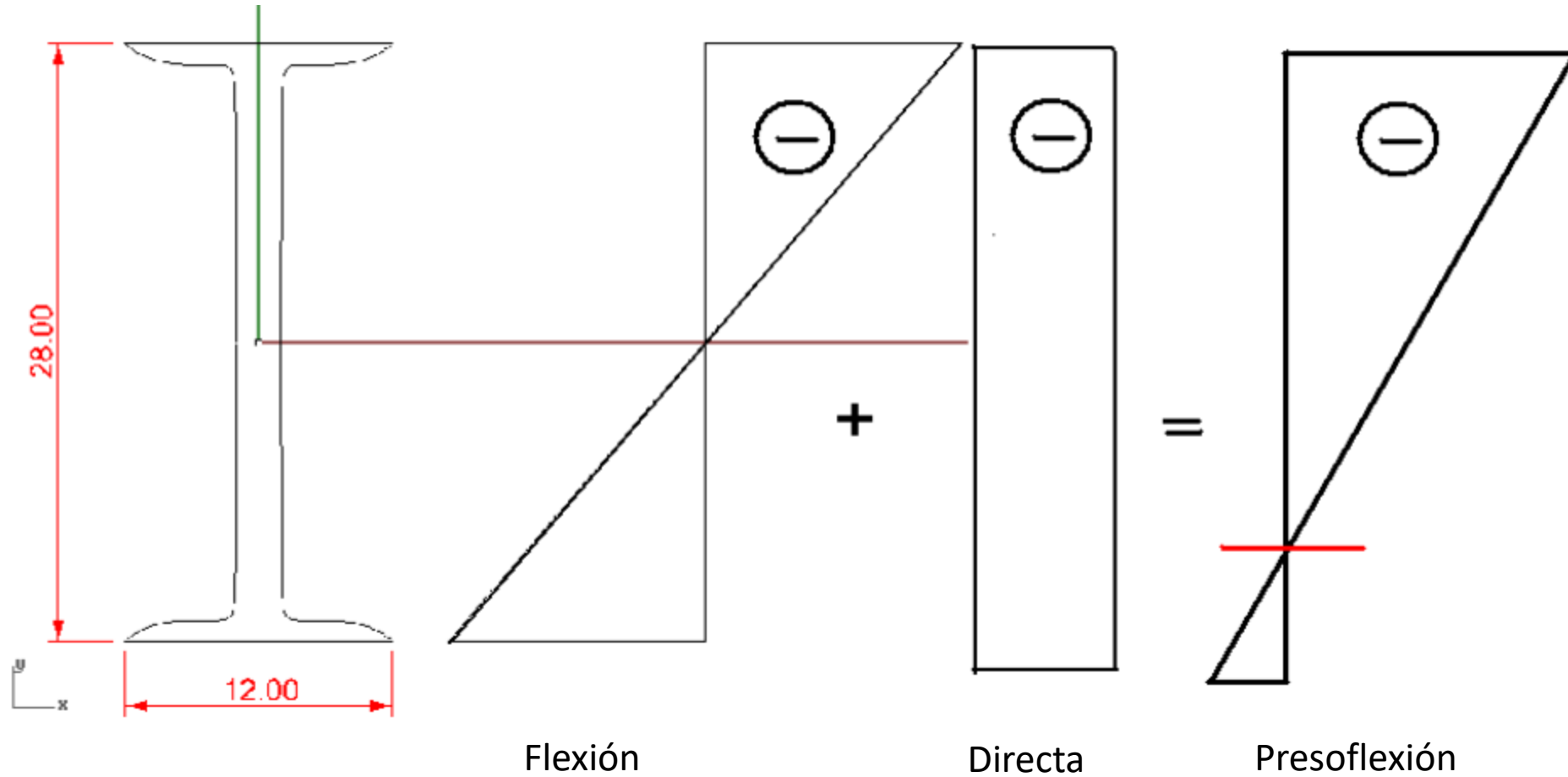
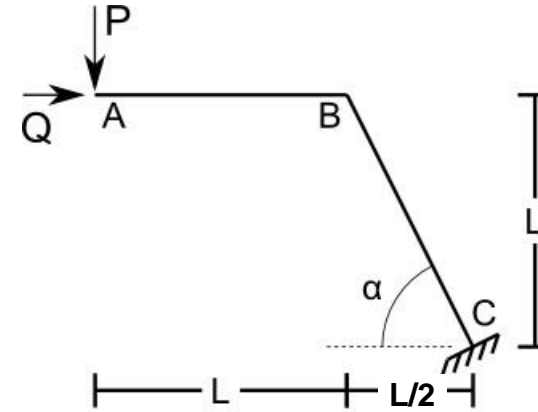
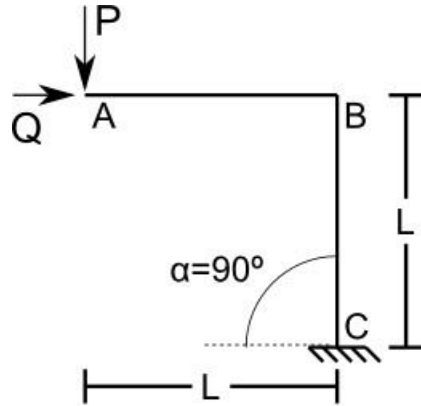


Pórticos

Flexión Compuesta







Caso particular de barras
en ángulo ortogonal.

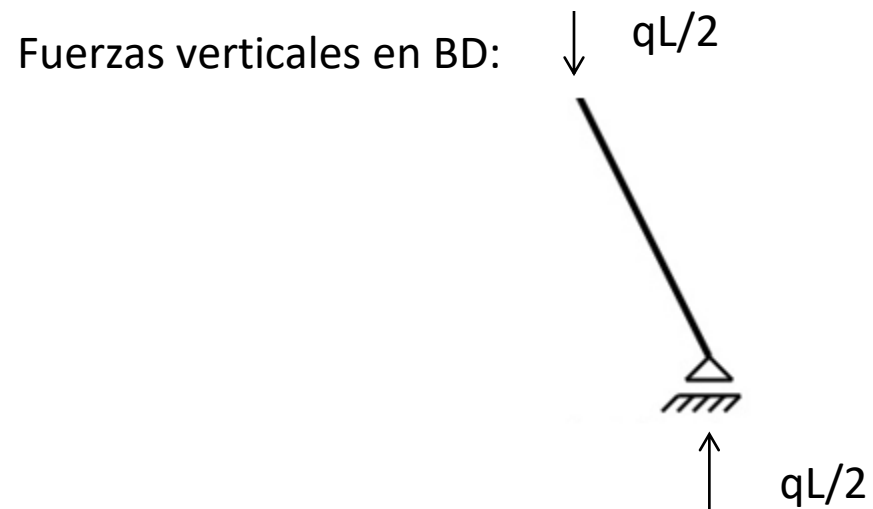
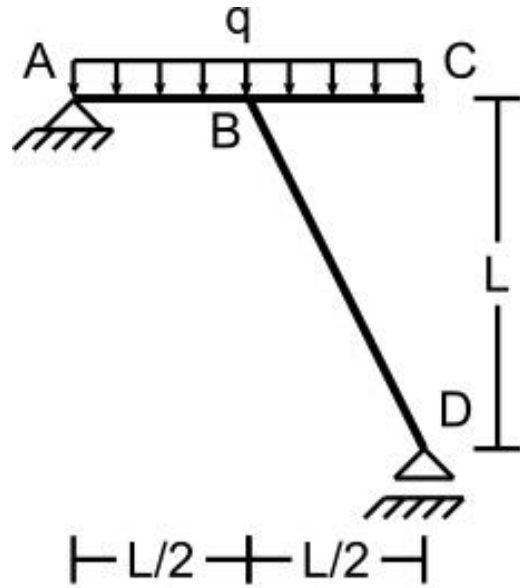
En B: $N^I = V^D$

$V^I = N^D$

$M^I = M^D$

Es decir, el cortante y la
directa se invierten, y el
momento se transmite.

Ejemplo



$$\text{Sum}(F_v)=0$$

$$R_A + R_D = qL$$

$$\text{Sum}(M_A)=0$$

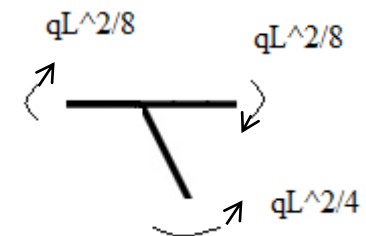
$$q \cdot L \cdot L/2 - R_D \cdot L = 0$$

$$R_D = qL/2$$

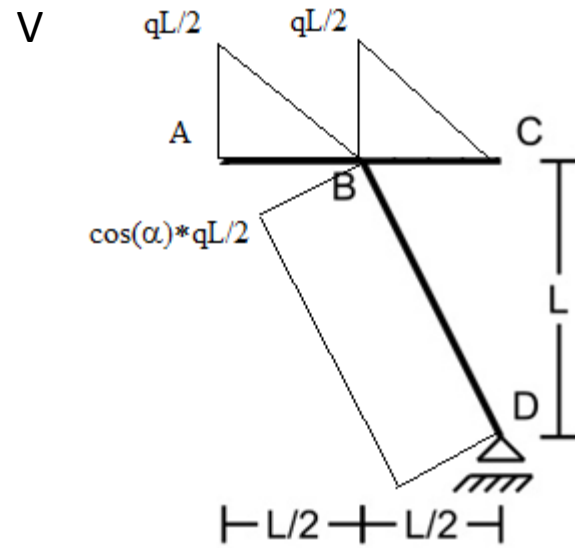
$$R_A = qL/2$$

$$\cos(\alpha) = 1/\text{raíz}(5)$$

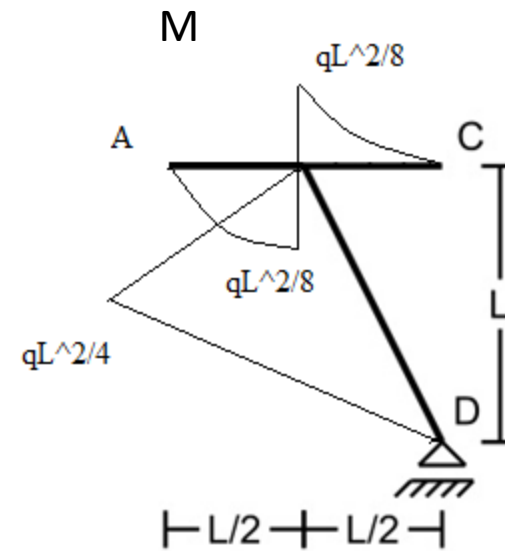
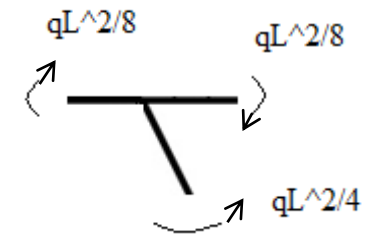
$$\text{sen}(\alpha) = 2/\text{raíz}(5)$$



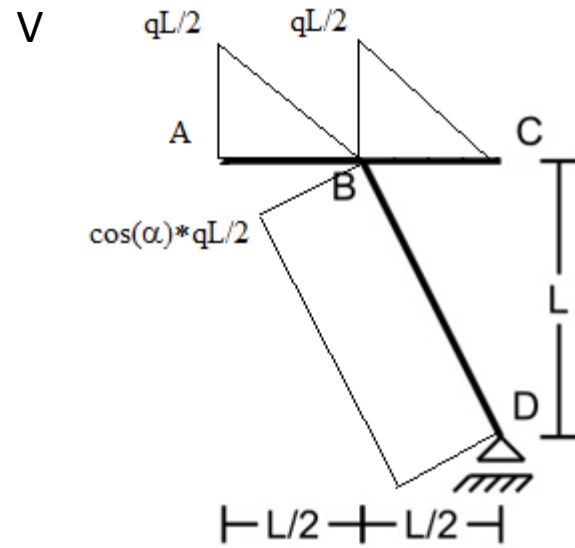
Diagramas



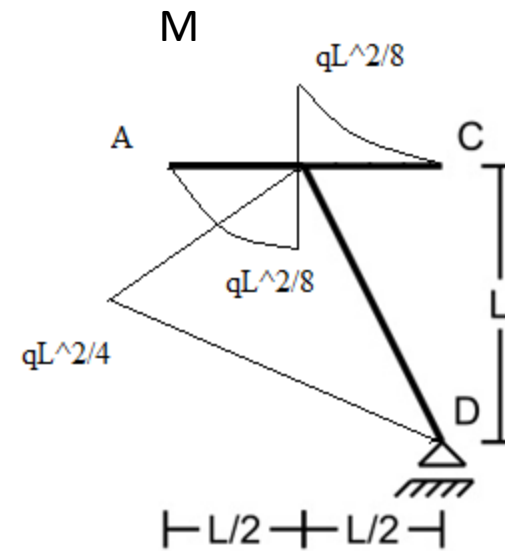
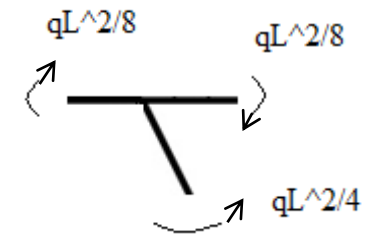
Momentos en el nudo=0



