



IH-2VOF Model

Mathematical/Numerical description



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OUTLINE

- 1.1 Wave transformation processes. Scope of application of the model
- 1.2. Approaches of study
 - physical experiments
 - numerical modeling
- 1.3 Why Navier-Stokes Models in coastal engineering?





1.1. Wave transformation processes

• General aspects



Wave transforms









Coastal structures











1.1. Wave transformation processes (Design analysis)

Functional analysis of the structure

- Any coastal structure is designed based on fulfill some requirements to be used.
- The lost of such as conditions implies failure: lost of functionality ("usability")
- Structural damage cannot appear

Structural failure of the structure

- Total or partial lost of the characteristics of the structure established in the design
- Structural damage: recovered or unrecovered







1.1. Wave transformation processes (Design analysis: Functionality)

<u>Run-up (R_{u})</u>: Vertical distance above SWL reached by the waves

<u>Run-down (R_d)</u>: Vertical distance below SWL reached by the waves

Overtopping discharge (q): Amount of water per unit time exceeding the breakwater crest

Wave Transmission: Wave agitation behind the structure











1.1. Wave transformation processes (Design analysis: Stability)









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1.2. Approaches of study (Physical tests)

Classical approach:



Mainly two-dimensional and small-scale tests

For development of most of the formulations used for design

Problems:

Froude scaling → Mach or Reynolds numbers are not conserved
Processes related with breaking and turbulence are not very well modeled
Not all the magnitudes of interest can be recorded

Economical cost:

•number of experiments \rightarrow repeatability of experiments

•Large scale experiments \rightarrow expensive

Results with a narrow range of applicability

New motivations: aesthetic, economical and environmental reasons









1.2. Approaches of study (Numerical modelling)

Non-linear Shallow Water Equations / Boussinesq

- Pros: cheap according to the computational cost, efficient, long simulations (reliable statistics) ...
- Cons: Wave breaking have to be triggered, vertical structures cannot be simulated, overtopping cannot be calculated, pressure field is not provided, wave dispersion, ...

SPH (Smooth Particle Hydrodynamics) models

- Pros: non-linear interaction in the fluid, pressure field is obtained, multi-connected free surface, ...
- Cons: ongoing research, porous media flow is not solved, highly diffusive, pressure field needs to be tailored adapted ...

<u>Navier-Stokes models \rightarrow RANS</u>

- Pros: non-linear interaction in the fluid, pressure field is obtained, multi-connected free surface, porous media flow, turbulence is considered, ...
- Cons: high computational cost, efficiency, methodology of use in coastal engineering





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1.3 Why Navier-Stokes Models in coastal engineering?





Why Navier-Stokes Models in coastal engineering?

- The <u>number of underlying assumptions is quite low</u> comparing with other approaches
- <u>Non-linear flow characteristics</u> during wave transformation are considered
- <u>Wave dispersion</u> is intrinsically included in the equations
- <u>Breaking is not triggered</u> artificially
- Wave induced flow is solved in the vertical (2D or 3D)
- <u>Wave-induced turbulence</u> can be considered
- <u>Huge potential</u> to find new insights in physical process which are nowadays studied with simplified models due to their complexity
- <u>Parallel computing</u> (not IH-2VOF)





Weak points of Navier-Stokes models when applying to coastal engineering

- Although their use is quite common in other fields (mechanical, aerospace, chemical, etc.), it is <u>not very</u> <u>common in civil engineering</u>
- The <u>computational cost is high</u> and can not solved for large domains or long periods.
- The <u>cost of commercial software is quite high</u> and a special training is required to get accurate results
- There are specific issues related with the wave induced flow which are not correctly solved and/or not implemented in commercial software packages: wave generation, wave absorption, porous media flow
- The use of a <u>massive computing machine</u> is required to be used for complex problems and geometries.
- There is a <u>lack of a methodology</u> to be applied to coastal engineering problems





2. IH-2VOF MODEL

OUTLINE

2.1 Mathematical model

- Navier-Stokes equations
- VARANS equations

2.2 Numerical implementation

- Computational domain
- Partial cell method
- Volume of Fluid Method
- Solving procedure
- Computational cycle





