

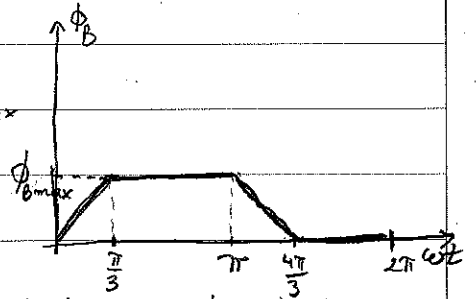
1.a) Área = $\frac{1}{2}\theta(b^2 - a^2)$; $\phi_b = B \cdot \frac{1}{2}\theta(b^2 - a^2)$, $\theta =$ ángulo en la región con B

$\rightarrow 0 < \omega t < \frac{\pi}{3}$, $\theta = \omega t$ $\phi_B = B \cdot \frac{1}{2}\omega t(b^2 - a^2)$

$\frac{\pi}{3} < \omega t < \pi$, $\theta = \frac{\pi}{3}$ $\phi_B = B \cdot \frac{\pi}{6}(b^2 - a^2) \equiv \phi_{Bmax}$

$\pi < \omega t < \frac{4\pi}{3}$, $\phi = \frac{4\pi}{3} - \omega t$ $\phi_B = B \cdot \frac{1}{2}(\frac{4\pi}{3} - \omega t)(b^2 - a^2)$

$\frac{4\pi}{3} < \omega t < 2\pi$, $\phi = 0$

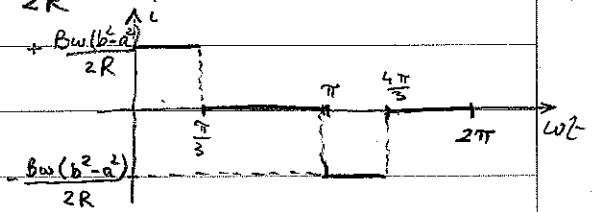


b) $0 < \omega t < \frac{\pi}{3}$, $|\frac{d\phi_B}{dt}| = B \frac{\omega}{2}(b^2 - a^2) \rightarrow i = + \frac{B\omega(b^2 - a^2)}{2R}$ (signo + por lenz)

$\frac{\pi}{3} < \omega t < \pi$, $|\frac{d\phi_B}{dt}| = 0 \rightarrow i = 0$

$\pi < \omega t < \frac{4\pi}{3}$, $|\frac{d\phi_B}{dt}| = B \frac{\omega}{2}(b^2 - a^2) \rightarrow i = - \frac{B\omega(b^2 - a^2)}{2R}$ (signo - por lenz)

$\frac{4\pi}{3} < \omega t < 2\pi$, $|\frac{d\phi_B}{dt}| = 0 \rightarrow i = 0$

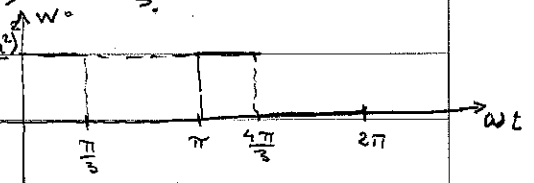


c) $W = Ri^2 \rightarrow W = \frac{B^2 \omega^2 (b^2 - a^2)^2}{4R}$ $0 < \omega t < \frac{\pi}{3}$ y en $\pi < \omega t < \frac{4\pi}{3}$

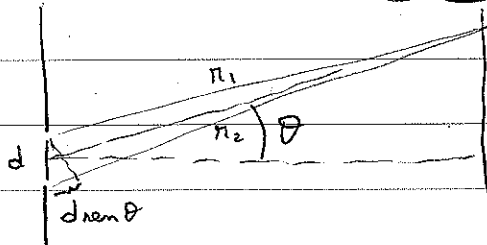
$W = 0$

$\frac{\pi}{3} < \omega t < \pi$ y en $\frac{4\pi}{3} < \omega t < 2\pi$

d) $\mathcal{E} = \frac{B^2 \omega^2 (b^2 - a^2)^2}{4R} \cdot 2 \cdot \frac{\pi}{3\omega} = \frac{\pi B^2 \omega (b^2 - a^2)^2}{6R}$



2.



Máximos en $d \cdot \text{sen} \theta = m \lambda$

Ceros en $d \cdot \text{sen} \theta = (m + \frac{1}{2}) \lambda$

a) $\lambda = 2d \Rightarrow \text{sen} \theta = 2m$; único máximo para $m=0 \Rightarrow \theta=0$, $y=0$

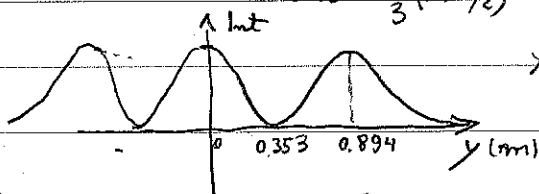
$\text{sen} \theta = 2(m + \frac{1}{2})$; único cero en $m=0 \Rightarrow \theta = \frac{\pi}{2}$ ($y \rightarrow \infty$)

b) $\lambda = \frac{2d}{3}$, $\text{sen} \theta = \frac{2m}{3}$; máximos en $m=0 \Rightarrow \theta=0$, $y=0$

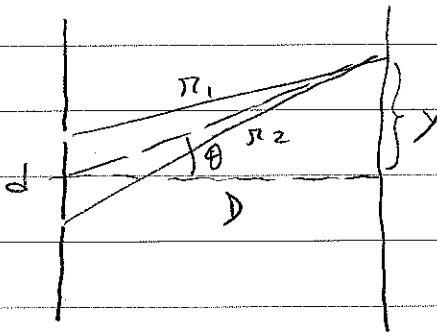
y en $m=1$, $\text{sen} \theta = \frac{2}{3}$, $\theta = 41,8^\circ$, $y = D \text{tg} \theta = 0,894 \text{ m}$

