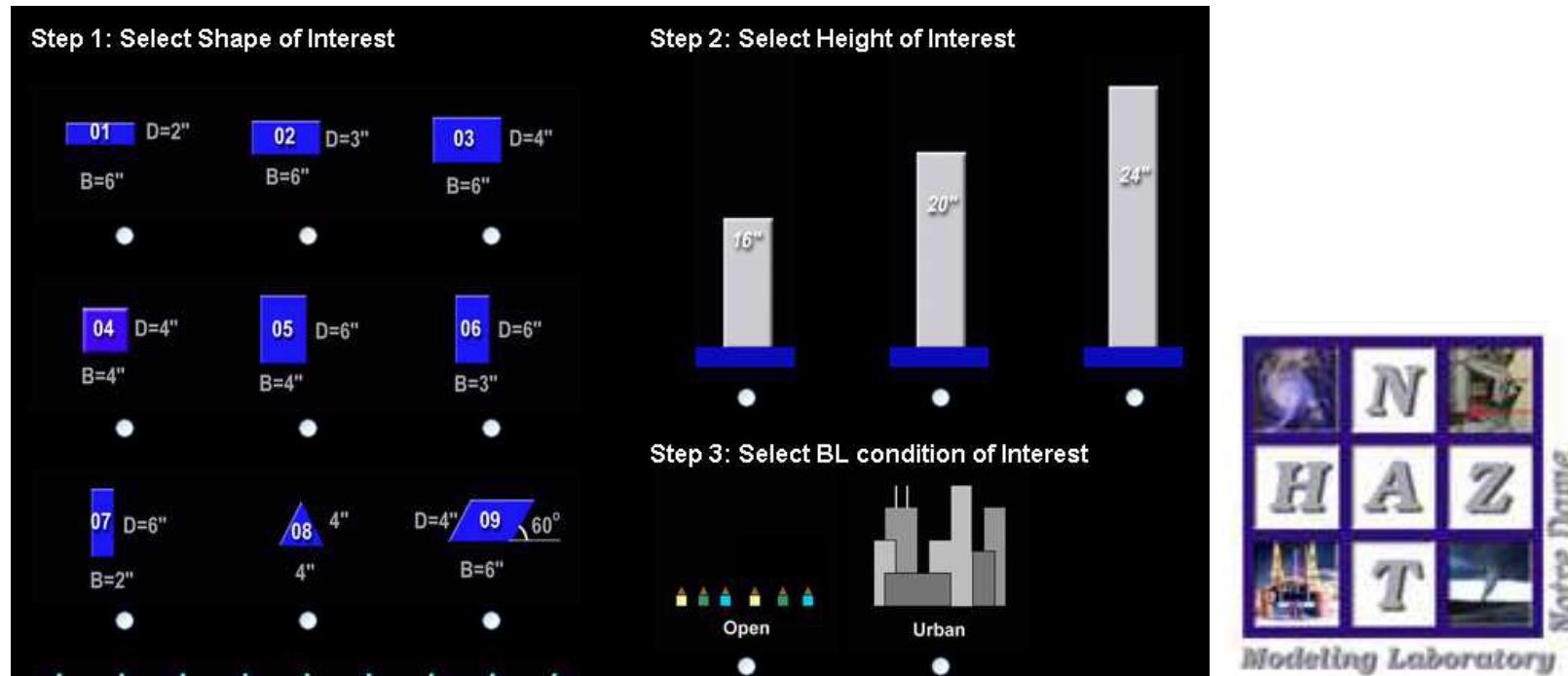


Full-scale tests



Computational Fluid Dynamics (CFD) models

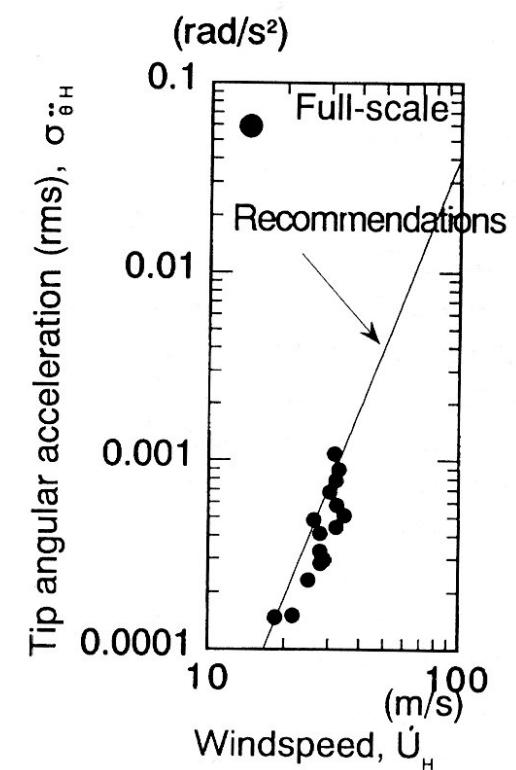