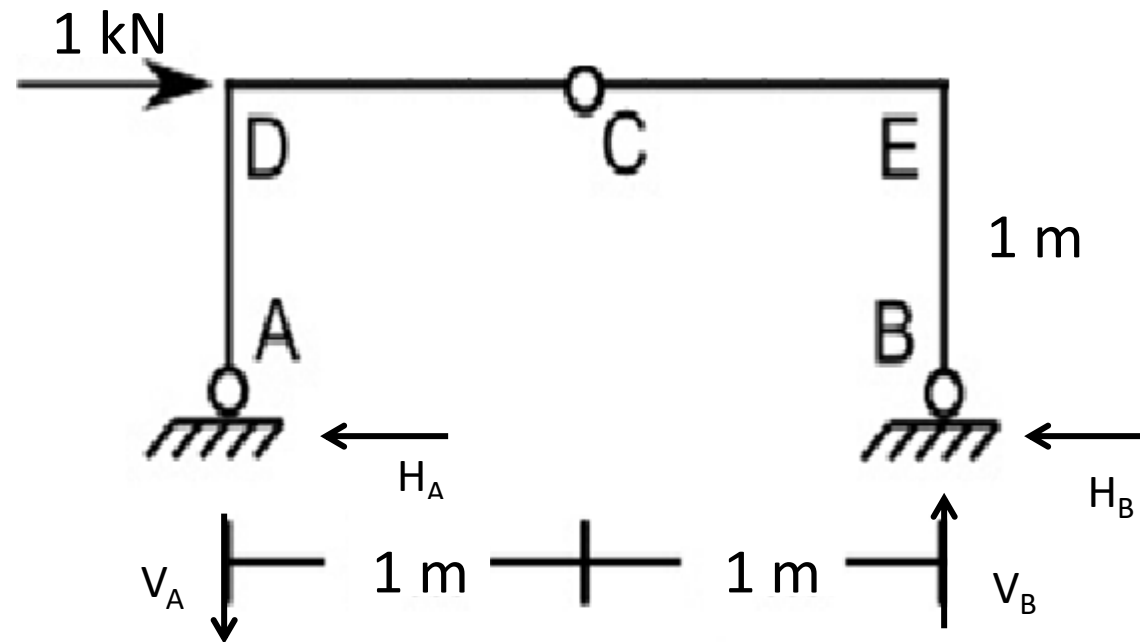
Diagramas



Momentos en
el nudo=0



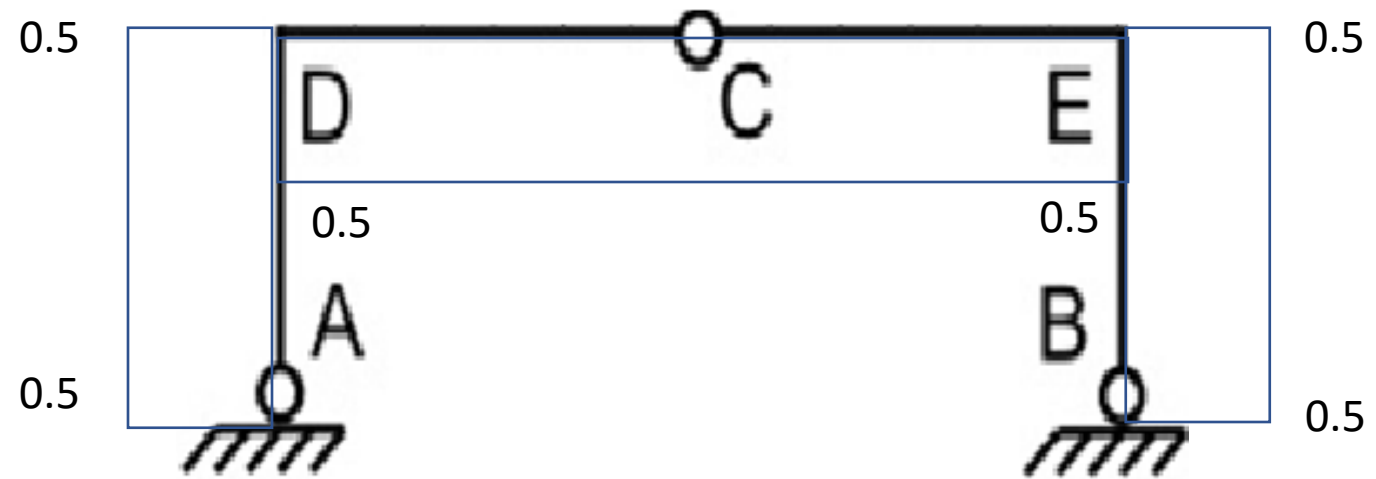
Ejemplo



$$\begin{aligned} -V_A + V_B &= 0 \\ H_A + H_B &= 1 \text{ kN} \end{aligned}$$

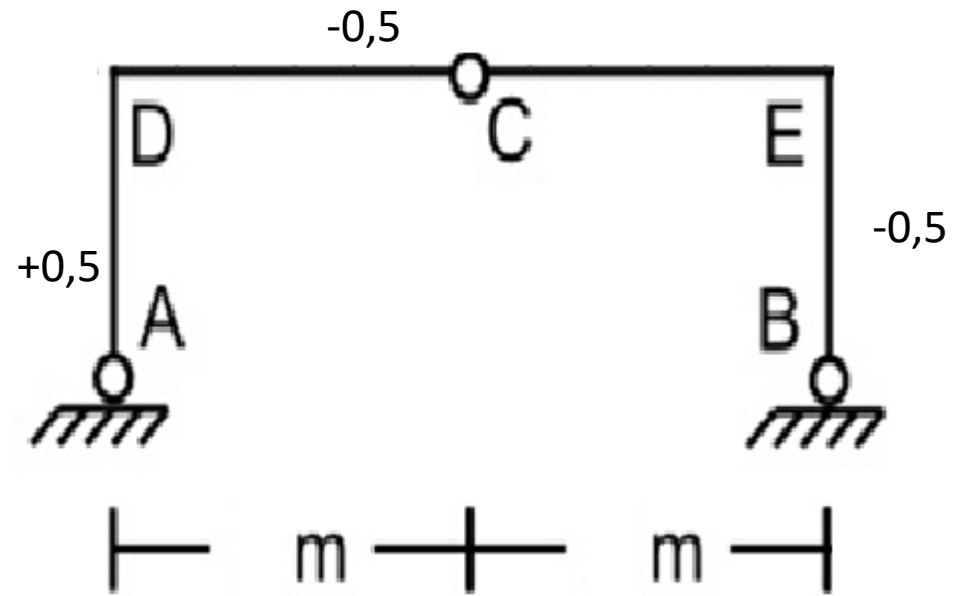
$$\begin{aligned} \text{Sum}(M_A) &= 0 \\ \text{Sum}(M_{izqC}) &= 0 \end{aligned}$$

V(kN)

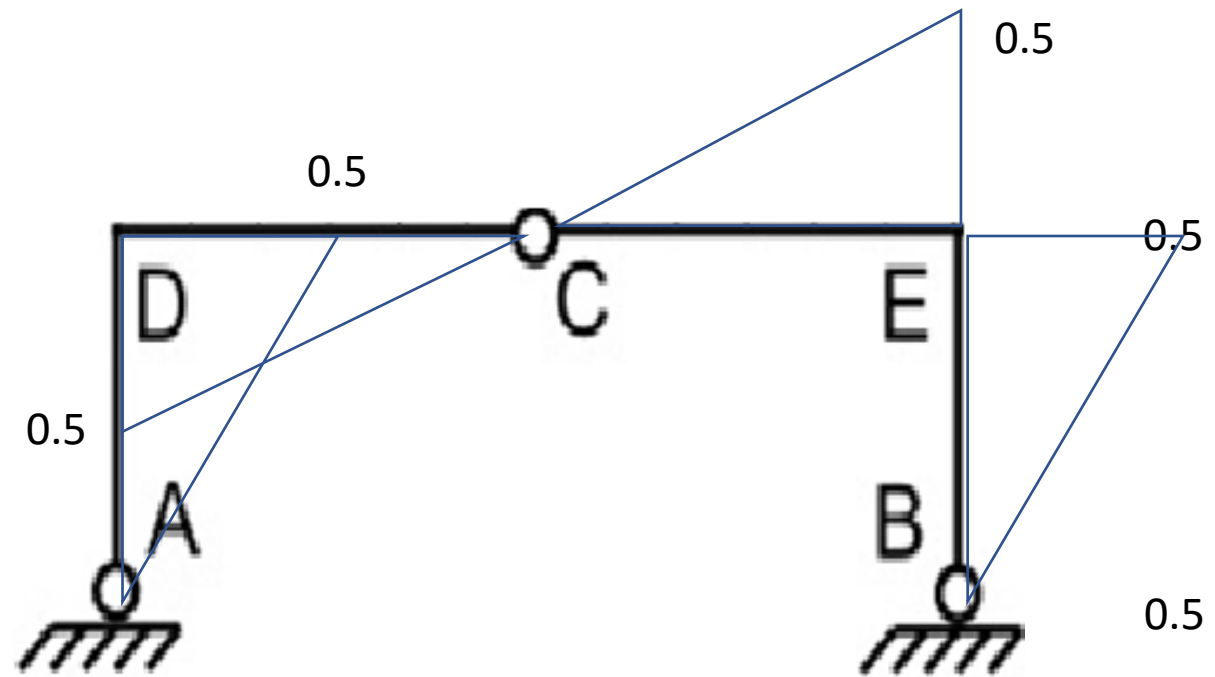


Tensiones Rasantes máximas

Diagrama de Directa N

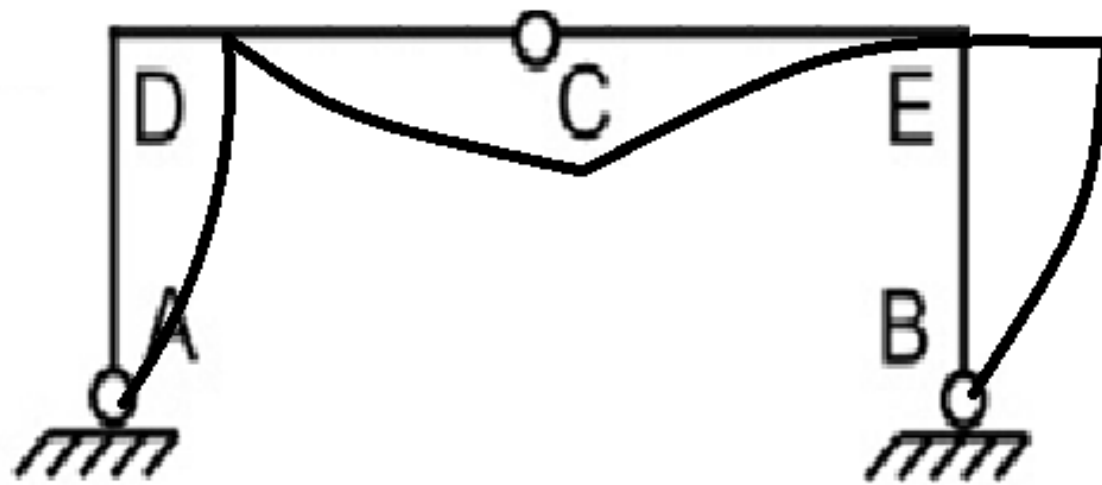


M(kN.m)

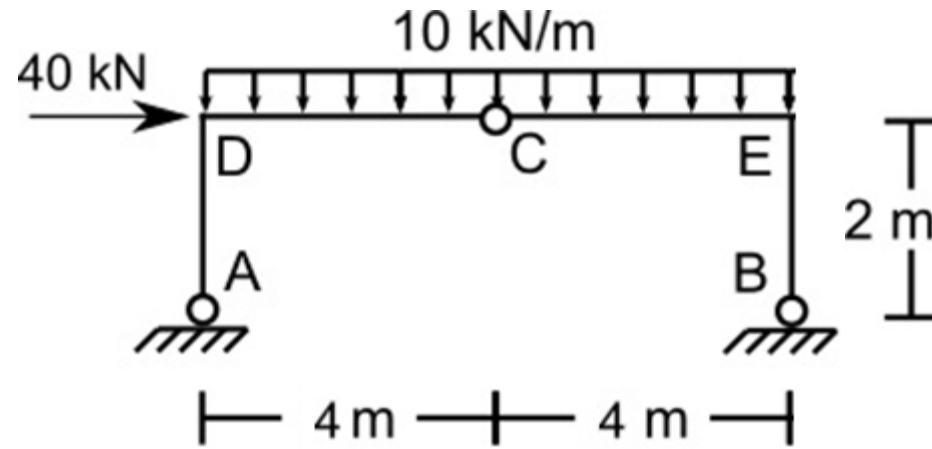


Tensiones Normales máximas (tensiones por M + tensiones por N)

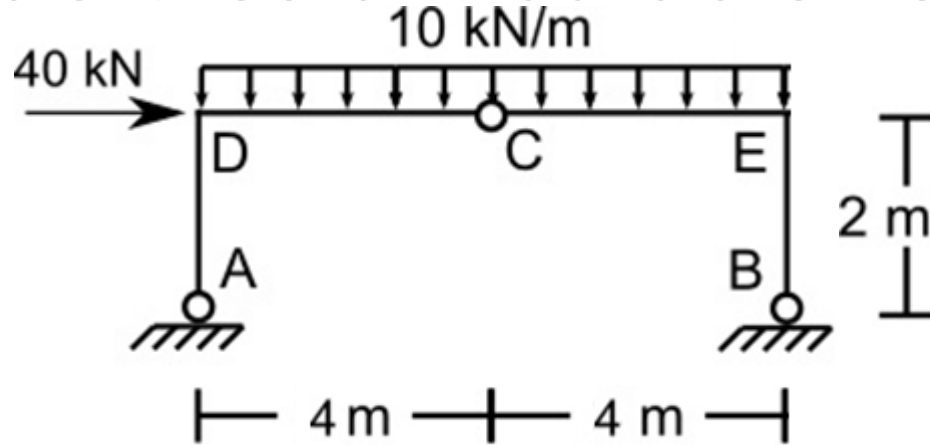
Ejemplo



Arco de tres Articulaciones



Arco de tres articulaciones



$$\text{Suma}(M_A)=0$$

$$40 \cdot 2 + 10 \cdot 8 \cdot 4 = 8 \cdot V_B \rightarrow V_B = 50 \text{ kN}$$

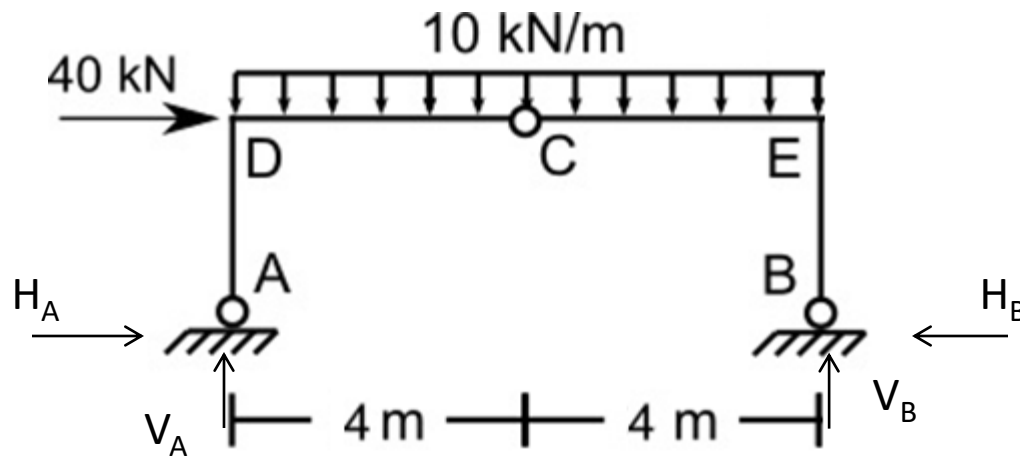
$$\text{Suma}(F_V) = V_A + 50 - 10 \cdot 8 = 0$$

$$V_A = 30 \text{ kN}$$

$$\text{Suma}(M_{\text{derC}}) = 4 \cdot 10 \cdot 2 - 50 \cdot 4 + H_B \cdot 2$$

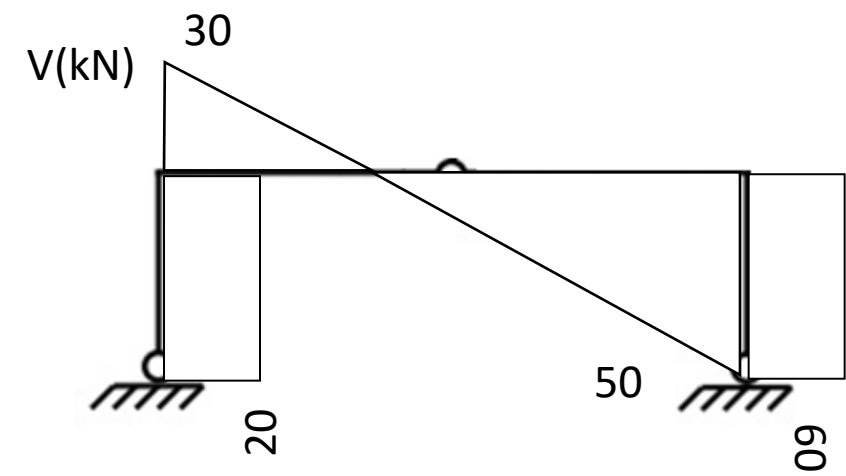
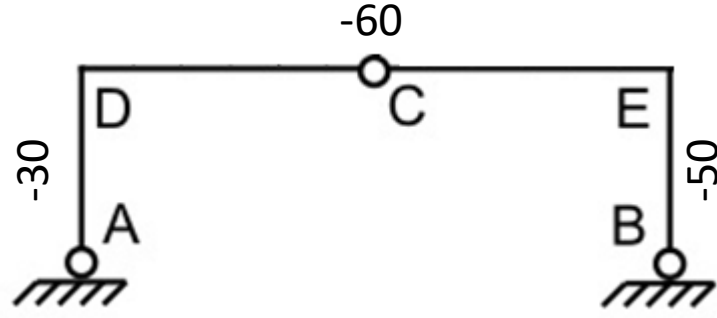
$$H_B = 60 \text{ kN}$$