$\text{sen} \theta = \frac{2}{3}(m + \frac{1}{2})$; cero en $m=0$, $\text{sen} \theta = \frac{1}{3}$, $\theta = 19,5^\circ$, $y = 0,353 \text{ m}$

y en $m=1$, $\text{sen} \theta = 1$, $\theta = \frac{\pi}{2}$, $y = \infty$



2. Otra forma (sin usar θ): $r_1 = \sqrt{D^2 + (y - \frac{d}{2})^2}$, $r_2 = \sqrt{D^2 + (y + \frac{d}{2})^2}$



$$r_2 - r_1 = \sqrt{D^2 + y^2 + \frac{d^2}{4} + dy} - \sqrt{D^2 + y^2 + \frac{d^2}{4} - dy}$$

$$= \sqrt{D^2 + y^2} \left[\sqrt{1 + \frac{\frac{d^2}{4} + dy}{D^2 + y^2}} - \sqrt{1 + \frac{\frac{d^2}{4} - dy}{D^2 + y^2}} \right]$$

$$\approx \sqrt{D^2 + y^2} \left[1 + \frac{1}{2} \left(\frac{\frac{d^2}{4} + dy}{D^2 + y^2} \right) - \left(1 + \frac{\frac{d^2}{4} - dy}{D^2 + y^2} \right) \right]$$

$$= \frac{dy}{\sqrt{D^2 + y^2}} = \begin{cases} m\lambda & \text{- constructiva} \\ (m + \frac{1}{2})\lambda & \text{- destructiva} \end{cases}$$

$\lambda = 2d \Rightarrow \frac{y}{\sqrt{D^2 + y^2}} = \begin{cases} 2m & \rightarrow \text{Solo } m=0, y=0 \\ 2(m + \frac{1}{2}) & \rightarrow \text{Solo } m=0, y=+\infty \end{cases}$

$\lambda = \frac{2d}{3} \Rightarrow \frac{y}{\sqrt{D^2 + y^2}} = \begin{cases} \frac{2}{3}m & \rightarrow m=0 \rightarrow y=0, \frac{y}{\sqrt{D^2 + y^2}} = \frac{2}{3}, y = \frac{2}{15}D = 0,894m \\ \frac{2}{3}(m + \frac{1}{2}) & \rightarrow m=0 \rightarrow \frac{y}{\sqrt{D^2 + y^2}} = \frac{1}{3} \rightarrow y = \frac{1}{15}D = 0,353, m=1 \rightarrow \frac{y}{\sqrt{D^2 + y^2}} = 1, y = \infty \end{cases}$

3. a) $V_{ef} = R \cdot i_{ef} \Rightarrow R = \frac{220}{5} = 44 \Omega$, $W = R \cdot i_{ef}^2 = 44 \times 5^2 = 1100 \text{ W}$

b) $i_{ef} = \frac{V_{ef}}{\sqrt{R^2 + (\omega L)^2}} \Rightarrow R^2 + (\omega L)^2 = \left(\frac{V_{ef}}{i_{ef}} \right)^2 = \left(\frac{220}{4} \right)^2 = 55^2 \Rightarrow \omega L = \sqrt{55^2 - 44^2} = 33 \Omega$

$\rightarrow L = \frac{33}{100\pi} = 0,105 \text{ H}$

c) $i_{ef} = \frac{V_{ef}}{\sqrt{R^2 + (\omega L - \frac{1}{\omega C})^2}}$

$W = R \cdot i_{ef}^2 = 44 \times 4^2 = 704 \text{ W}$

$\rightarrow R^2 + (\omega L - \frac{1}{\omega C})^2 = \left(\frac{V_{ef}}{i_{ef}} \right)^2 = \left(\frac{220}{5} \right)^2 = 44^2 \Rightarrow \omega L - \frac{1}{\omega C} = 0$

$C = \frac{1}{\omega^2 L} = \frac{1}{(100\pi)^2 \times 0,105} = 96,5 \mu\text{F}$

$W = R \cdot i_{ef}^2 = 44 \times 5^2 = 1100 \text{ W}$

d) $i_{ef} = \frac{V_{ef}}{\sqrt{R^2 + (\omega'L - \frac{1}{\omega C})^2}}$

$\omega'L = 120\pi \times 0,105 = 39,6 \Omega$

$\frac{1}{\omega C} = \frac{1}{120\pi \times 96,5 \times 10^{-6}} = 27,5 \Omega$

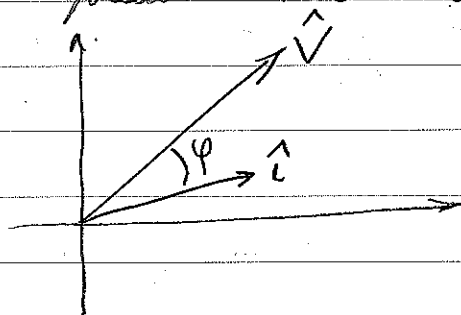
$\Rightarrow i_{ef} = \frac{220}{\sqrt{44^2 + (39,6 - 27,5)^2}} = 4,82 \text{ A}$

$W = R \cdot i_{ef}^2 = 44 \times 4,82^2 = 1023 \text{ W}$

$W = V_{ef} \cdot i_{ef} \cdot \cos \varphi = 1023 \text{ W} \Rightarrow \cos \varphi = \frac{1023}{220 \times 4,82} = 0,965 = \text{factor de pot.}$

e) Como $\omega'L > \frac{1}{\omega C}$

predominantemente inductivo



$\varphi = \arccos 0,965 = 15,3^\circ$

