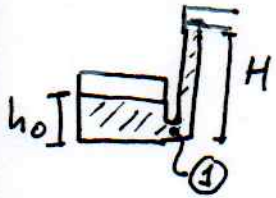


P1) a) $P_{min} \Rightarrow$ El fluido llega a H e/ $v_s = 0$,



$$P_s = P_c + \rho g h_0 \quad \rightarrow \quad P_c = P_0 + \rho g (H - h_0)$$

$$P_s = P_0 + \rho g H$$

$$P_{min} = 158,465 \text{ kPa}$$

b) e/ $P_c > P_{min} \Rightarrow v_s \neq 0$. $P_c = 220 \text{ kPa} > P_{min}$ ✓

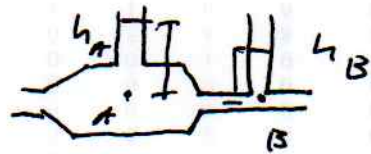
$$P_c + \rho g h_0 + \frac{1}{2} \rho v_c^2 = P_0 + \rho g H + \frac{1}{2} \rho v_s^2$$

$\Delta h_0 \approx cte$

$$v_s = \sqrt{\frac{2}{\rho} (P_c - P_{min})} \Rightarrow v_s = 11,42 \text{ m/s}$$

$$Q = v_s \cdot \frac{\pi d_B^2}{4} \Rightarrow Q = 7,86 \times 10^{-3} \text{ m}^3/\text{s}$$

c) En presencia de fluido:



$$P_A + \frac{1}{2} \rho v_A^2 = P_B + \frac{1}{2} \rho v_B^2$$

$$v_B = v_s \quad v_s \cdot d_B^2 = v_A \cdot d_A^2 \Rightarrow v_A = \left(\frac{d_B}{d_A}\right)^2 \cdot v_s$$

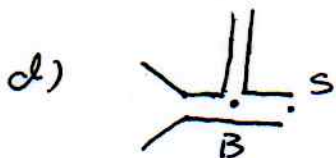
$$P_A - P_B = \frac{1}{2} \rho v_s^2 \left[1 - \left(\frac{d_B}{d_A}\right)^4\right]$$

$$P_A = P_0 + \rho g h_A \quad > \quad P_A - P_B = \rho g \underbrace{(h_A - h_B)}_{\Delta h} \Rightarrow \Delta h = \frac{v_s^2}{2g} \left[1 - \left(\frac{d_B}{d_A}\right)^4\right]$$

$$P_B = P_0 + \rho g h_B$$

$$\Delta h = 5,49 \text{ m} > 0 \Rightarrow h_A > h_B \text{ . Correcto : } -v_A < v_B$$

¶ $d_A > d_B$ y $P_A > P_B$ por el T. Bernoulli.



$$P_B + \frac{1}{2} \rho v_B^2 = P_0 + \frac{1}{2} \rho v_s^2 \Rightarrow P_B = P_0$$

$$\Rightarrow h_B = 0$$

P2

$n = 10$, diatómico \Rightarrow g.l. = 5

$c_v = \frac{5}{2} R$

2/6

$c_p = \frac{7}{2} R$

$\gamma = c_p / c_v = \frac{7}{5} = 1,4$

a)	P (kPa)	V ($\times 10^{-3} m^3$)	T (K)
A	540	249	4528,2
B	204,07	479	4476,3
C	405	931	4476,3
D	405	249	314

$T_A = \frac{P_A V_A}{nR}$

A-B - Adiabático

$P_A V_A^\gamma = P_B V_B^\gamma$

$P_B = P_A \left(\frac{V_A}{V_B} \right)^\gamma$

$T_B = \frac{P_B V_B}{nR}$

$T_C = T_B$

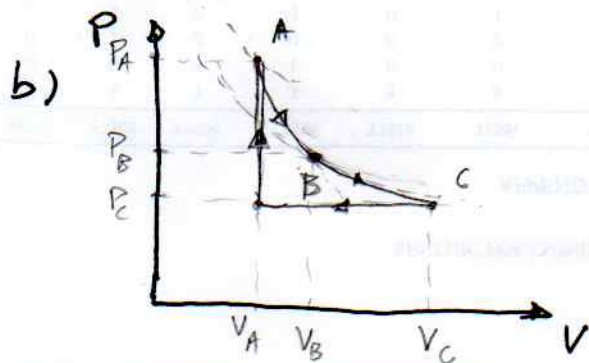
B-C - Isotérmico

$P_B V_B = P_C V_C \Rightarrow V_C = \left(\frac{P_B}{P_C} \right) V_B$

C-D - Isóbaro

$P_D = P_C$

$T_D = \frac{P_D V_D}{nR}$



d) Ciclo horario \Rightarrow M.T.

$|W_{A \rightarrow C}| > |W_{C \rightarrow B}|$

$W_{A \rightarrow C} < 0 ; W_{C \rightarrow B} > 0$

$\Rightarrow W_{neto} < 0 !$

c)

