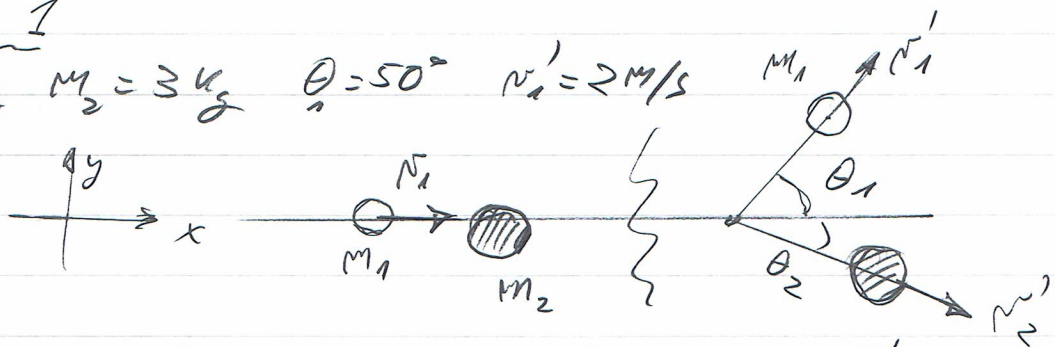


Física 1. Tecnólogo - 2^{da} parcial 28/11/2019

Ejercicio 1

$m_1 = 1 \text{ kg}$ $m_2 = 3 \text{ kg}$ $\theta = 50^\circ$ $v_1' = 2 \text{ m/s}$
 $v_1 = 6 \text{ m/s}$



Conservación en P_x : $m_1 v_1 = m_1 v_1' \cos \theta_1 + m_2 v_2' \cos \theta_2$
 $\Rightarrow 6 = 1,29 + 3 v_2' \cos \theta_2 \Rightarrow v_2' \cos \theta_2 = 1,57 \frac{\text{m}}{\text{s}}$

Conservación en P_y : $0 = m_1 v_1' \sin \theta_1 - m_2 v_2' \sin \theta_2$
 $\Rightarrow 0 = 1,53 - 3 v_2' \sin \theta_2 \Rightarrow v_2' \sin \theta_2 = 0,51 \frac{\text{m}}{\text{s}}$

a) $v_2' = \sqrt{v_{2x}'^2 + v_{2y}'^2} = 1,65 \frac{\text{m}}{\text{s}}$ $\theta_2 = \arctan \frac{v_{2y}'}{v_{2x}'} \approx 18^\circ$

$K_{\text{ini}} = \frac{1}{2} m v_1^2 = 18 \text{ J}$ $K_{\text{fin}} = \frac{1}{2} m_1 v_1'^2 + \frac{1}{2} m_2 v_2'^2$

$K_{\text{fin}} = 2 + 4,08 = 6,08 \text{ J} \Rightarrow \Delta K = 6,08 - 18 = -11,92$

b) Se invirtieron 11,92 J en la deformación.

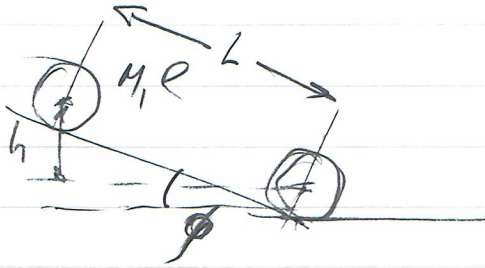
$\vec{I}_1 = \Delta \vec{P}_1 \Rightarrow I_{1x} = \Delta P_{1x} = m_1 v_1' \cos \theta_1 - m_1 v_1$
 $I_{1x} = m_1 v_1' \cos \theta_1 - m_1 v_1 = -4,71 \frac{\text{kg} \cdot \text{m}}{\text{s}}$

$I_{1y} = \Delta P_{1y} = m_1 v_1' \sin \theta_1 - 0 = m_1 v_1' \sin \theta_1 = 1,53 \frac{\text{kg} \cdot \text{m}}{\text{s}}$

c) $I_1 = \sqrt{I_{1x}^2 + I_{1y}^2} = 4,95 \frac{\text{kg} \cdot \text{m}}{\text{s}}$ $\gamma = \arctan \left| \frac{I_{1y}}{I_{1x}} \right| \approx 18^\circ$

Ejercicio 2

Conservación de la energía:



$$K_{\text{final}} = U_{\text{inicial}} \Rightarrow \frac{1}{2} M v_{\text{cm}}^2 + \frac{1}{2} I \omega^2 = M g h$$

$$\omega = v_{\text{cm}}/R \Rightarrow \frac{1}{2} M v_{\text{cm}}^2 + \frac{1}{2} \frac{I}{R^2} v_{\text{cm}}^2 = M g h$$