$$H_A = 20 \text{ kN}$$

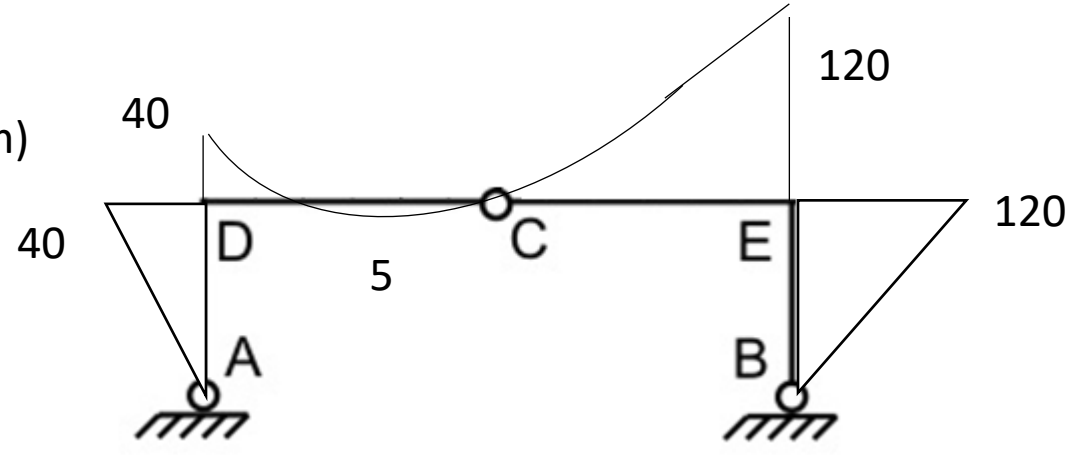


Diagramas

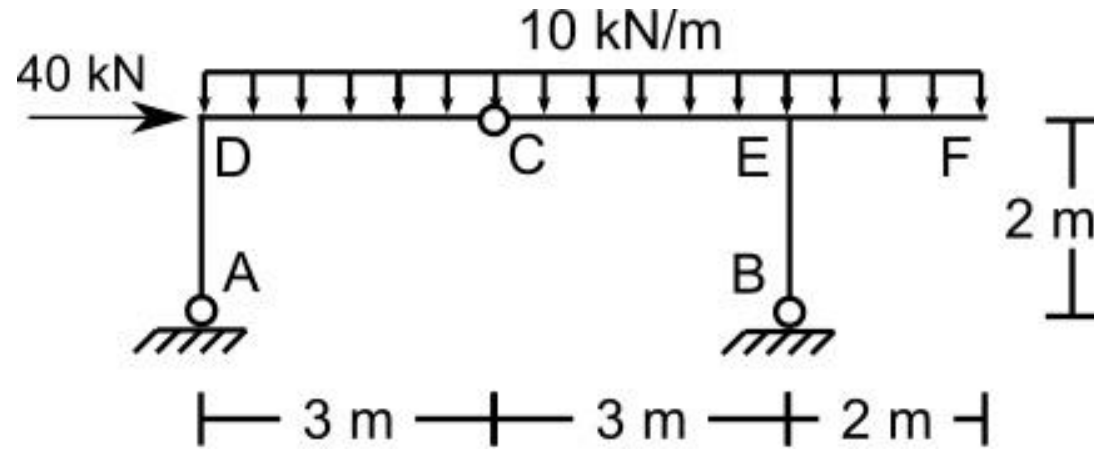
N(kN)



M(kN.m)



Arco de tres articulaciones



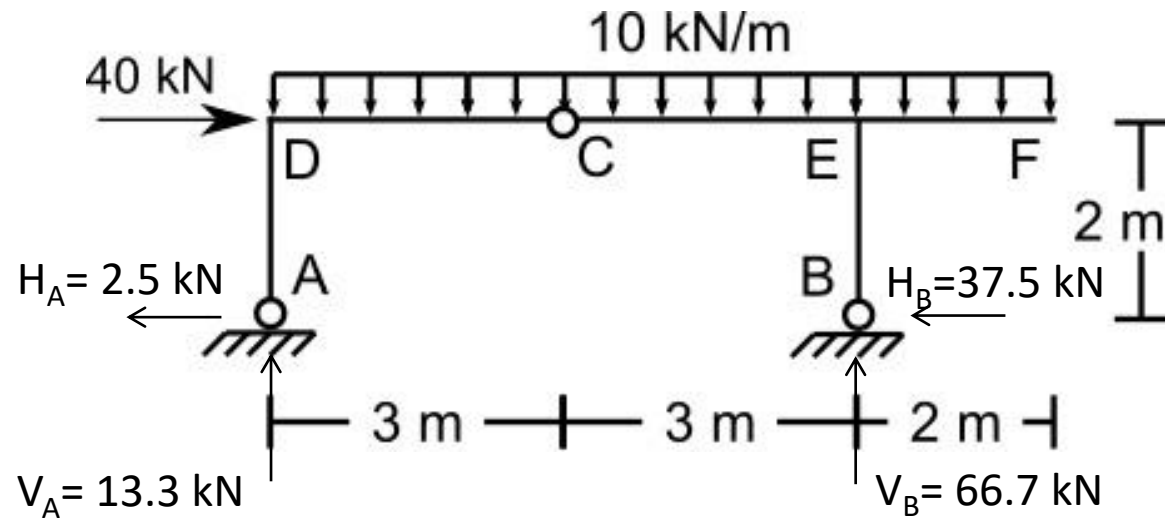
$$\text{Suma}(M_A)=0 \quad 40 \cdot 2 + 10 \cdot 8 \cdot 4 - V_B \cdot 6 = 0 \quad \rightarrow V_B = 66.7 \text{ kN}$$

$$\text{Suma}(F_V)=0 \quad V_A + V_B = 80 \quad \rightarrow V_A = 13.3 \text{ kN}$$

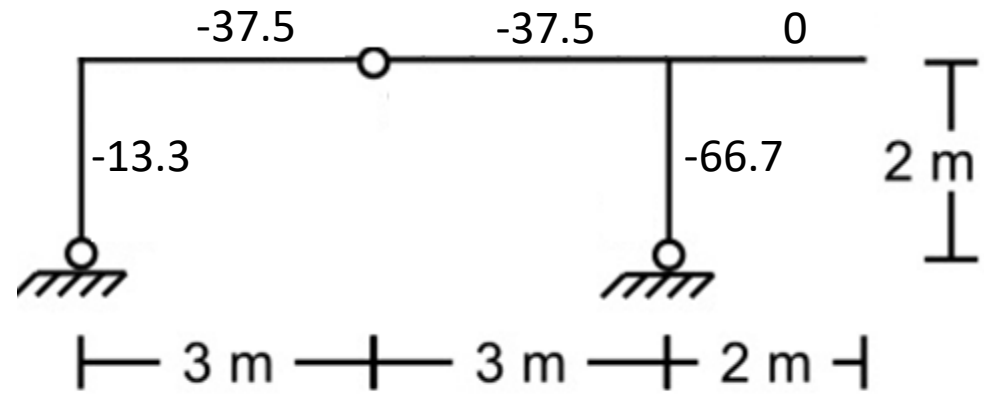
$$\text{Suma}(M_{\text{derC}})=0 \quad 10 \cdot 5 \cdot 2.5 - 66.7 \cdot 3 + H_B \cdot 2 = 0 \quad \rightarrow H_B = 37.5 \text{ kN}$$

$$H_A = 2.5 \text{ kN}$$

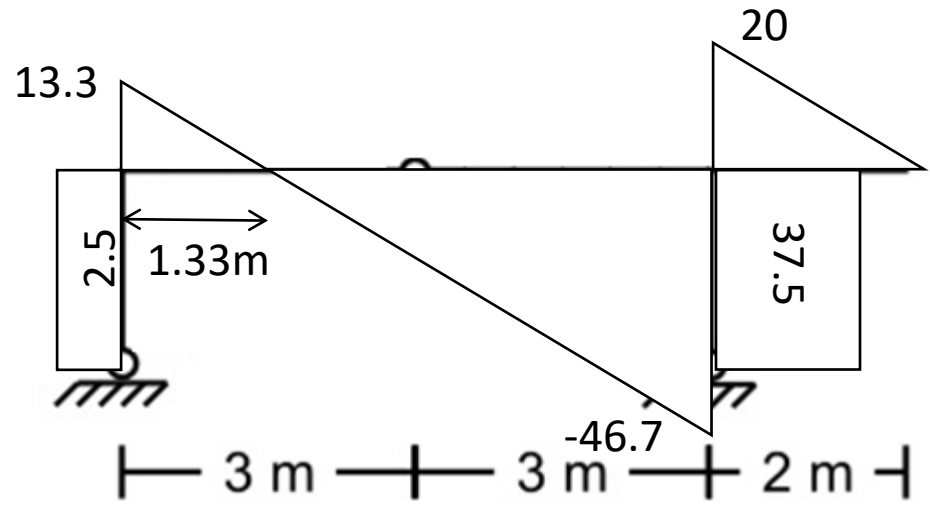
Reacciones

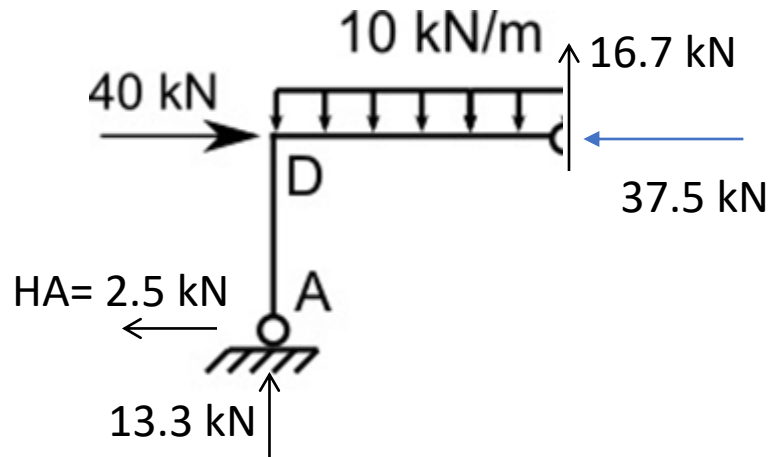


N(kN)

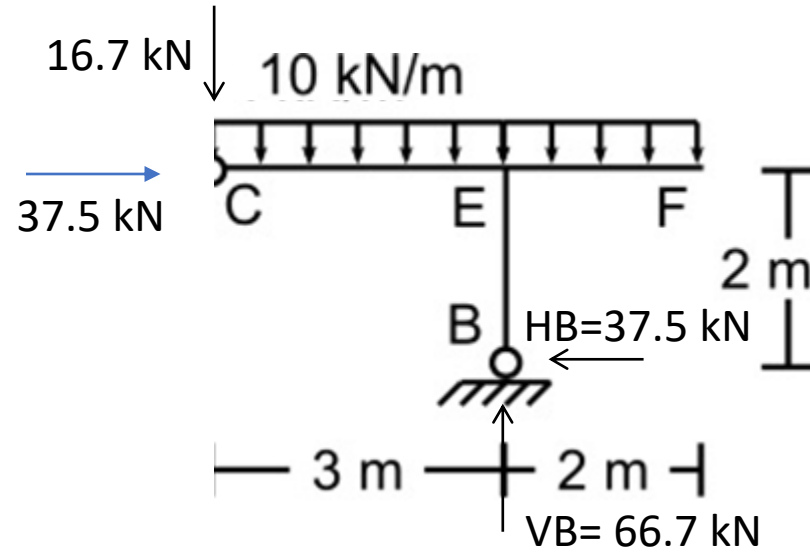
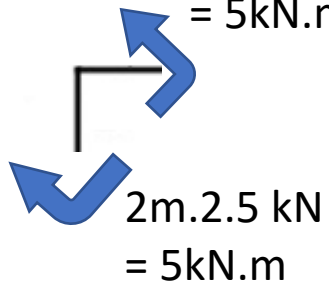


V(kN)

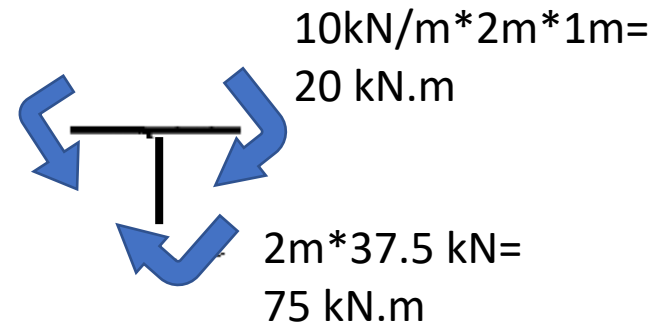




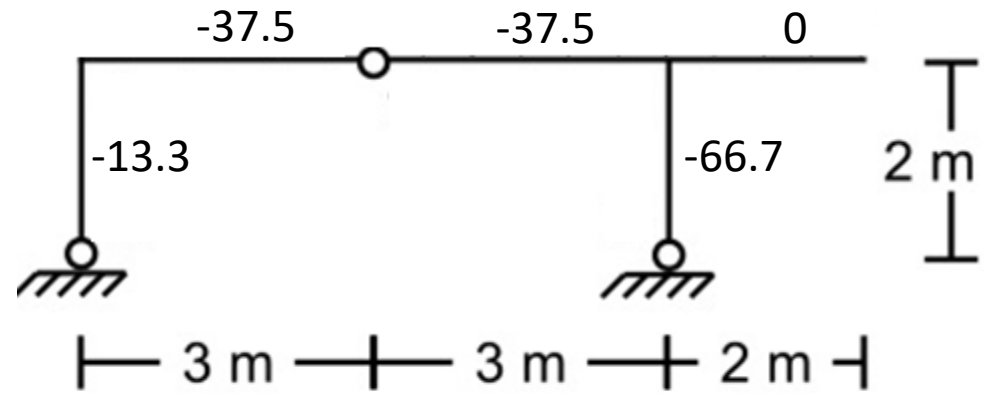
$$3 \text{m} \cdot 16.7 \text{ kN} - 10 \text{ kN/m} \cdot 3 \text{m} \cdot 1.5 \text{m} = 5 \text{ kN.m}$$



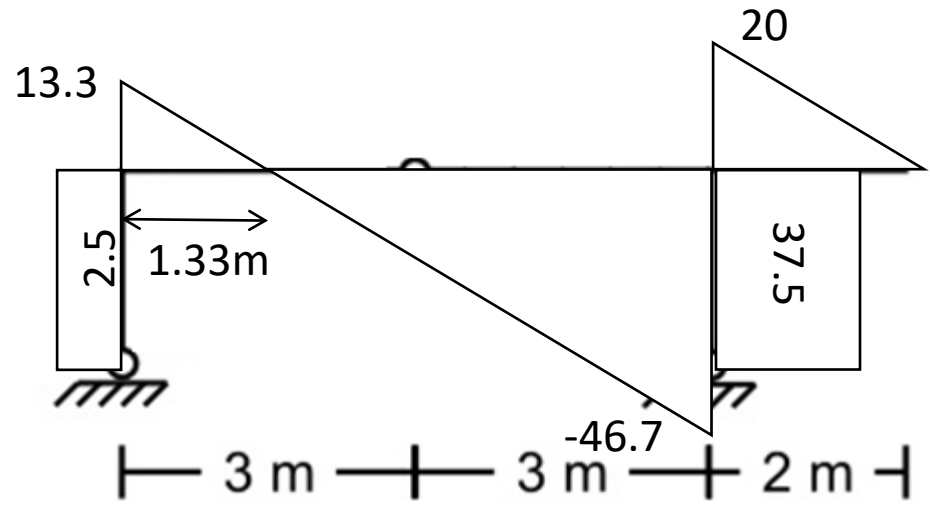
$$3 \cdot 16.7 + 10 \cdot 3 \cdot 1.5 = 95 \text{ kN.m}$$

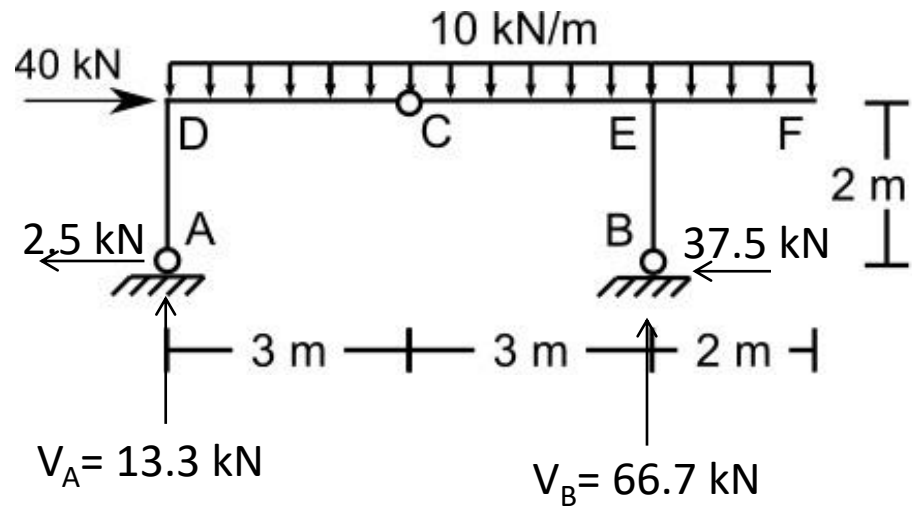


N(kN)