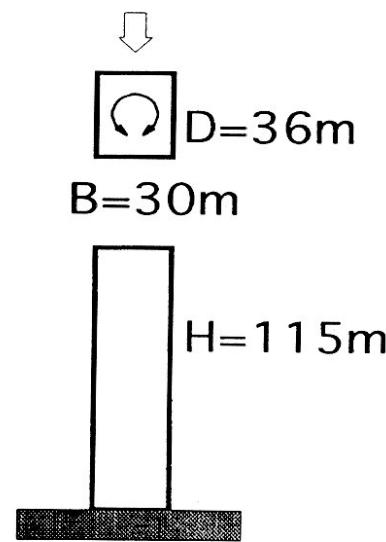
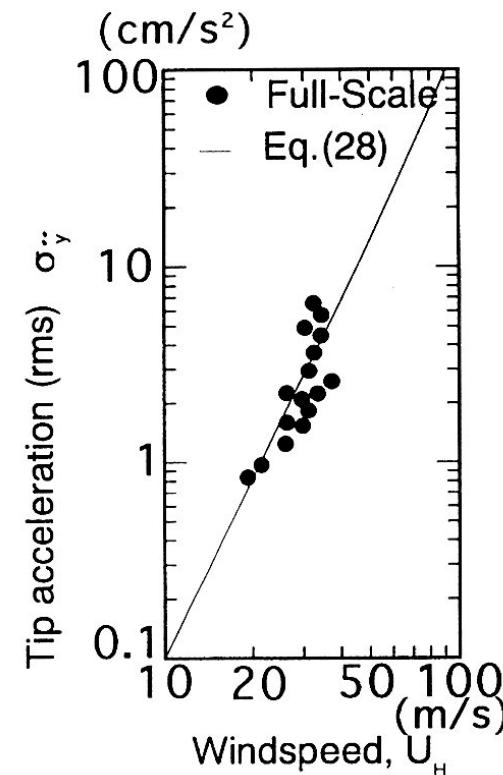
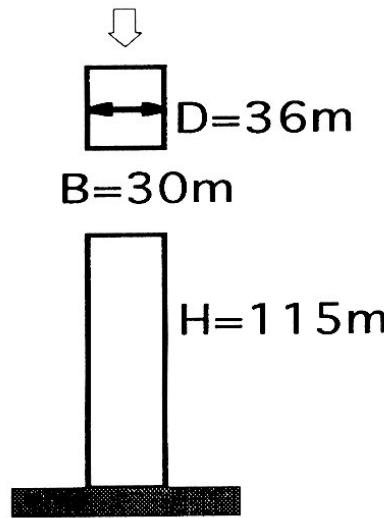
# NatHaz Aerodynamic Data Base, Notre Dame, Indiana, U.S.