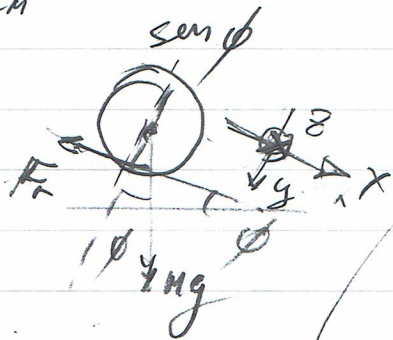
$$\frac{1}{2} v_{\text{cm}}^2 \left(M + \frac{I}{R^2} \right) = M g h \Rightarrow v_{\text{cm}}^2 = \frac{2 M g h}{M + I/R^2}$$

$$v_{\text{cm}} = \sqrt{\frac{2 g h}{1 + I/MR^2}} \Rightarrow \text{Cilindro } I = \frac{1}{2} M R^2 \Rightarrow$$

a)
$$v_{\text{cm}}^{\text{(cil)}} = \sqrt{\frac{4 g h}{3}}$$

anillo: $I = M R^2 \Rightarrow v_{\text{cm}}^{\text{(an)}} = \sqrt{g h}$

$$L = \frac{1}{2} a_{\text{cm}} t^2 = h \Rightarrow t = \sqrt{\frac{2 h}{a_{\text{cm}} \text{ sen } \phi}}$$



$$F_x = M g \text{ sen } \theta - F_r = M a_{\text{cm}}$$

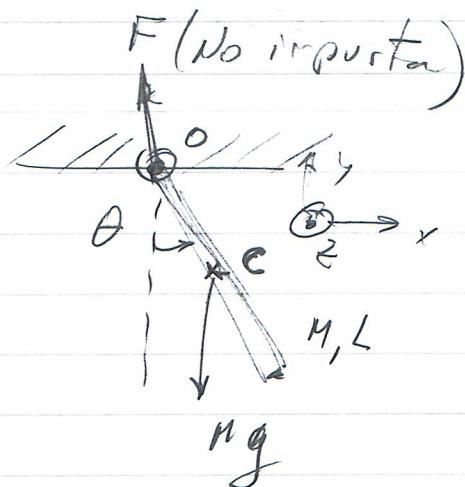
$$\tau_z = F_r R = I \alpha = I \frac{a_{\text{cm}}}{R} \Rightarrow$$

$$\Rightarrow F_r = \frac{I a_{\text{cm}}}{R^2} \rightarrow M g \text{ sen } \theta - \frac{I}{R^2} a_{\text{cm}} = M a_{\text{cm}}$$

$$g \text{ sen } \theta - \frac{I}{M R^2} a_{\text{cm}} = a_{\text{cm}} \Rightarrow a_{\text{cm}} = \frac{g \text{ sen } \theta}{1 + I/MR^2}$$

b) Cilindro $I = \frac{1}{2} M R^2 \Rightarrow a_{\text{cm}} = \frac{2 g \text{ sen } \theta}{3} \Rightarrow t = \frac{1}{\text{sen } \theta} \sqrt{\frac{3 h}{g}}$

Ejercicio 3



$$\tau_0 = -Mg \frac{L}{2} \sin \theta = I_0 \ddot{\theta}$$

$$\ddot{\theta} + \frac{Mg \frac{L}{2} \sin \theta}{I_0} = 0$$

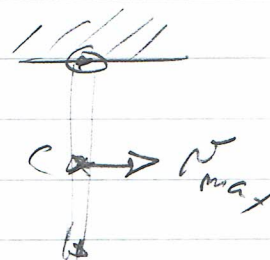
pequeñas oscilaciones $\sin \theta \approx \theta \Rightarrow$

$$\ddot{\theta} + \frac{Mg \frac{L}{2} \theta}{I_0} = 0 \quad I_0 = I_c + M \left(\frac{L}{2}\right)^2 = \frac{1}{12} ML^2 + \frac{ML^2}{4}$$

$$I_0 = \frac{1}{3} ML^2 \Rightarrow \ddot{\theta} + \frac{3g}{2L} \theta = 0 \quad \text{a)}$$

$$\omega = \sqrt{\frac{3g}{2L}} = \frac{2\pi}{T} \Rightarrow T = 2\pi \sqrt{\frac{2L}{3g}} \quad \text{b)}$$

$$\theta(t) = \theta_0 \cos \omega t \quad \dot{\theta}(t) = -\omega \theta_0 \sin \omega t$$



$$\dot{\theta}_{\text{max}} = \omega \theta_0 \approx v_{\text{max}} / (L/2)$$

$$v_{\text{max}} \approx \frac{L}{2} \omega \theta_0 \approx \frac{\theta_0}{2} \sqrt{\frac{3gL}{2}} \quad \text{c)}$$

$$\dot{\theta}_{\text{max}} = \frac{1}{2} \sqrt{3gL(1 - \cos \theta_0)}$$

Conservación energía sin aproximación de pequeñas oscilaciones