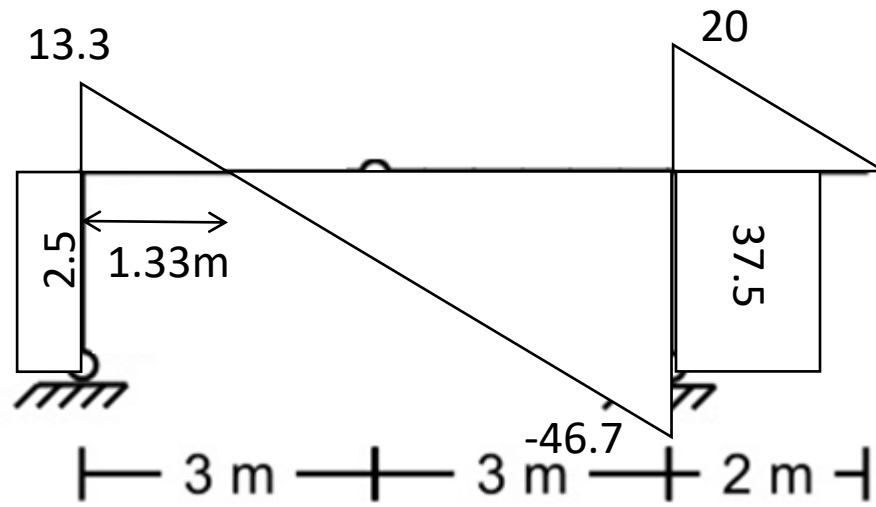


V(kN)

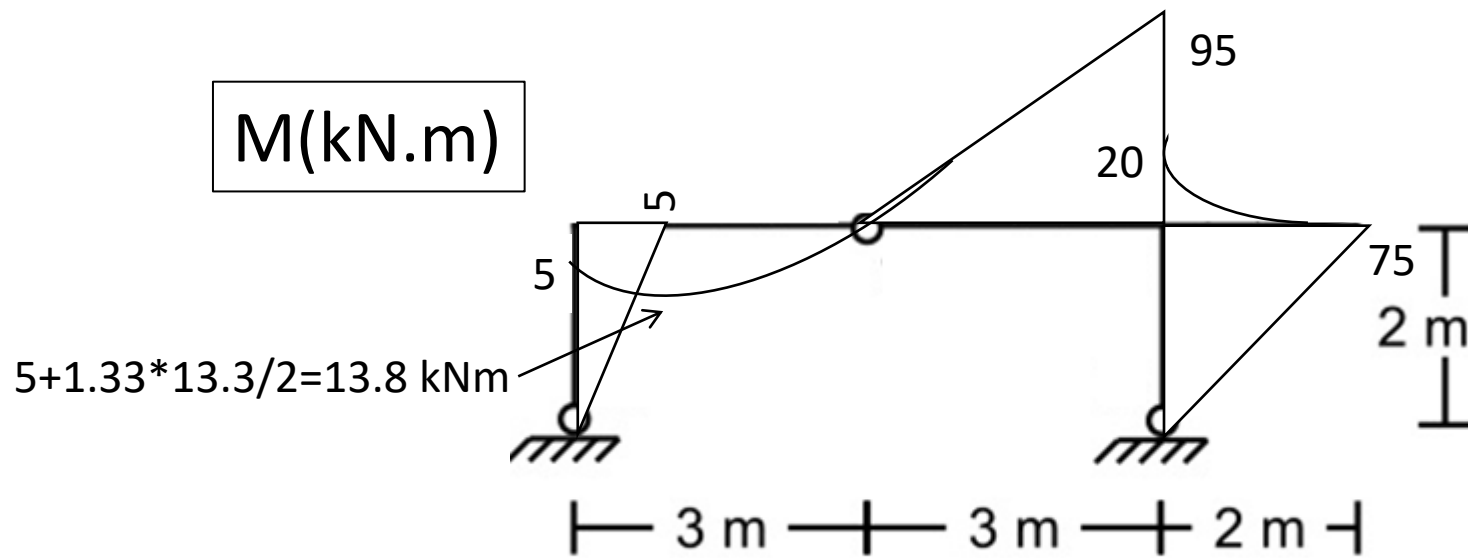




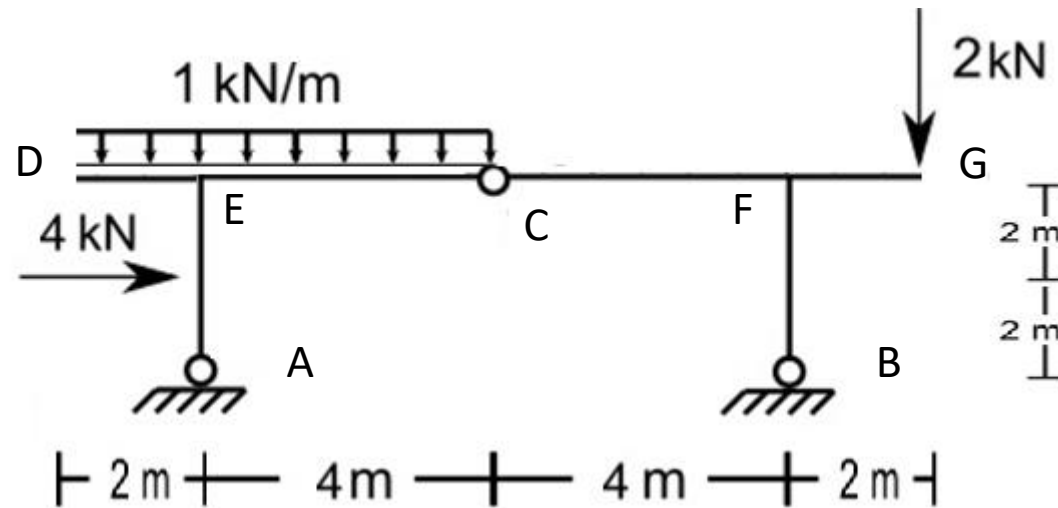
V(kN)



M(kN.m)



Ejemplo



$$\text{Suma}(FV)=0$$

$$V_A+V_B=2+6$$

$$\text{Suma}(FH)=0$$

$$H_A+H_B=4$$

$$V_A=3.75 \text{ kN}$$

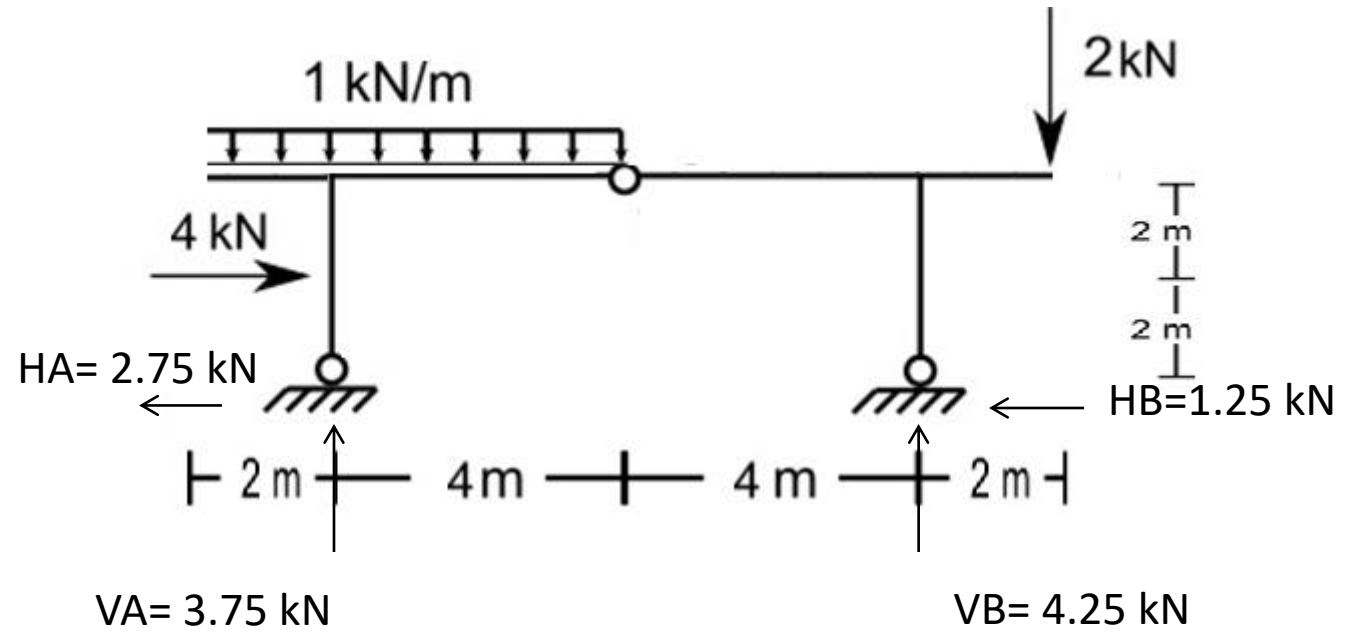
$$\text{Suma}(MA)=0$$

$$4 \cdot 2 + 4 \cdot 2 - 2 \cdot 1 + 2 \cdot 10 - 8 \cdot V_B = 0 \rightarrow V_B = 4.25 \text{ kN}$$

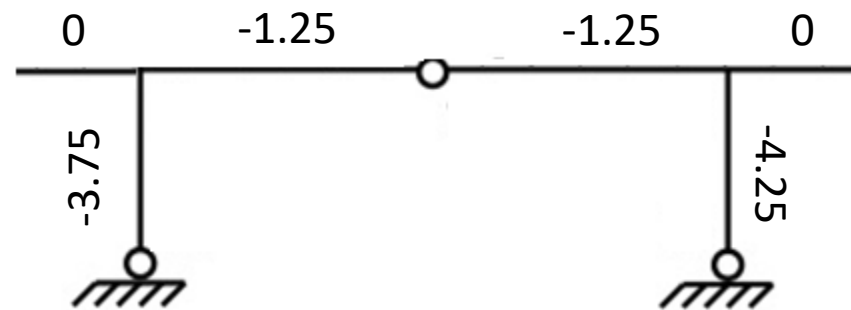
$$\text{Suma}(MC_{\text{derecha}})=0$$

$$-V_B \cdot 8 + H_B \cdot 4 + 2 \cdot 6 = 0 \rightarrow H_B = 1.25 \text{ kN}$$

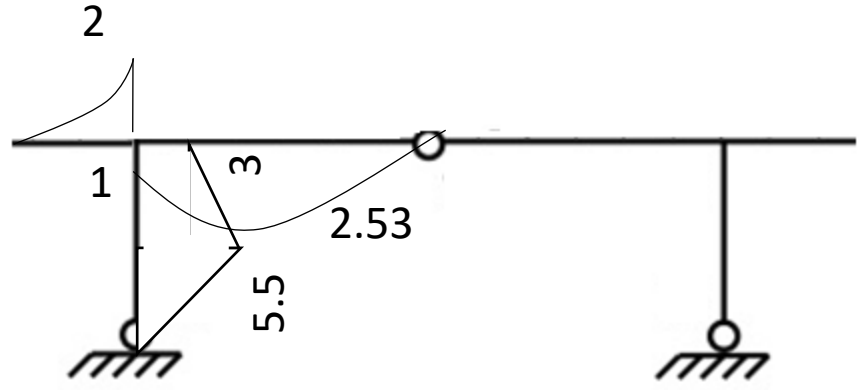
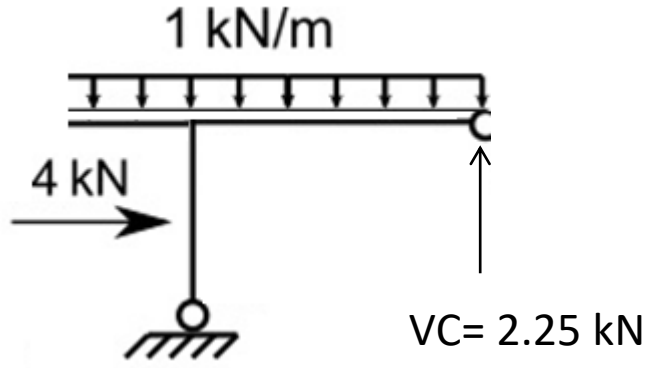
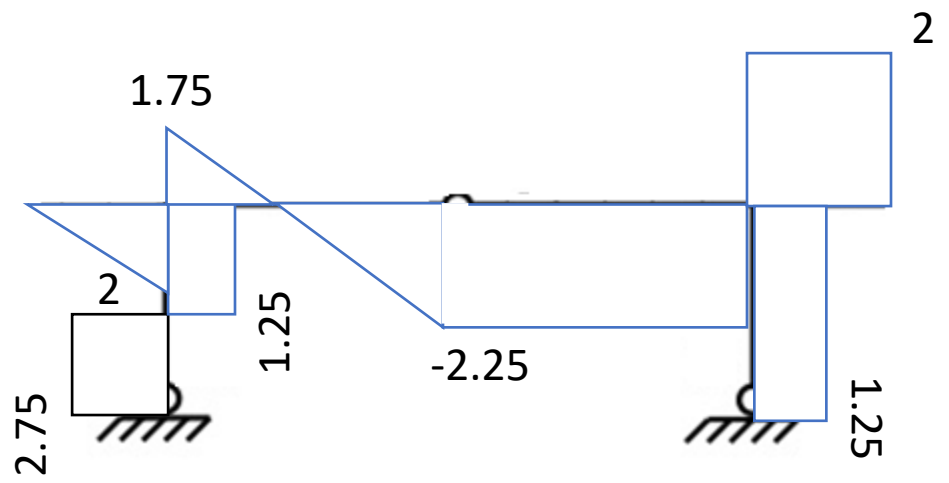
$$H_A = 2.75 \text{ kN}$$



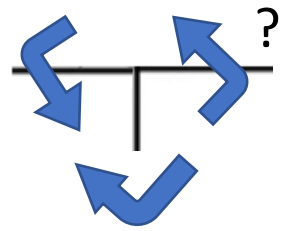
$N(\text{kN})$



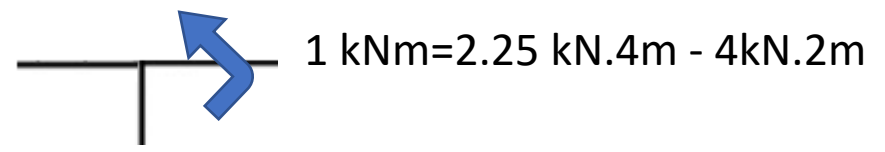
V(kN)