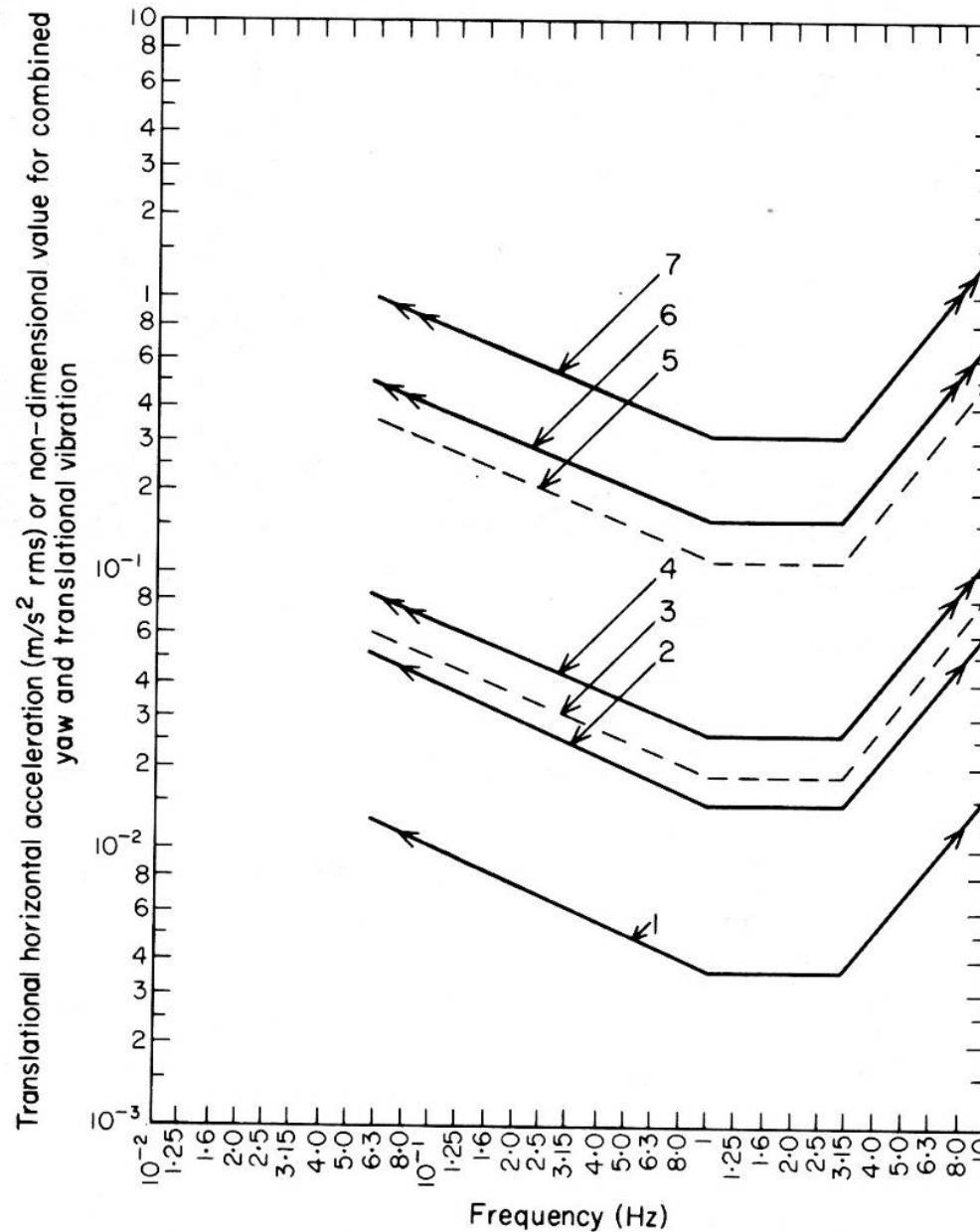
Model #	1	2	3	4	5	6	7	8	9
Shape									
D:B [in.]	2:6	3:6	4:6	4:4	6:4	6:3	6:2	4:4	4:6 (60°)