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2.3 Wave boundary condition

- Introduction
- Methods
- Wave absorption

2.4 Mesh generator: CORAL







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• Mass and momentum conservation equations:

$$\vec{\nabla}\cdot\vec{V}=0$$

$$\rho \frac{D \vec{V}}{D t} = \rho \vec{g} + \nabla \cdot \sigma_{ij}$$

4 Equations and 10 unknowns

VTERNACIONAL

$$\sigma_{ij} = \begin{pmatrix} \sigma_{xx} & \sigma_{xy} & \sigma_{xz} \\ \sigma_{yx} & \sigma_{yy} & \sigma_{yz} \\ \sigma_{zx} & \sigma_{zy} & \sigma_{zz} \end{pmatrix} = \begin{pmatrix} -p & 0 & 0 \\ 0 & -p & 0 \\ 0 & 0 & -p \end{pmatrix} + \begin{pmatrix} \tau_{xx} & \tau_{xy} & \tau_{xz} \\ \tau_{yx} & \tau_{yy} & \tau_{yz} \\ \tau_{zx} & \tau_{zy} & \tau_{zz} \end{pmatrix}$$



• Terms in momentum equations:





Reynolds Average Navier-Stokes Equations

Equations in the fluid region

$$u_i = u_i + u_i'$$
; $p = p + p'$

- u_i: mean velocity (ensemble average)
- u'_i : turbulent fluctuation
- u_i: instantaneous velocity







Nonlinear Reynolds stress closure model

Shih et al. (1999) $\overline{u_i'u_j'} = \frac{2}{3}k\delta_{ij} - 2v_iS_{ij}$ $-\frac{k^{3}}{\varepsilon^{2}}\left[C_{1}\left(\frac{\partial\overline{u_{i}}}{\partial x_{l}}\frac{\partial\overline{u_{l}}}{\partial x_{j}}+\frac{\partial\overline{u_{j}}}{\partial x_{l}}\frac{\partial\overline{u_{l}}}{\partial x_{i}}-\frac{2}{3}\frac{\partial\overline{u_{l}}}{\partial x_{k}}\frac{\partial\overline{u_{k}}}{\partial x_{l}}\delta_{ij}\right)\right]$ $+C_2\left(\frac{\partial \overline{u_i}}{\partial x_k}\frac{\partial \overline{u_j}}{\partial x_k}-\frac{1}{3}\frac{\partial \overline{u_l}}{\partial x_k}\frac{\partial \overline{u_l}}{\partial x_k}\delta_{ij}\right)$ Eddy viscosity $+C_{3}\left(\frac{\partial \overline{u_{k}}}{\partial x_{i}}\frac{\partial \overline{u_{k}}}{\partial x_{i}}-\frac{1}{3}\frac{\partial \overline{u_{l}}}{\partial x_{k}}\frac{\partial \overline{u_{l}}}{\partial x_{k}}\delta_{ij}\right)]$ $V_t = C_d \frac{k^2}{c}$

Reynolds stresses are dependent only on the mean velocity gradients and the characteristic scales of turbulence characterized by the turbulent kinetic energy k and its dissipation rate ε



Coefficients

k-ε turbulence transport model:

$$C_{1\varepsilon} = 1.44$$
 $C_{2\varepsilon} = 1.90$ $\sigma_k = 1.0$ $\sigma_{\varepsilon} = 1.3$

Nonlinear Reynolds Stress Closure Model:

Boundary conditions:

k-e turbulence transport model

Free surface: no flux condition

Solid wall: log-law turbulent boundary layer

$$\frac{\partial k}{\partial n} = \frac{\partial \varepsilon}{\partial n} = 0$$
$$\frac{u_n}{u_*} = \frac{1}{\kappa} \ln \frac{Eu_* y}{v}$$

RANS equations

Free surface: zero shear stress

Solid wall: non-slip condition

$$\tau_s = 0 \qquad \tau_n = p$$
$$\overline{u_t} = \overline{u_n} = 0$$

2.1 Mathematical model (VARANS equations)

Momentum equations:

$$\frac{\partial q_i}{\partial t} + \frac{q_j}{n(1+c_A)} \frac{\partial q_i}{\partial x_j} = \frac{n}{\rho(1+c_A)} \left[-\frac{\partial \langle \overline{p} \rangle}{\partial x_i} - \frac{\partial \rho \langle \overline{u_i'u_j'} \rangle}{\partial x_j} + \frac{\partial \langle \overline{\tau}_{ij} \rangle}{\partial x_j} + \rho g_i \right]$$
$$-\frac{n}{1+c_A} \left[\frac{\alpha v(1-n)^2}{n^3 D_{50}^2} q_i + \frac{\beta(1-n)}{n^3 D_{50}} \sqrt{q_1^2 + q_2^2} q_i \right]$$