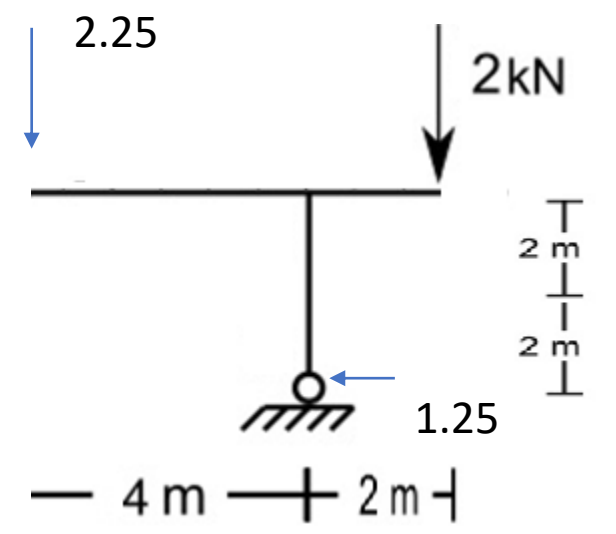
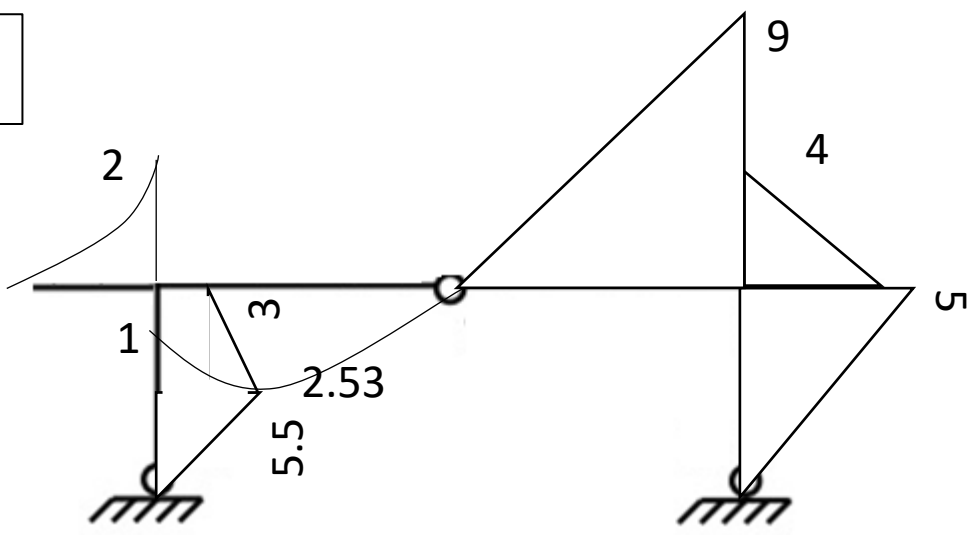
$2 \text{ kNm} = 2 \cdot 1$



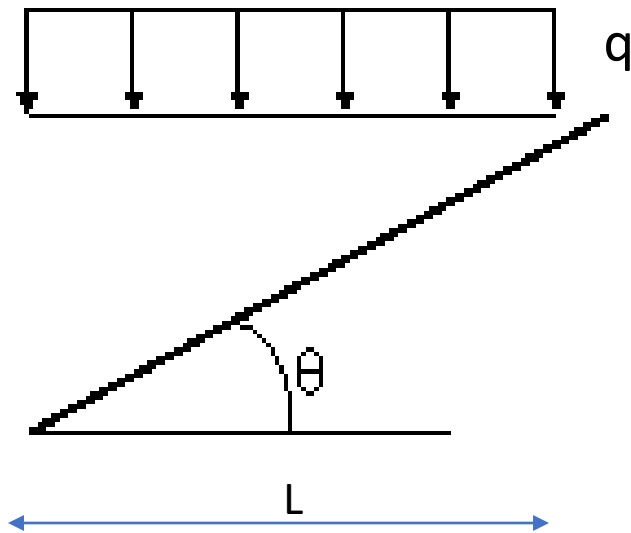
$3 \text{ kNm} = -2.75 \text{ kN} \cdot 4 \text{ m} + 4 \text{ kN} \cdot 2 \text{ m}$



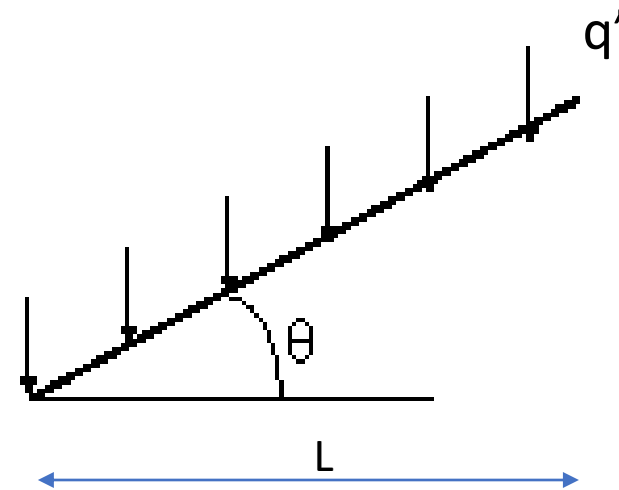
M(kN.m)



Carga distribuida

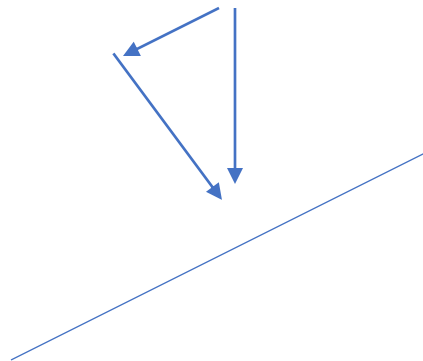
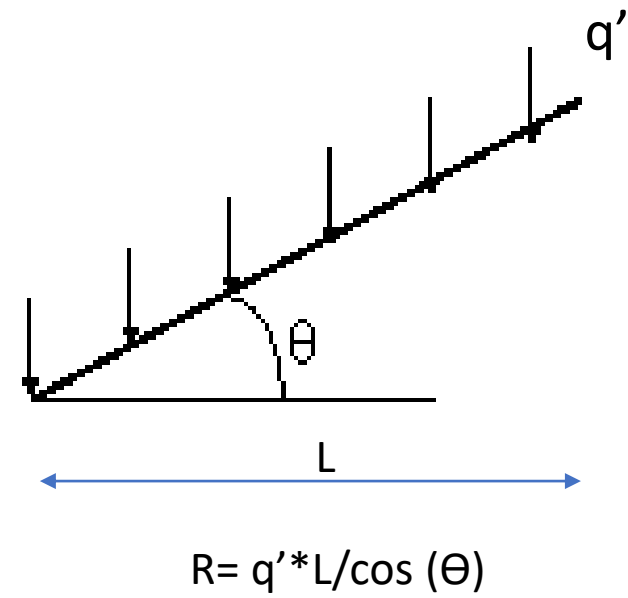
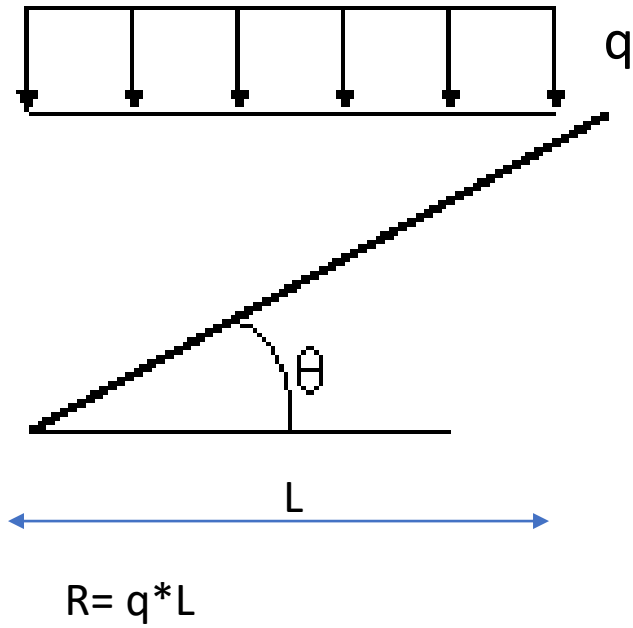


$$R = q * L$$



$$R = q' * L / \cos(\theta)$$

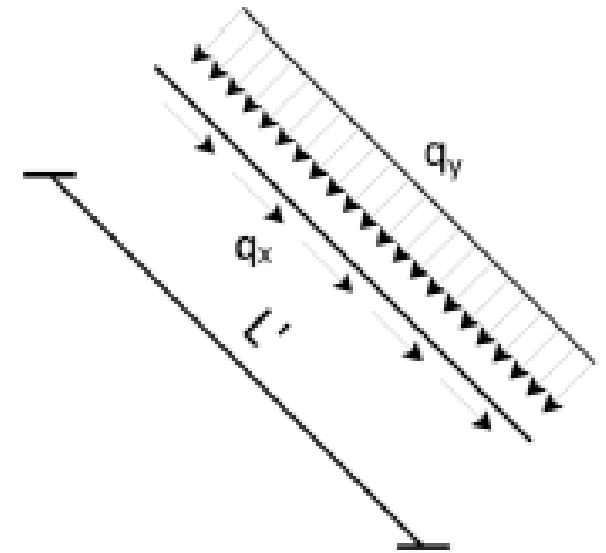
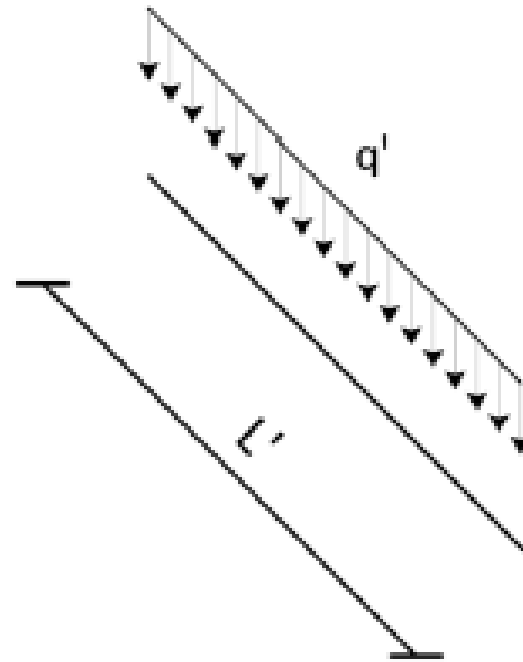
Carga distribuida

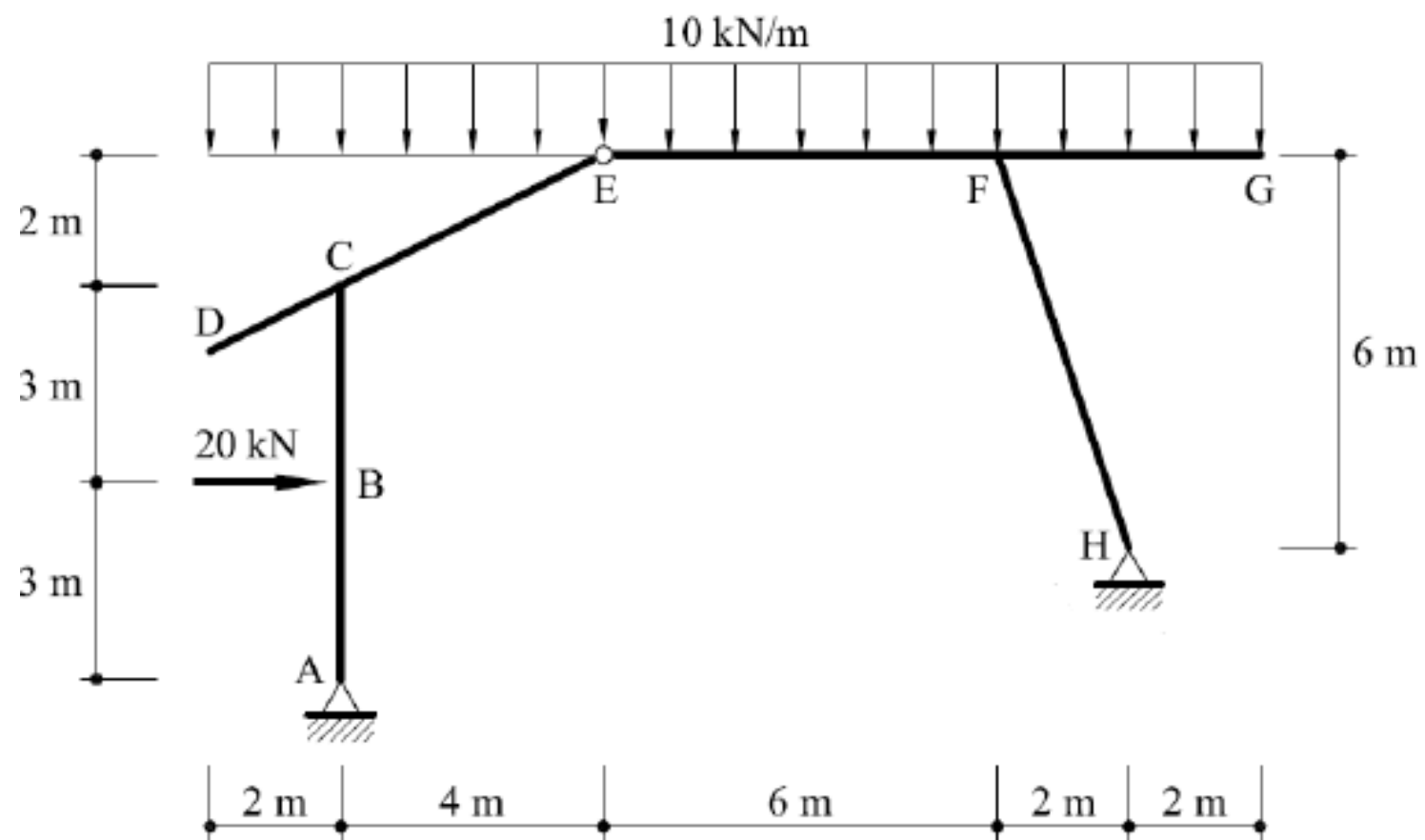


Puede resultar útil trabajar con la carga en los ejes locales de la barra, por lo que descomponemos en cargas q_x y q_y

$$q_y = q' \cos \alpha$$

$$q_x = q' \sin \alpha$$





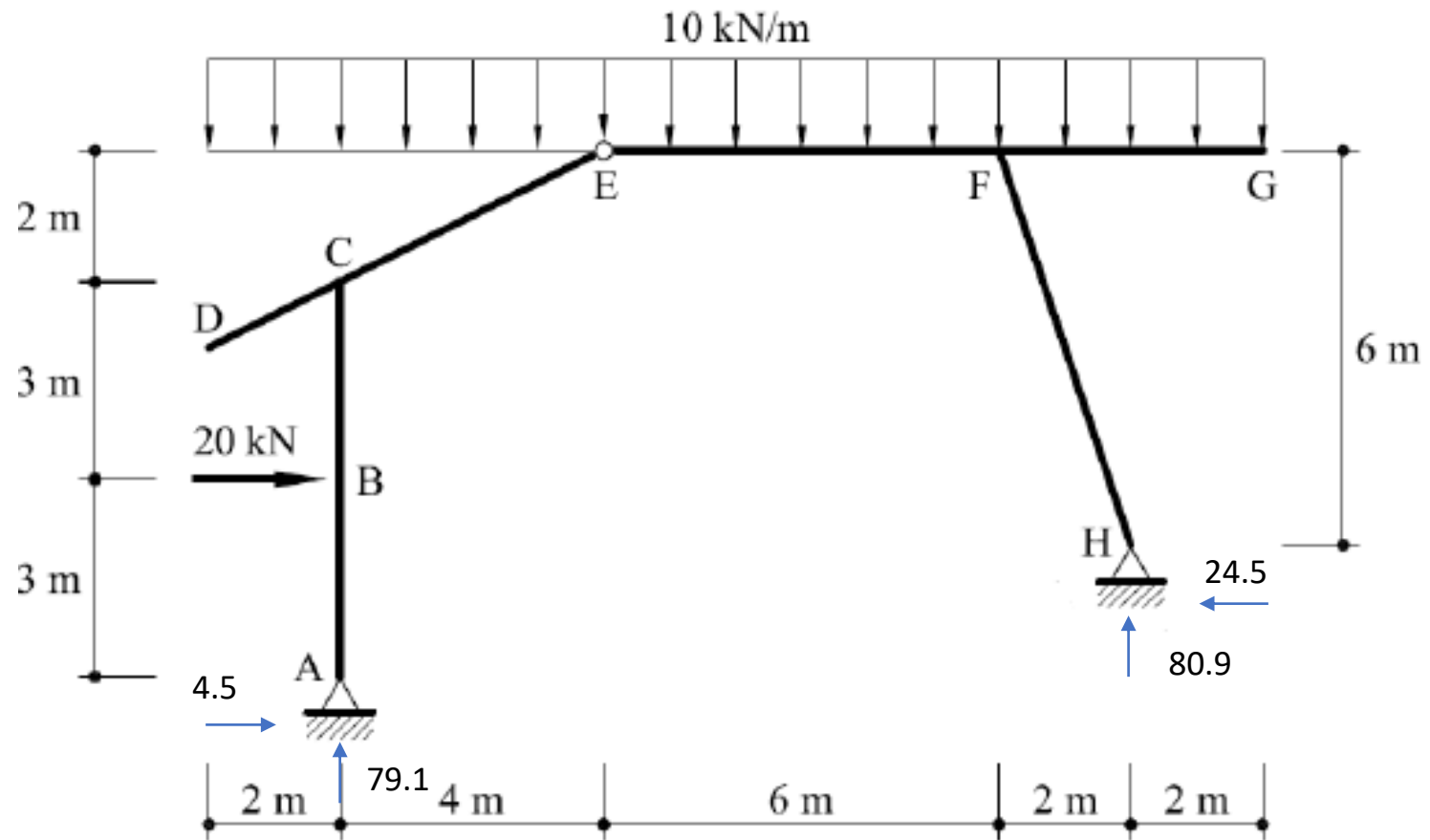
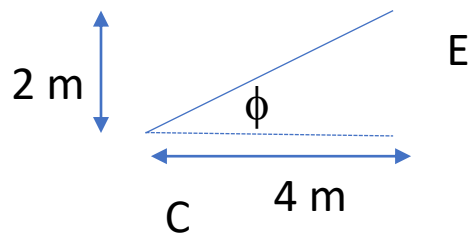
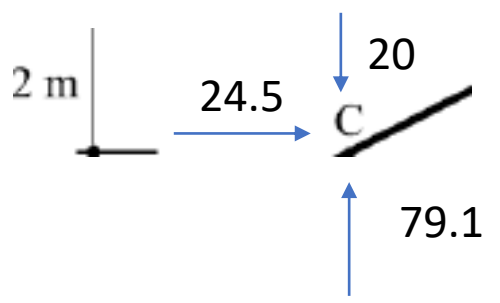