Electronic data bases

## Architectural Institute of Japan (AIJ) Recommendations (1996)



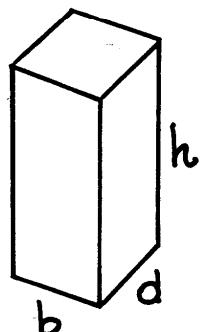
Analytical methods



1      Perceptible  
 2,3,4    Annoying  
 5,6,7    Intolerable

Human comfort criterion – Irwin (1981)

## Esempio: Edificio multipiano metallico



$V_{ref} = 26 \text{ m/s}$ ; Categoria III

$$b = d = 30 \text{ m}$$

$$1) h = 50 \text{ m} \Rightarrow M_1 = 0.92 \text{ Hz}$$

$$\delta = 0.05$$

$$2) h = 100 \text{ m} \Rightarrow M_1 = 0.46 \text{ Hz}$$

$$\delta = 0.05$$

$$3) h = 200 \text{ m} \Rightarrow M_1 = 0.23 \text{ Hz}$$

$$\delta = 0.05$$

$$\bar{R} = 5 \text{ anni} \Rightarrow V_{ref} = 26 \times 0.85 = 22.1 \text{ m/s}$$

Alongwind  
Response

	Edificio 1	Edificio 2	Edificio 3
$W(h) \text{ (N/m}^2\text{)}$	1256	1609	2088
$x_{max}(h)$	$h/6165$	$h/2371$	$h/902$
$\sigma_{\ddot{x}}(h) \text{ (m/s}^2\text{)}$	0.010	0.021	0.039

Nota:  $W, x_{max}$  calcolati per  $V_{ref} = 26 \text{ m/s}$

$\sigma_{\ddot{x}}$  calcolato per  $V_{ref} = 22.1 \text{ m/s}$

## Across-wind response (Japanese code)

$$H = 200 \text{ m}, B = D = 30 \text{ m}$$

$$V_{ref} = 26 \text{ m/s, Category 3, } z_0 = 0.1 \text{ m, } K_z = 0.2$$

$$m_1 = 0.23 \text{ Hz, } \delta = 0.05$$

$$W_L(z) = 3q_H C_L g_L \sqrt{1 + R_L \left(\frac{z}{H}\right)}$$

$$q_H = \frac{1}{2} \rho U_H^2; U_H = V_{ref} K_z \ln(H/z_0) = 26 \times 0.2 \times \ln(200/0.1) = 39.52 \text{ m/s}$$

$$q_H = 976.38 \text{ N/m}^2$$

$$C_L^1 = 0.0082 (D/B)^3 - 0.071 (D/B)^2 + 0.22 (D/B) = 0.1572$$

$$g_L = \sqrt{2 \ln(600 z_0) + 1.2} = 3.325$$

$$R_L = \frac{\pi F_L}{4m_p}; \eta_p = \delta/2\pi = 0.008$$

$$F_L = \sum_{i=1}^m \frac{4 \chi_i (1+0.6\beta_j) \beta_j}{\pi} \frac{(m_0/n_{sj})^2}{[1-(m_0/n_{sj})^2]^2 + 4\beta_j^2 (m_0/n_{sj})^2}$$

$$m = 1, \chi_1 = 0.85, \beta_1 = 0.169, m_{s1} = 0.19 \text{ Hz} \Rightarrow F_L = 0.095 \Rightarrow$$

$$R_L = 9.34 \Rightarrow W_L(z) = 3 \times 976.38 \times 0.1572 \times 3.325 \times \sqrt{1+9.34} (z/H) \Rightarrow$$