Formulations for porous induced drag:

Autnors	a	D
Kozeny (1927)	$36\kappa\frac{(1-n)^2}{n^3}\frac{\nu}{gd^2}, \kappa=5$	0
Ergun (1952)	$150 \frac{(1-n)^2}{n^3} \frac{\nu}{g d^2}$	$1.75 \frac{1-n}{n^3} \frac{1}{gd}$
Engelund (1953)	$\alpha_E \frac{(1-n)^3}{n^2} \frac{\nu}{gd^2}$	$\beta \frac{1-n}{n^3} \frac{1}{gd}$
Ward (1964)	$\frac{\nu}{gK_s}$	$\frac{c}{g\sqrt{K_s}}, c = 0.550$
van Gent (1995)	$1000 \frac{(1-n)^2}{n^3} \frac{\nu}{g d_{50}^2}$	$1.1 \frac{(1-n)}{n^3} \frac{1}{gd_{50}}$
Liu <i>et al.</i> (1999b)	$200 \frac{(1-n)^2}{n^3} \frac{\nu}{g d_{50}^2}$	$1.1\frac{(1-n)}{n^3}\frac{1}{gd_{50}}$

2.1 Mathematical model (VARANS equations)

Friction coefficients

-Linear friction coefficient $\rightarrow \alpha$

+ α=200

+Limited influence (Lara, 2002)

+ β depends on geometry, flux, etc...

+Has been calibrated at laboratory scale

+A prototype scale calibration is needed

Non linear friction coefficients typical values			
Autor	Descripción	β	
Lara (2002)	Wave breaking over porous slopes	0.2	
Garcia (2005)	Submerged sea dikes	1.2 (core) 0.8 (External layers)	
Guanche (2007)	Vertical and composite breakwaters	Vertical: 0.8 (Ext.layer) 1.1 (core) Composite: 0.8 (core); 1.1 (Int.layer); 0.7 (Ext.layer)	

2.1 Mathematical model (VARANS equations)

Transport equations for k and ε:

small scale turbulence quantities:

Generation of turbulence smaller than the volume averaging scale

Nakayama and Kuwahara (1999):

$$\varepsilon_{\infty} = 39.0 \frac{(1-n)^{2.5}}{n} (q_1^2 + q_2^2)^{3/2} \frac{1}{D_{50}}$$
$$k_{\infty} = 3.7 \frac{(1-n)}{\sqrt{n}} (q_1^2 + q_2^2)$$

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2.2 Numerical implementation

Finite differences: rectangular domain, strutured orthogonal mesh

Free surface reconstruction based on a VOF technique (VOF function)

Solid boundary: partial cell treatment (infinite density, openness function)

Two step projection method (Chorin, 1968 and 1969)

2.2 Numerical implementation (Computational domain)

Finite differences:

- rectangular domain
- Structured orthogonal grid
- Center of cell: Pressure, VOF, k, ε
- Cell edges: Velocity

2.2 Numerical implementation (Volume Of Fluid, VOF, Technique)

Hirt & Nichols, 1981

$$\frac{\partial F}{\partial t} + \frac{\partial}{\partial x}(uF) + \frac{\partial}{\partial y}(vF) = 0$$

$$F = \frac{\rho}{\rho_f}$$

$$\left|\frac{\partial F}{\partial y}\right| > \left|\frac{\partial F}{\partial x}\right| \quad \frac{\partial F}{\partial x} <, > 0$$

Free surface reconstruction

2.2 Numerical implementation Solving procedure (two step projection method, Chorin 1968)

 $\frac{u_i^{n+1} - u_i^n}{\Delta t} + u_j^n \frac{\partial u_j^n}{\partial x_j} = -\frac{1}{\rho^n} \frac{\partial p^{n+1}}{\partial x_i} + g_i + \frac{\partial \tau_{ij}^n}{\partial x_j}, \qquad \frac{\partial u_i^{n+1}}{\partial x_i} = 0,$

Projection step

Pressure Poisson Equation (PPE)

Corrector step

 $\frac{u_i^{n+1} - \tilde{u}_i^n}{\Delta t} = -\frac{1}{\rho^n} \frac{\partial p^{n+1}}{\partial x_i}, \qquad \frac{\partial u_i^{n+1}}{\partial x_i} = 0,$ $\frac{\partial}{\partial x_i} \left(\frac{1}{\rho^n} \frac{\partial p^{n+1}}{\partial x_i} \right) = \frac{1}{\Delta t} \frac{\partial \tilde{u}_i^{n+1}}{\partial x_i},$

$$\frac{u_i^{n+1} - \widetilde{u_i}^{n+1}}{\Delta t} = -\frac{1}{\rho^n} \frac{\partial p^{n+1}}{\partial x_i}$$