Diagrama de Directa

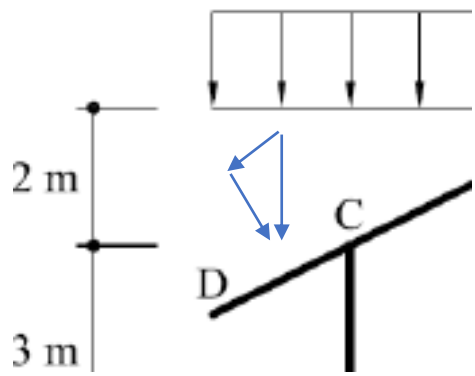


$\tan \phi = 2/4$
 $\cos \phi = 0.8944$
 $\sin \phi = 0.4472$



$59.1 \cdot 0.4475 + 24.5 \cdot 0.8944 = 48.4 \text{ kN}$

$19.1 \cdot 0.4475 + 24.5 \cdot 0.8944 = 30.5 \text{ kN}$

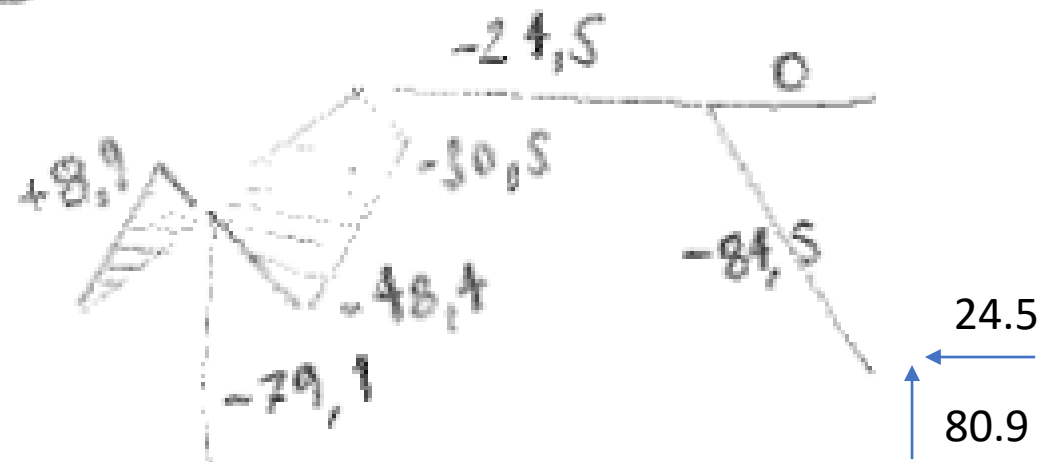


$qN = 10 \cdot 0.4472$
 $qV = 10 \cdot 0.8944$

Directa DC en C

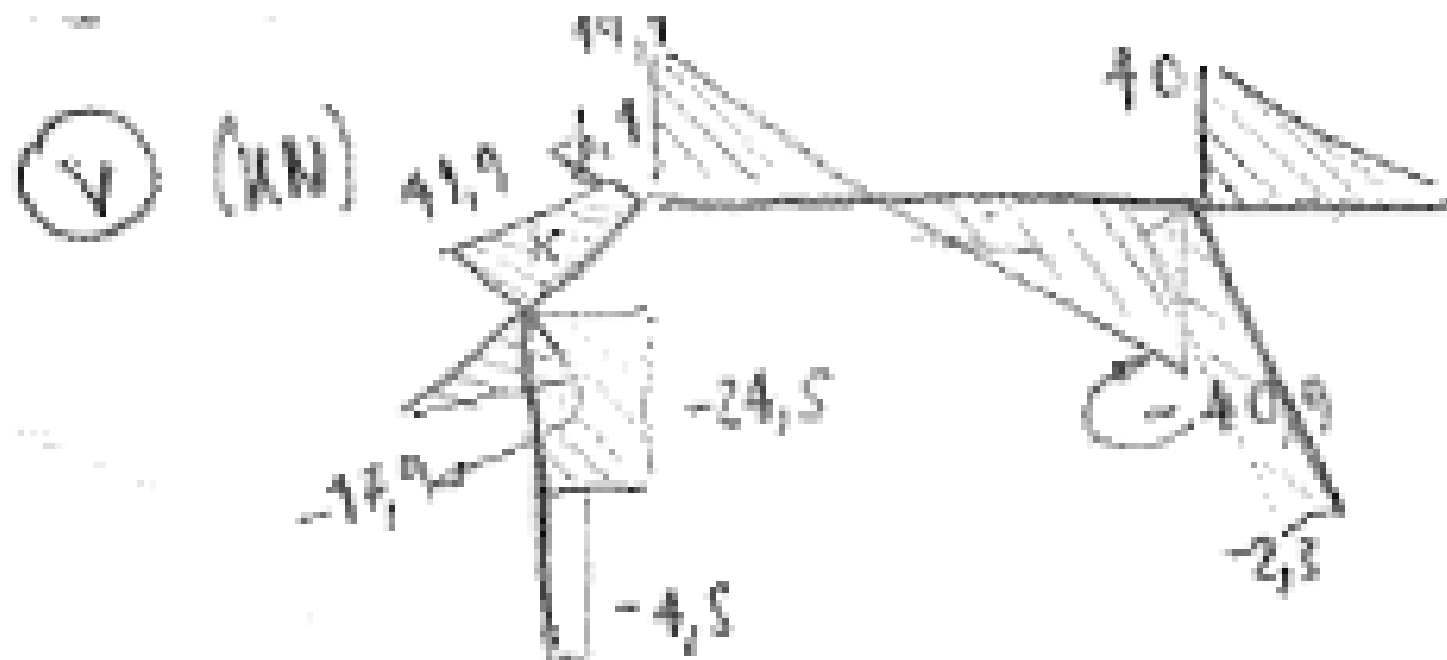
$N_{DC} = 2 \cdot 10 \cdot 0.4472 = 8.9 \text{ kN}$

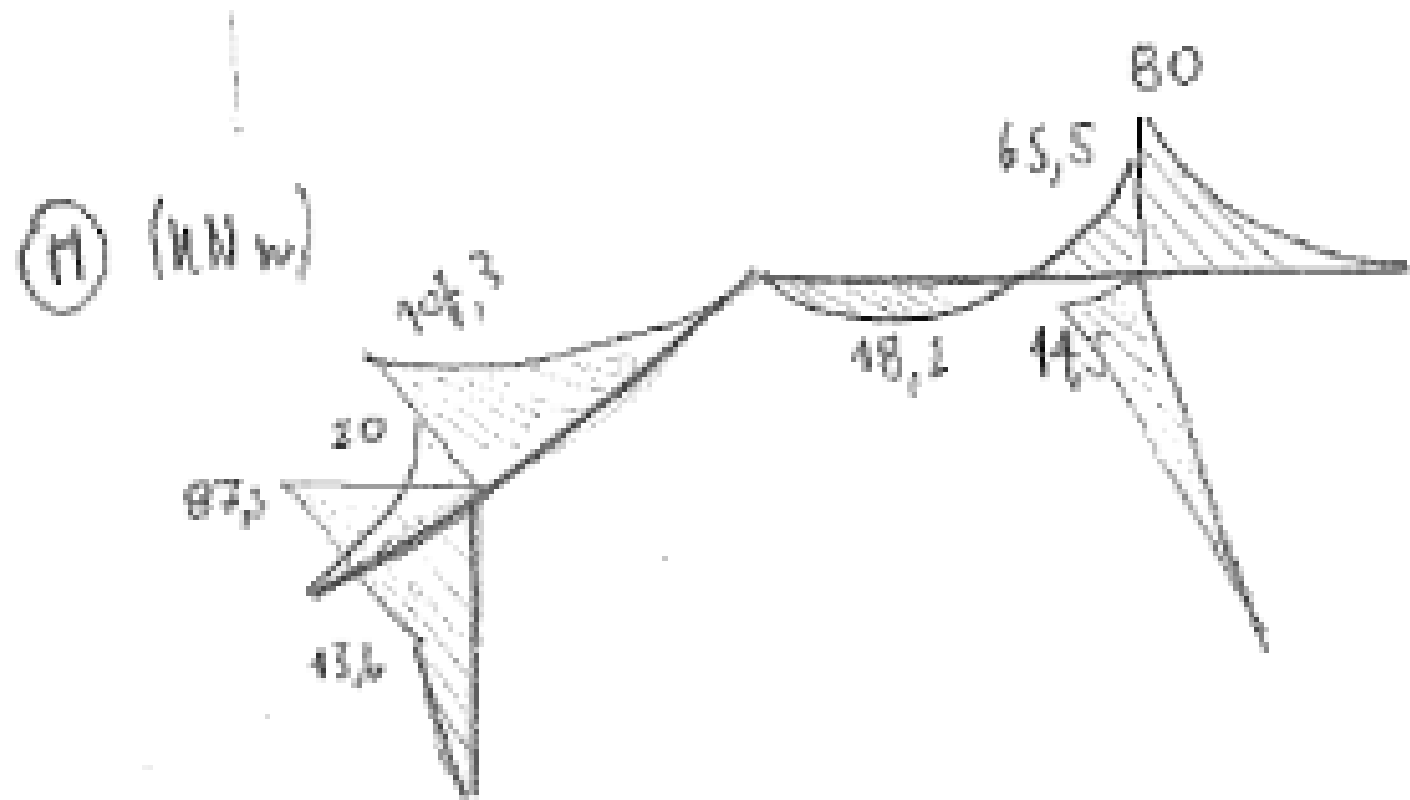
(N) (xN)



$24.5 \cdot \sin a + 80.9 \cdot \cos a = 84.5 \text{ kN}$

Diagrama de Cortante



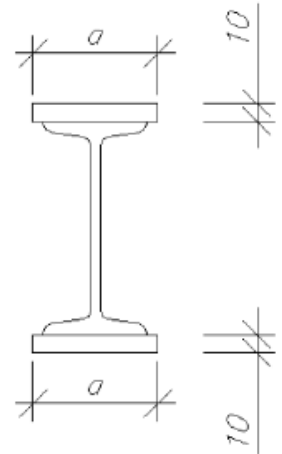
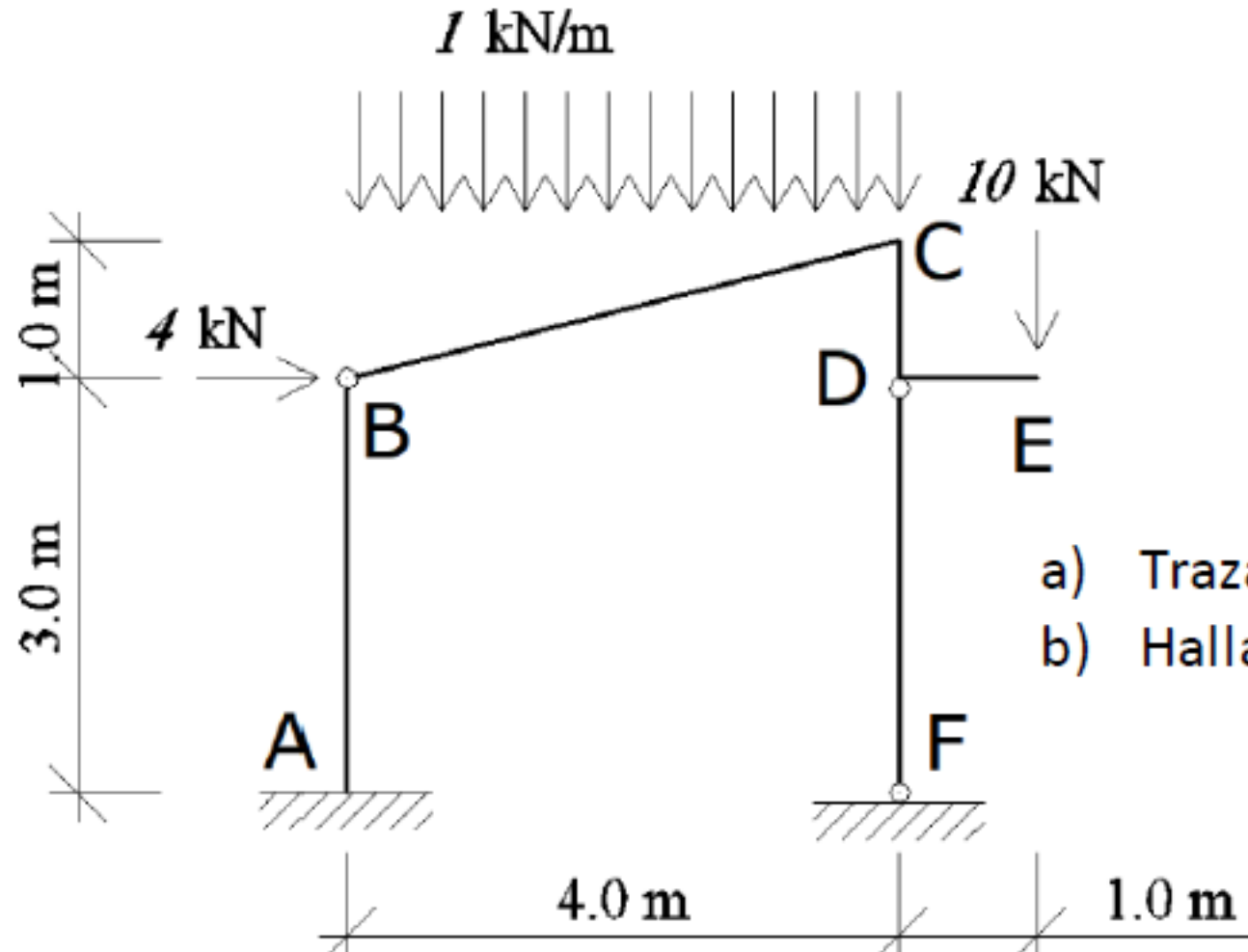