	Q (kJ)	W (kJ)	(kJ) ΔU
A-B	0	-73,1	-73,1
B-C	65,0	-65,0	0
C-D	-250,6	71,6	-179,0
D-A	252,1	0	252,1

$\Delta U = Q + W$

A-B: Adiabático ; $Q_{AB} = 0$

$$W_{AB} = \Delta U_{AB} = n C_V (T_B - T_A) = -73,1 \text{ kJ}$$

B-C: Isotérmico

$$\Delta U_{BC} = 0$$

$$W_{BC} = -n R T_B \ln\left(\frac{V_C}{V_B}\right) = -65 \text{ kJ}$$

$$Q_{BC} = -W_{BC}$$

C-D: Isobárico ;

$$Q_{CD} = n C_P (T_D - T_C) = -250,6 \text{ kJ}$$

$$W_{CD} = -P_C (V_D - V_C) = 71,6 \text{ kJ}$$

$$\Delta U_{CD} = Q_{CD} + W_{CD} = n C_V (T_D - T_C) = -179,0 \text{ kJ}$$

D-A: Isocórico ;

$$Q_{DA} = n C_V (T_A - T_D) = 252,1 \text{ kJ}$$

$$W_{DA} = 0 \quad \Delta U_{DA} = Q_{DA}$$

d) ciclo: el queo q/ $\Delta U_{AB} + \Delta U_{BC} + \Delta U_{CD} + \Delta U_{DA} = 0 \checkmark$

$$W_{\text{Neto}} = W_{AB} + W_{BC} + W_{CD} = -66,45 \text{ kJ } 20 \text{ } \underline{\underline{U.T.}}$$

$$e) \text{ Eficiencia : } \gamma = \frac{W}{Q_H} = 1 - \frac{Q_L}{Q_H}$$

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$$Q_L = Q_{CD} < 0$$

$$Q_H = Q_{BC} + Q_{DA} > 0$$

$$\Rightarrow \boxed{\gamma = 0,21}$$

Mag. de Carnot :

$$T_L = 314 \text{ K}$$

$$T_H = 1528,2 \text{ K}$$

Extremos del ciclo

$$\gamma_c = 1 - \frac{T_L}{T_H}$$

$$\Rightarrow \boxed{\gamma_c = 0,79}$$

Esta es la máxima eficiencia del ciclo

$$f) \Delta S_U = \cancel{\Delta S_{\text{ciclo}}} + \Delta S_H + \Delta S_L$$

ciclo

$$\Delta S_H = - \frac{(Q_{BC} + Q_{DA})}{T_A} = -207,5 \text{ J/K}$$

$$\Delta S_L = - \frac{(Q_{CD})}{T_D} = 796,6 \text{ J/K}$$

$$\boxed{\Delta S_U = 589,1 \text{ J/K} > 0}$$

P3 I.a) $Y_R(x,t) = A \left\{ \underset{\substack{\downarrow \\ \text{sentido } x > 0}}{\cos(kx - \omega t + \delta)} - \underset{\substack{\downarrow \\ \text{Inv. de } \\ \text{fase en la} \\ \text{reflexión.}}}{\cos(kx + \omega t + \delta)} \right\}$ $x < 0$

En el argumento de los cosenos,

$a = kx + \delta$ y uso la fórmula de suma
 $b = \omega t$

$$Y_R = A \left\{ \cancel{\cos(kx + \delta)} \cos \omega t + \cancel{\sin(kx + \delta)} \sin \omega t \right. \\ \left. - \cos(kx + \delta) \cos \omega t + \sin(kx + \delta) \sin \omega t \right\}$$

$$Y_R = 2A \sin(kx + \delta) \sin \omega t$$

No tiene la forma $f(x-vt)$,

sino que $f(x) \cdot g(t) \Rightarrow$ Onda Estacionaria.

I.b) Para $\forall t$ $Y_R(x) \propto 2A \sin(kx + \delta)$

P/ $x=0$ $Y(0)=0 \Rightarrow Y(0) = 2A \sin \delta = 0 \Rightarrow \boxed{\delta=0}$

$x=L$ $Y(L)=0 \Rightarrow Y(L) = 2A \sin(kL) = 0$

$kL = m \cdot \pi$; $m = 1, 2, 3, \dots$

$\frac{2\pi}{\lambda_m} L = m \pi \Rightarrow \boxed{\lambda_m = \frac{2L}{m}}$

$v = \lambda_m \nu \Rightarrow \sqrt{\frac{T}{\mu}} = \frac{2L}{m} \cdot \nu$

$\nu = \sqrt{\frac{T}{\mu}}$

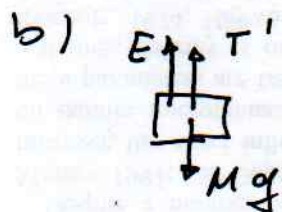
$$\boxed{\nu_m = \frac{m}{2L} \sqrt{\frac{T}{\mu}}}$$

$$\text{II. a)} \quad v = 140 \text{ Hz} \quad T = Mg$$

6/6

$$m = 2$$

$$v = \frac{1}{L} \sqrt{\frac{Mg}{\mu}} \Rightarrow M = \frac{\mu}{g} (Lv)^2 \Rightarrow \boxed{M = 900 \text{ g}}$$



$$T' + E = Mg \Rightarrow T' = Mg - E$$

$$E = \rho \cdot V_s \cdot g$$

$$T' \Rightarrow v = 140 \text{ Hz} \quad \text{y} \quad m = 3$$

$$v = \frac{L}{2L} \sqrt{\frac{Mg}{\mu}} \Leftrightarrow v = \frac{3}{2L} \sqrt{\frac{T'}{\mu}}$$

$$\frac{3}{2} \sqrt{\frac{T'}{\mu}} = \sqrt{\frac{Mg}{\mu}} \Rightarrow \boxed{T' = \frac{4}{9} Mg}$$

$$\rho V_s g = Mg - T' = Mg - \frac{4}{9} Mg = \frac{5}{9} Mg$$

$$\rho V_s = \frac{5}{9} M \Rightarrow V_s = \frac{5}{9} \frac{M}{\rho} \Rightarrow \boxed{V_s = 0,5 \text{ lt}}$$

$$\frac{V_s}{V_0} = 0,5 = 50\%$$

c) Para aumentar v manteniendo el mismo modo 'm' es preciso aumentar la tensión, por lo tanto reducir el empuje, por lo tanto $\rho_{\text{agua}} < \rho_{\text{masa}}$.