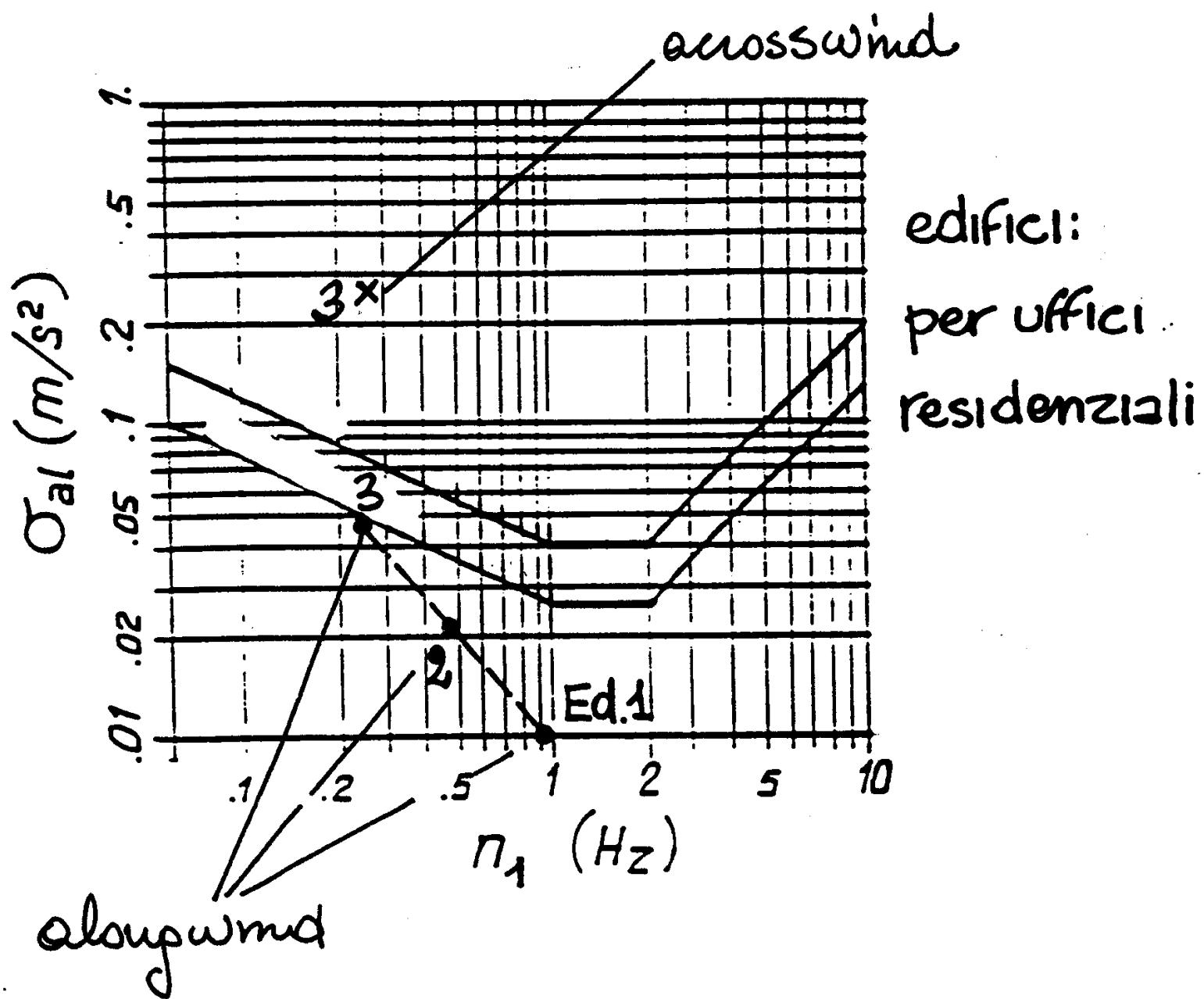
$$W_L(z) = 4923.17 (z/H) \text{ N/m}^2 \quad (\text{along wind } W(h) = 2088 \text{ N/m}^2)$$

## Acceleration (Commentary)

$$\alpha_{ij}(z) = 3q_H C_L \frac{B}{m} \sqrt{R_L \left(\frac{z}{H}\right)} \quad m = 180,000 \text{ kg/m}$$

$$\alpha_{ij}(H) = 3 \times 976.38 \times 0.1572 \frac{30}{180,000} \sqrt{9.34} = 0.235 \text{ m/s}^2$$

$$(\text{along wind } \alpha_{ij}(h) = 0.039 \text{ m/s}^2)$$



Acceleration control for habitability