Gere, 5^a Ed. (2002): 5.12

Ortiz Berrocal, 3^a Ed. (2007): 6.5

Beer, 3^a Ed. (2004): 4.12

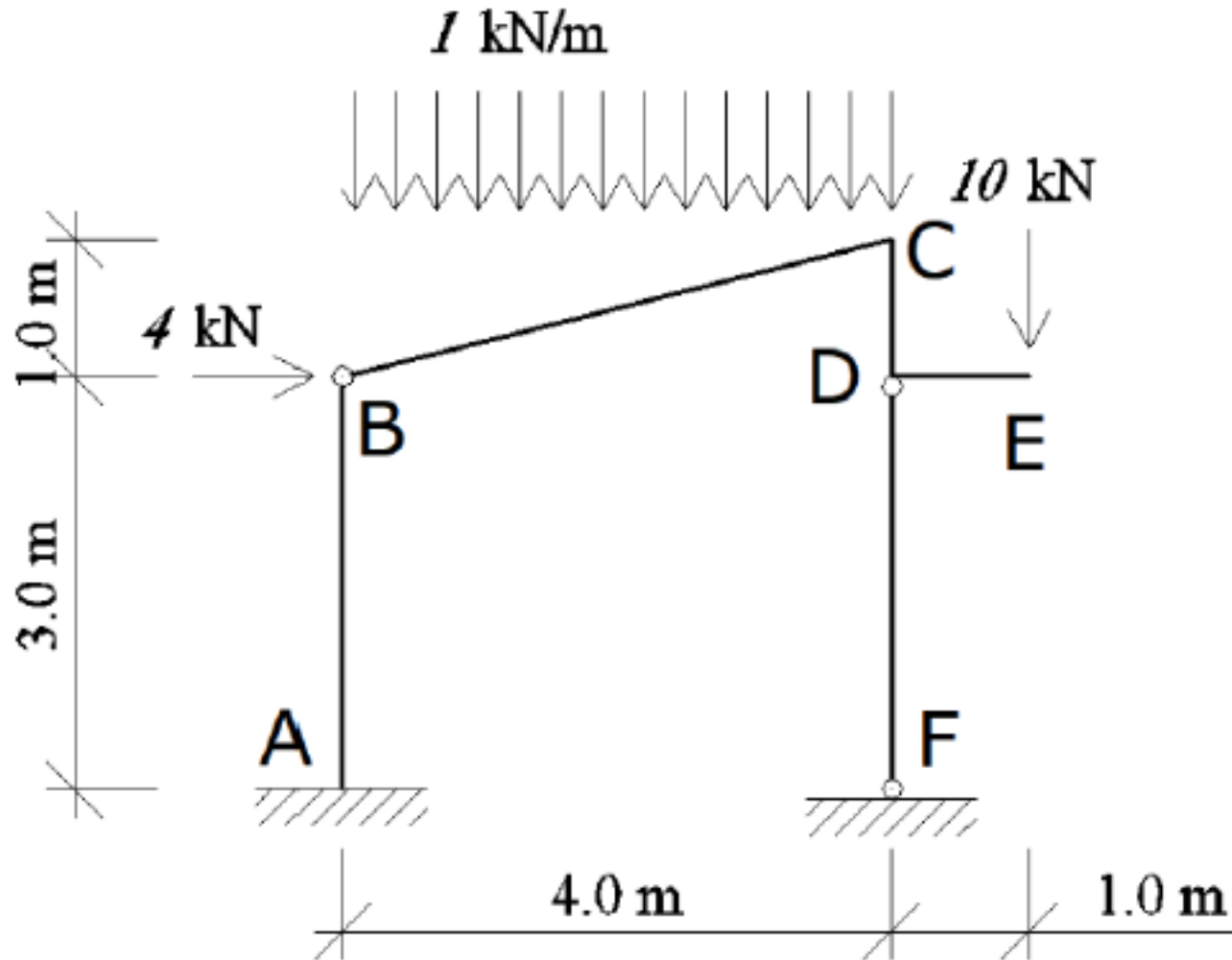
La estructura de la figura 4, ABCDEF, se encuentra sometida a una carga uniformemente distribuida hacia abajo de 1 kN/m en el tramo BC, a una carga puntal de 10 kN hacia abajo aplicada en el punto E y a una carga puntal de 4 kN horizontal y hacia la derecha aplicada en el punto B. La estructura se materializa mediante una sección formada por un perfil PNI 120 y dos planchuelas metálicas de 10 mm de espesor cada una; siendo éstas del mismo material que el perfil. Se pide:



UNIDADES EN *mm*.

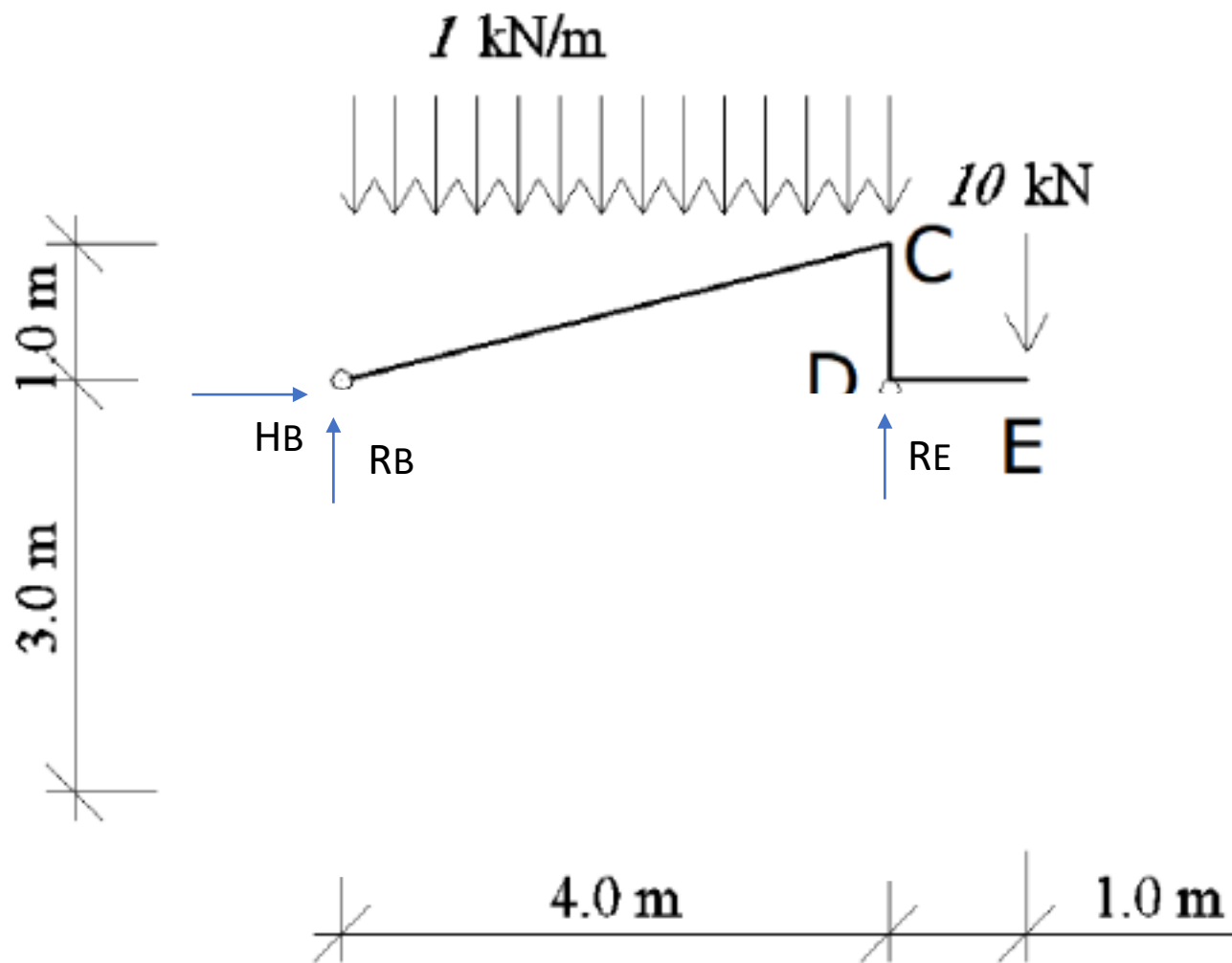
- a) Trazar los diagramas de solicitaciones.
 - b) Hallar el valor del ancho a de las planchuelas,
- tensión normal admisible de 140 MPa
 tensión rasante admisible de 90 MPa

Hallar reacciones



$$\cos(\alpha) = 4/\sqrt{17}$$
$$\cos(\alpha) = 0.97$$

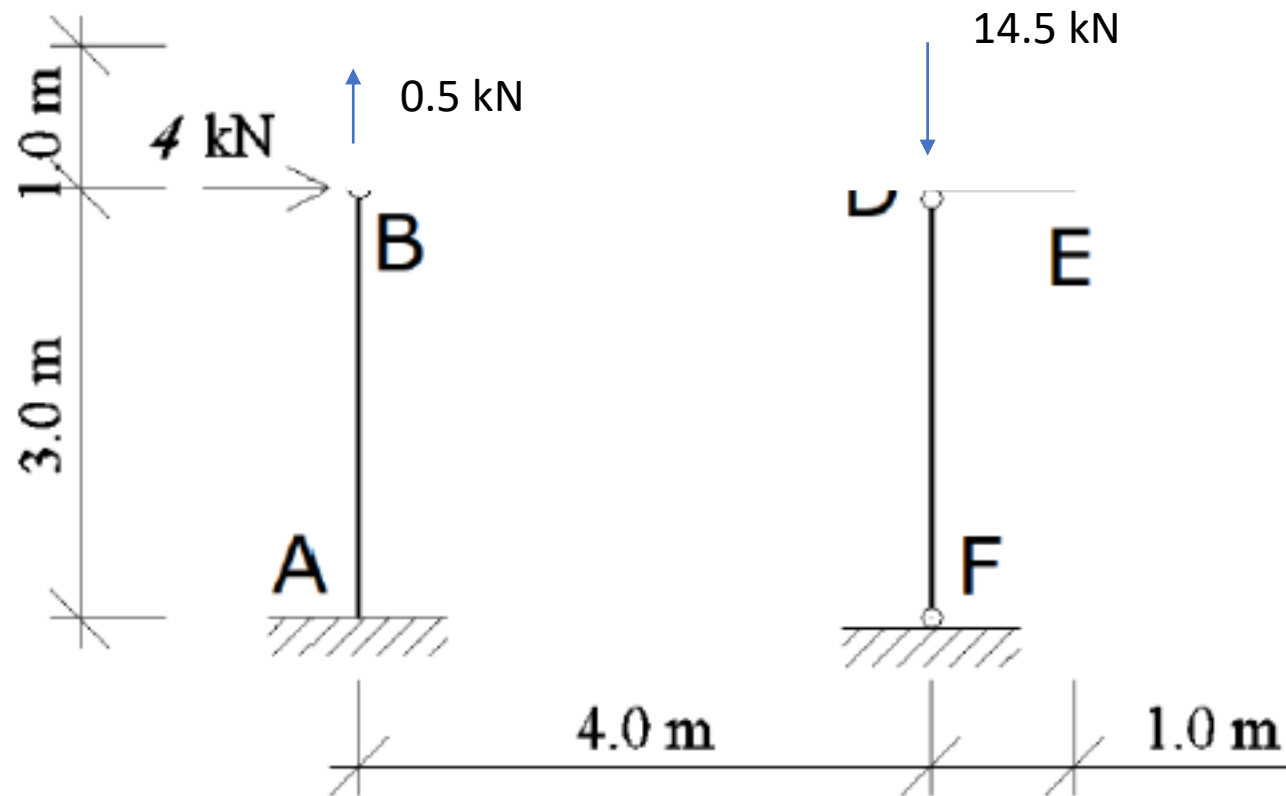
$$\sin(\alpha) = 1/\sqrt{17}$$
$$\sin(\alpha) = 0.24$$

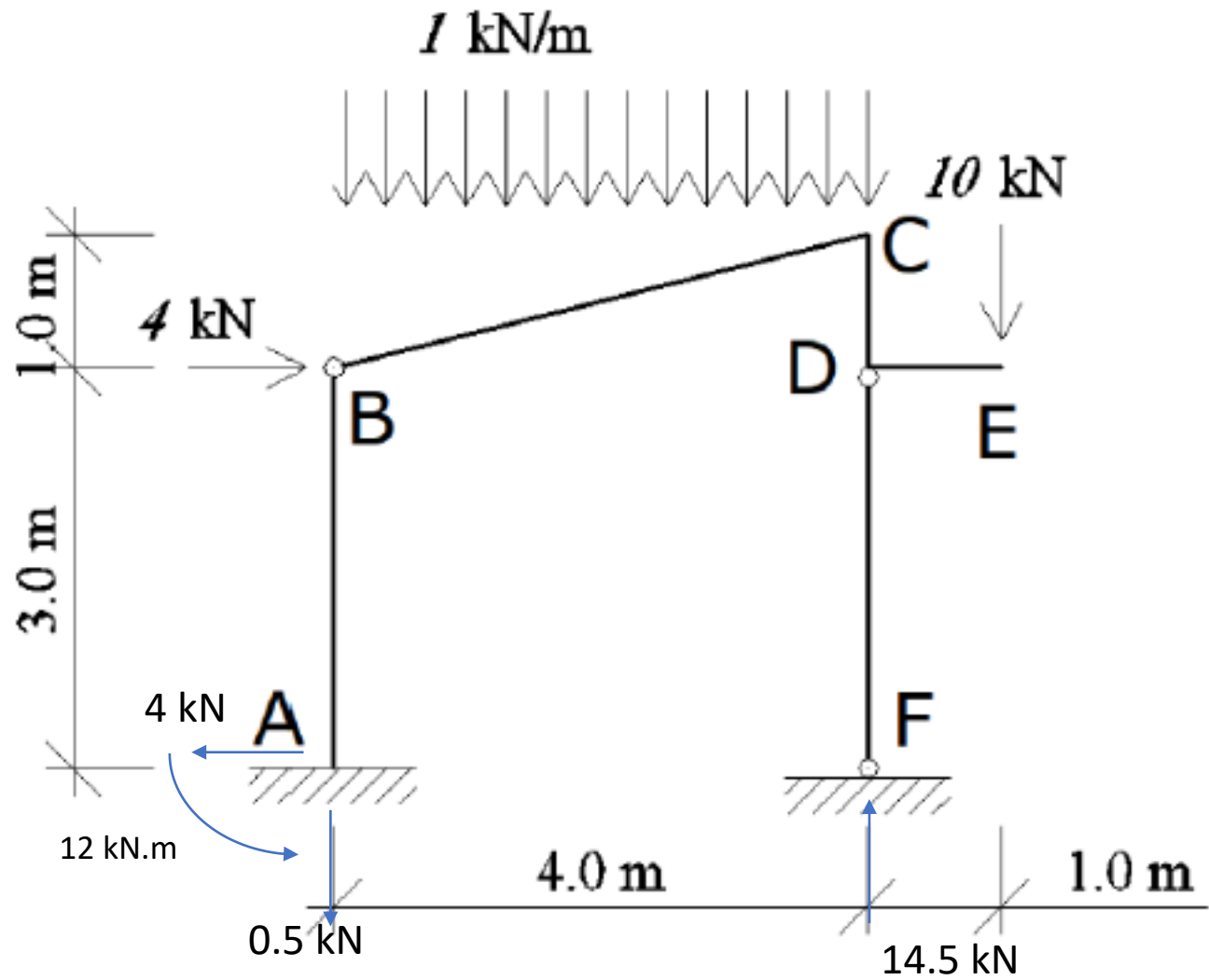


$$\begin{aligned} \text{Suma}(M_B) &= 0 \\ 4 \cdot 2 + 50 - 4 \cdot R_E &= 0 \\ R_E &= 14,5 \text{ kN} \end{aligned}$$