2.3 Wave boundary condition

- Introduction
- Methods
- Wave absorption

2.4 Mesh generator: CORAL

2.3 Wave boundary condition Introduction

- Numerical simulations of nearshore hydrodynamics are carried out for a computational domain that is usually limited by fictitious boundaries.
- Boundary conditions need to be specified along these open boundaries in order to simulate the effect induced on hydrodynamics inside the computational domain by processes occurring outside
- The boundary condition suited for nearshore simulations should generate the incoming wave motion and absorb the outgoing waves. It is thus referred to as absorbing-generating boundary condition.

2.3 Wave boundary condition Introduction

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- Wave generation is the key factor for a coastal engineering model.
- Currently IH-2VOF supports 2 methods.
 - Dirichlet boundary condition
 - Moving boundary method

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2.3 Wave boundary condition Methods

Dirichlet Boundary Condition

- The numerical study of wave motion in the nearshore requires a wave generation algorithm able to reproduce the incoming wave conditions
- A convenient approach able to accurately reproduce incoming waves is based on imposing the theoretical free surface and the velocity field at the open boundary.
- VOF gets value 1 under free surface, 0 otherwise.
- Free surface and velocities for each cell in the first column are specified as input at a given sampling rate.
- Values are linearly interpolated as the simulation advances, and fixed in the boundary.

2.3 Wave boundary condition Methods

Dirichlet Boundary Condition

Theories implemented

- Regular waves:
 - First order
 - Second order
 - Fifth order (not in the GUI yet)
 - Cnoidal
 - Solitary

- Irregular waves:
 - First order
 - Second order (LH62 wave theory)

2.3 Wave boundary condition Methods

Moving Boundary Method

- This boundary condition replicates a piston type wave maker. It needs the paddle position as input.
- Velocity is then calculated as a first order forward derivative of position.
- The interaction of the paddle with the water makes use of openness coefficients and the virtual boundary forces.
- The moving wave maker appears as a source term in the momentum equation determined by the body surface velocity. $\theta_t^{n+1} = \alpha$

Wave Absorption Methods

The problem of wave absorption at the boundary in numerical models involves both incoming and outgoing waves.

Two main goals of wave absorption can be identified:

- 1. absorption of the reflected long waves which propagate toward the boundary
- 2. avoid of unrealistic total mass increase/decrese inside the computational domain.

An absorption routine is needed to achieve a significant improvement in the wave generation at the boundary

Wave Absorption Methods

- Wave absorption allows simulations.
 - Smaller domains.
 - Longer runtime before increasing agitation.
- Perfect absorption is idealistic: results up to 10% reflection are very good.
- Currently 2 supported methods
 - Active wave absorption
 - Passive wave absorption: Sponge layer

Wave Absorption Methods

- Active wave maker absorption is also included in the model using the same procedure followed in physical flumes. Theory has developed in: Review of Multidirectional Active Wave Absorption Methods (Schäffer & Klopman, 2000)
- The system absorbs depending on an input value: water level at the boundary.
- It is based on linear long wave theory: it has proven to work fine for waves outside this assumption.

$$U \cdot h = c \cdot \eta$$
 $c = \sqrt{g \cdot h}$ $U = -\sqrt{rac{g}{h}} \eta_c$

 $\eta_c = \eta_{\text{measured}} - \eta_{\text{theoretical}}$

Experimental set-up

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 $\Delta x = \Delta y = 0.01 \text{ m}$

- It ensures better stability for long simulations
 - It prevents the rise of water level due to the unbalance between wave crest-trough.
 - It allows a great percentage of reflected energy to flow out, avoiding its unbounded increase within the domain.
 - It does not noticeably increase the computational cost.
- Preferred among dissipation zones
 - They increase the domain in around 2 wave lengths.
 - They tend to increase the mean level due to the added friction.

Conclusions

The simultaneous wave generation and absorption problem is of great importance for a detailed study of wave transformation on coastal waters.

The challenge is in specifying incident waves through an inflow boundary with the presence of offshore wave radiation.

Different algorithms are implemented in the IH-2VOF model in order to achieve a high accuracy of the generation and the absorption routines

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