$$R_B = -0,5 \text{ kN}$$

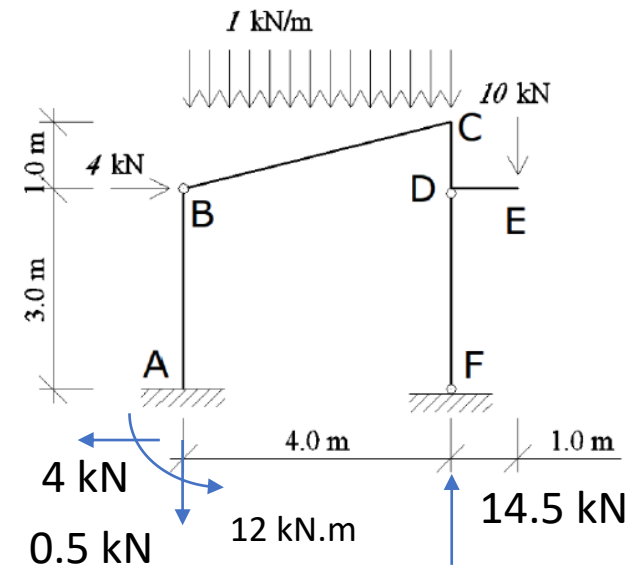
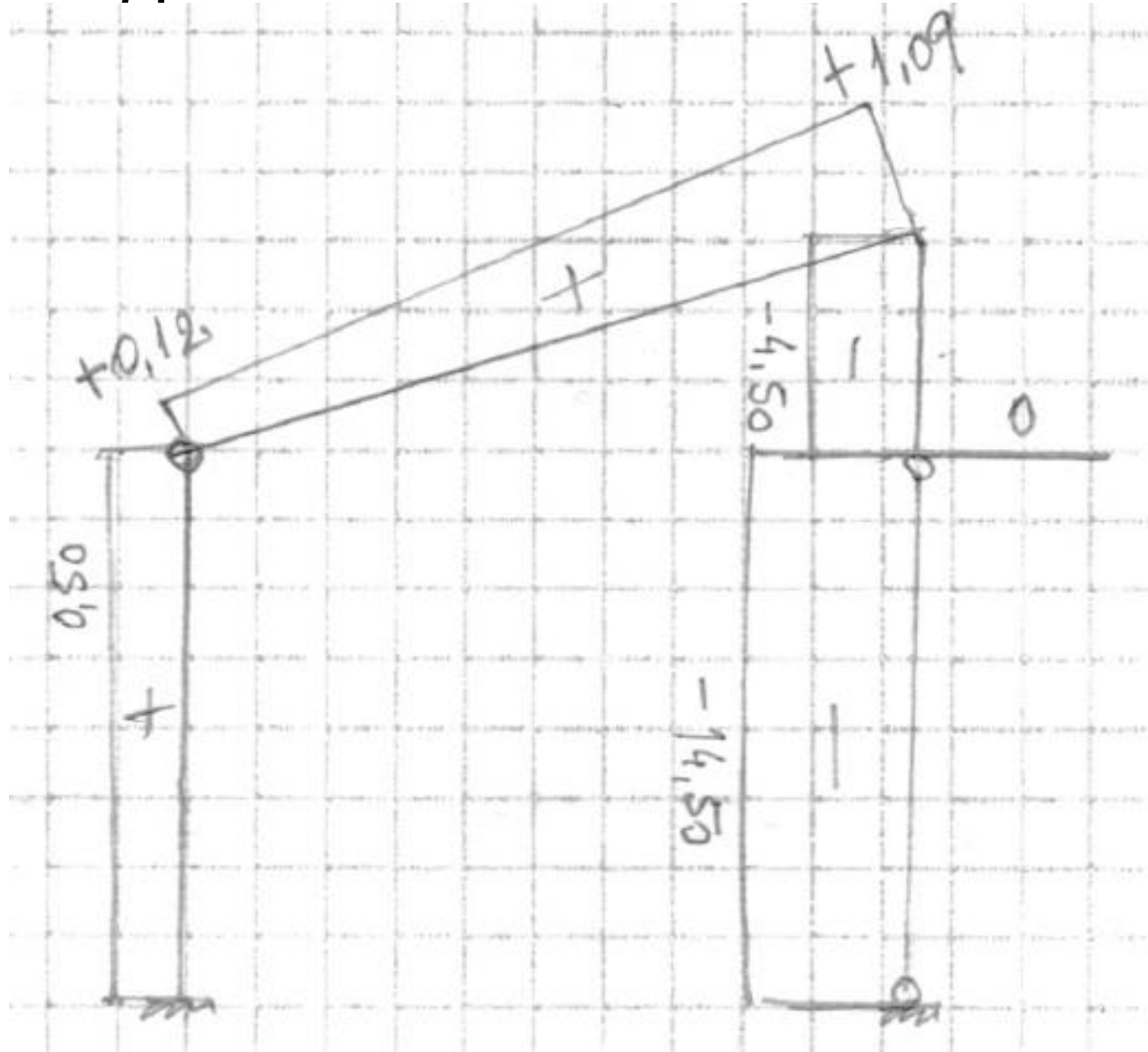
Hallar reacciones



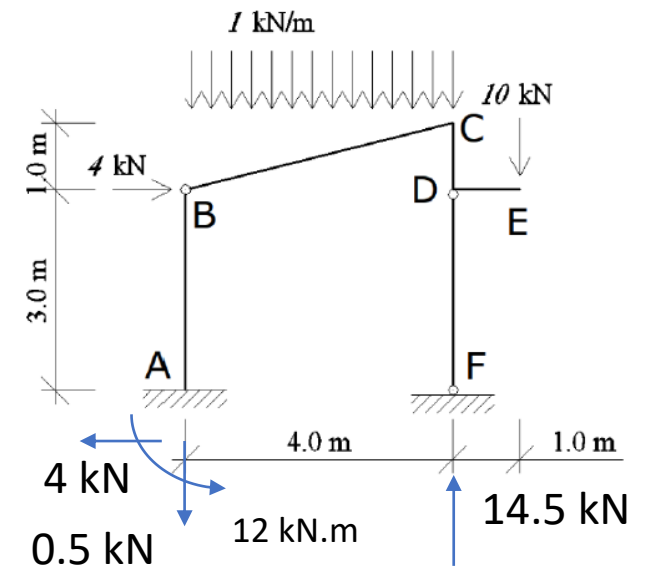
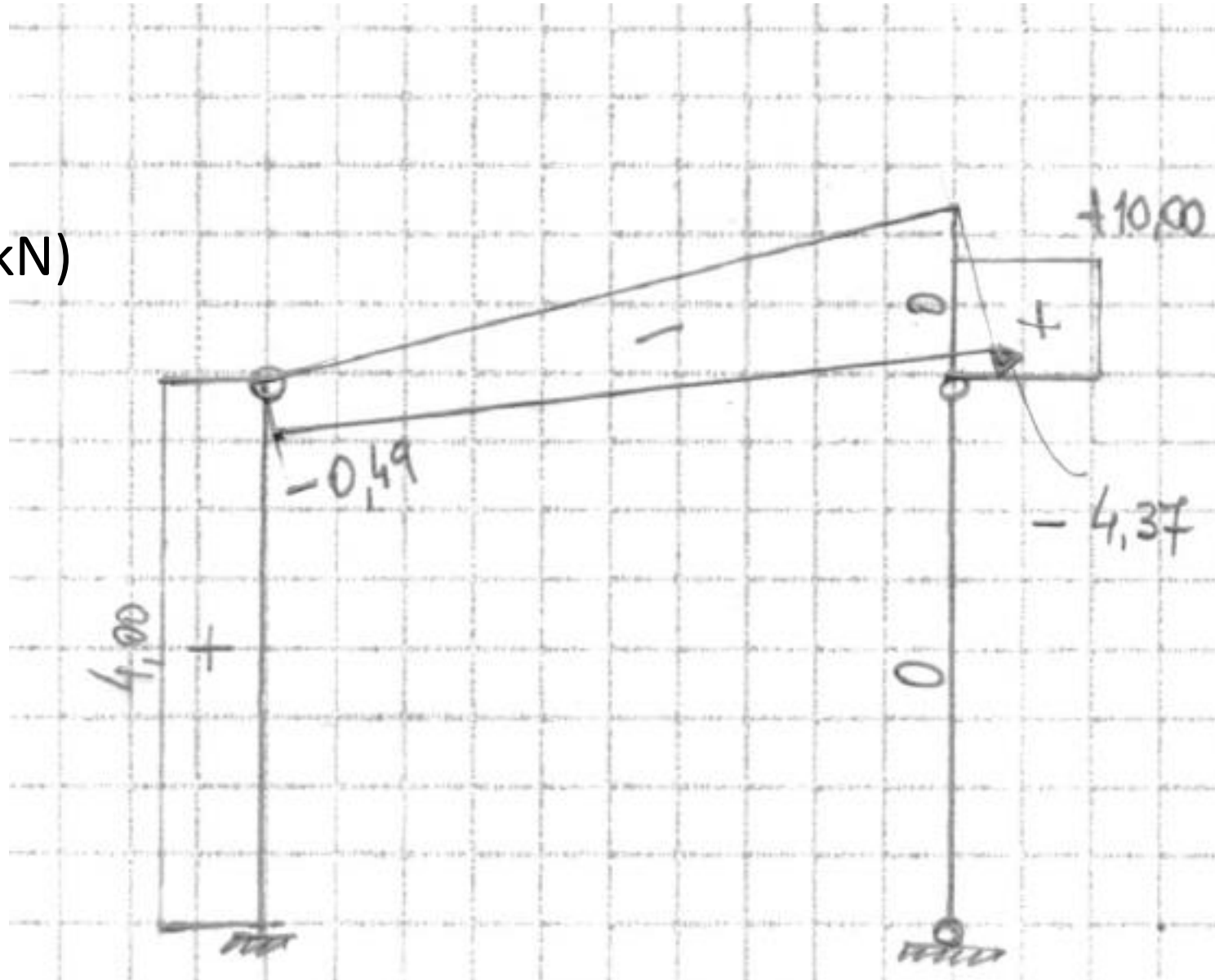


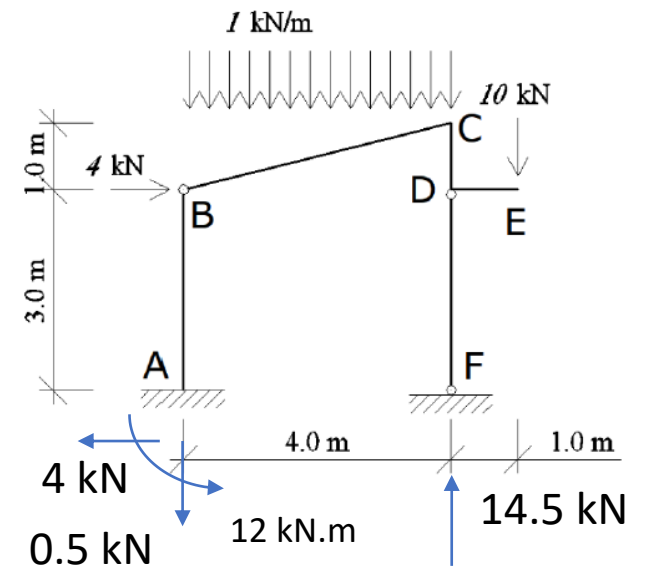
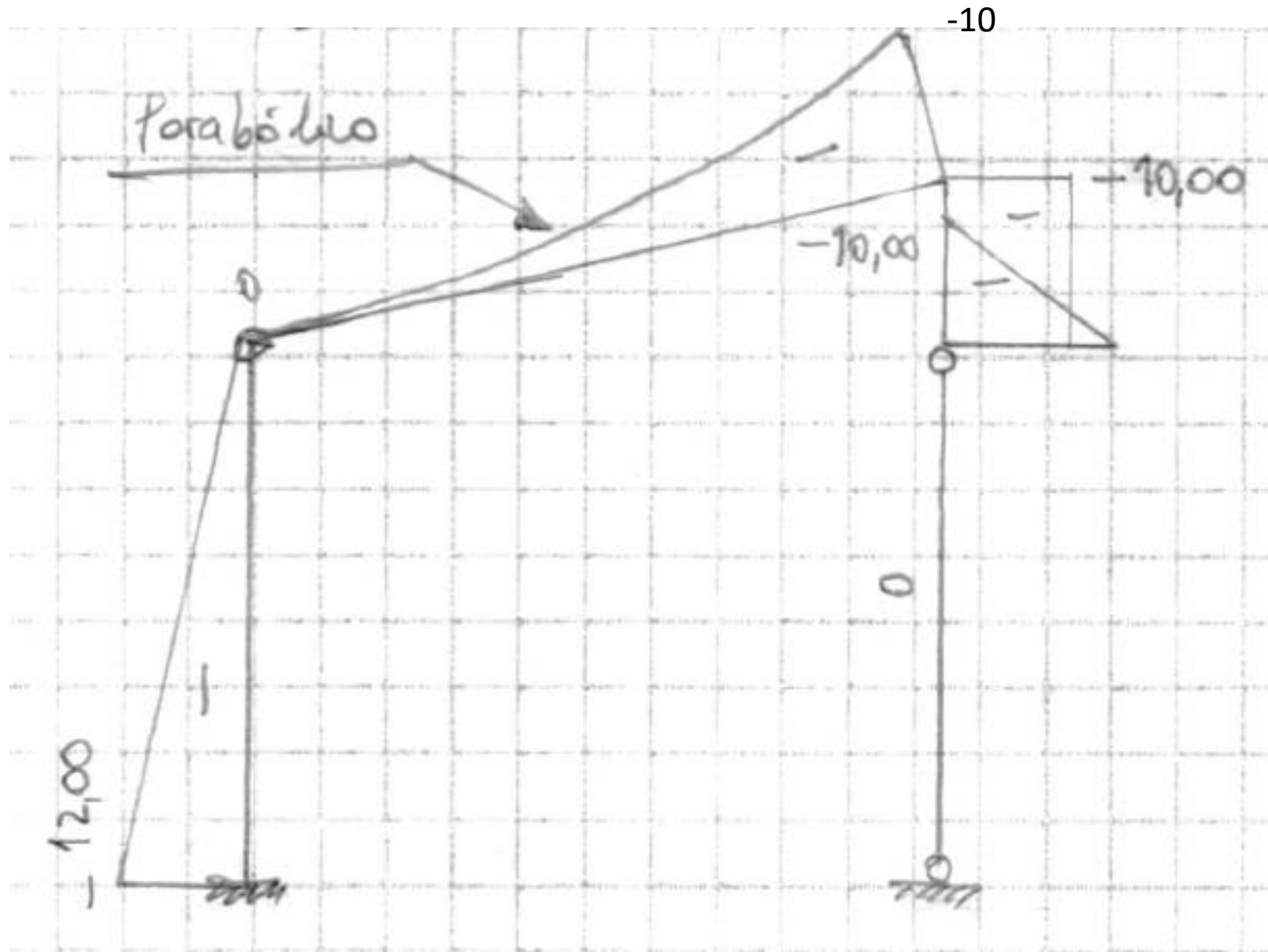
Trazar Diagramas

- N (kN)



• V(kN)





Dimensionado

- En barra AB: $M_{\max} = 12 \text{ kNm}$ y $N = +0.5 \text{ kN}$
- En CD: $M = 10 \text{ kNm}$ y $N = -4.5 \text{ kN}$
- $N = -14.5 \text{ kN}$
- $V = -10 \text{ kN}$

PNI 12

$$I_x = 328 \times 10^4$$

$$I_x = 2 \cdot \left(\frac{a \cdot 10^3}{12} + 10 \cdot a \cdot 65^2 \right)$$

Placas

$$I_x = 328 \times 10^4 + 84,67 \times 10^3 \cdot a \quad [\text{mm}^4]$$

PNI 12

EN A: $M_{\max} = 12 \text{ kNm}$ y $N = +0.5 \text{ kN}$

$$\sigma = \frac{500}{14,20 \times 10^2 + 20 \cdot a} + \frac{12 \times 10^6 \cdot 70}{328 \times 10^4 + 84,67 \times 10^3 a} \leq 140$$

$$237,086 \times 10^6 \cdot a^2 + 9,174 \times 10^9 a - 542,376 \times 10^9 \geq 0$$

$$a \geq 32,25 \text{ mm}, \text{ luego } \underline{\underline{a = 33 \text{ mm}}}$$

VERIFICACION EN CD: $M = 10 \text{ kNm}$ y $N = -4.5 \text{ kN}$

$$A = 2,080 \times 10^3 \text{ mm}^2$$

$$I_x = 6,074 \times 10^6 \text{ mm}^4$$

$$|\sigma| = 117,4 \leq 140 \text{ MPa} \quad (\text{OK})$$

VERIFICACION DE CONTANTES:

$$M_x = 31,8 \times 10^3 + 10,33 \cdot 65 = 53,25 \times 10^3 \text{ mm}^3$$

$$\tau = \frac{53,25 \times 10^3 \cdot 10000}{6,074 \times 10^6 \cdot 5,1} = 17,2 \text{ MPa} \leq 90 \text{ MPa} \rightarrow \underline{\underline{\text{OK}}} \checkmark$$