

EX. 18/12/2014

PROB 1:

$$A = 0,0075 \text{ m}^2 \quad a = \frac{A}{10}$$

$$H = 2,0 \text{ m}$$

PARTE A: VÁLVULA CERRADA

$$V_0 = 7,5 \text{ l} = 7,5 \times 10^{-3} \text{ m}^3 \quad z_0 = 1,0 \text{ m}$$

$$P_2 = P_1 + \rho g z_0 + \frac{Mg}{A} = P_{\text{máx}} \quad / \quad P_1 = P_0$$

$$M = \frac{(P_{\text{máx}} - P_0) A}{g} - \rho V_0 = 69 \text{ Kg}$$

PARTE B:

$$P_0 + \frac{Mg}{A} + \rho \frac{v_1^2}{2} + \rho g z = P_0 + \rho g H + \rho \frac{v_3^2}{2}$$

$$v_1 A = v_3 a \quad v_3 = v_1 \frac{A}{a}$$

$$\frac{\rho}{2} v_1^2 \left(1 - \frac{A^2}{a^2}\right) = \rho g (H - z) - \frac{Mg}{A}$$

$$i) \quad v_1^2 = \frac{2}{\rho} \left[ \frac{Mg}{A} - \rho g (H - z) \right] \left( \frac{A^2}{a^2} - 1 \right)^{-1}$$

$$ii) \quad v_1 = 0 \rightarrow M = \rho A (H - z) \quad / \quad z = \frac{(V_0 - V)}{A} = 0,4 \text{ m}$$

$$M = 12 \text{ Kg}$$

$$V = 4,5 \text{ l}$$

PARTE C:

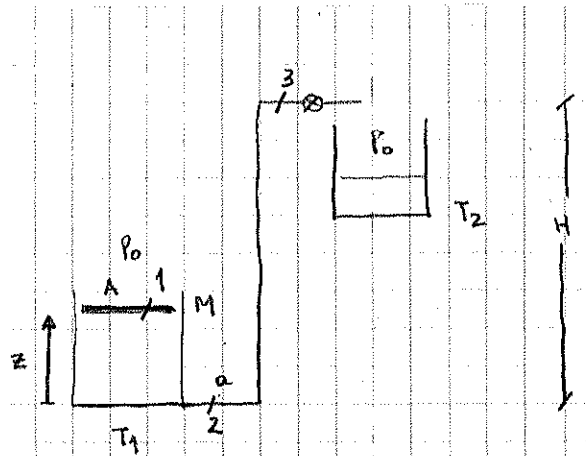
$$V_B = 3 \text{ l} \quad z_B = 0,4 \text{ m} \quad m_A = 3 \text{ Kg}$$

$$F_B = (M z_B + m_A z_B / 2) g$$

$$F_C = m_A H g + m_A \frac{v_3^2}{2}$$

$$\Delta E (\text{mJ}) = m_A (H - z_B / 2) g - M z_B g = 5,88 \text{ J}$$

$$\begin{matrix} v_3 = 0 \\ v_1 = 0 \end{matrix} \left. \vphantom{\begin{matrix} v_3 = 0 \\ v_1 = 0 \end{matrix}} \right\} \text{ PROCESO CUASIESTÁTICO}$$



PROB 2. PARTE A

$$y_1(x,t) = y_0 \sin(k_1 x - \omega_1 t)$$

$$y_2(x,t) = y_0 \sin(k_2 x - \omega_2 t)$$

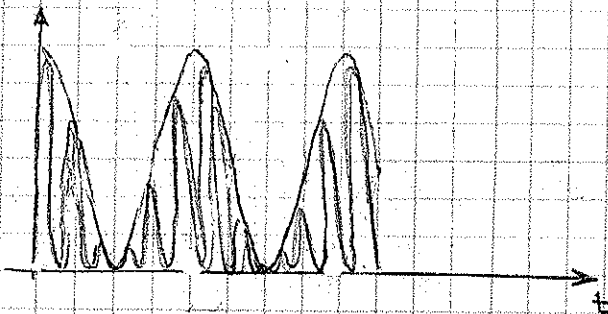
$$\sin \alpha + \sin \beta = 2 \sin \left( \frac{\alpha + \beta}{2} \right) \cos \left( \frac{\alpha - \beta}{2} \right)$$

$$y_T(x,t) = 2y_0 \sin(k_A x - \omega_A t) \cos(k_B x - \omega_B t)$$

$$k_A = \frac{k_1 + k_2}{2} \quad \omega_A = \frac{\omega_1 + \omega_2}{2} \quad k_B = \frac{k_1 - k_2}{2} \quad \omega_B = \frac{\omega_1 - \omega_2}{2}$$

$$I \propto y_T^2 = 4y_0^2 \sin^2(k_A x - \omega_A t) \cos^2(k_B x - \omega_B t)$$

$$I(x=0,t) \propto 4y_0^2 \sin^2(\omega_A t) \cos^2(\omega_B t) \quad / \quad \tau_A = \frac{2\pi}{\omega_A} \ll \frac{2\pi}{\omega_B} = \tau_B$$



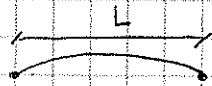
— Envelope:  $4y_0^2 \cos^2 \omega_B t$   
 — Función:  $\sin^2 \omega_A t$

$$\cos^2 \alpha = \frac{1}{2} (1 + \cos 2\alpha)$$

$$\omega_B = \frac{\omega_1 - \omega_2}{2} \quad 2\omega_B = \omega_1 - \omega_2$$

$$\omega_{\text{BATIDO}} = 2\omega_B$$

PARTE B



$$\sin kL = 0 \rightarrow kL = n\pi \rightarrow k = \frac{n\pi}{L}$$

$$k_1 = \frac{\pi}{0,49} = 6,41 \text{ m}^{-1}$$

$$v = \frac{\omega_0}{k_1} = \frac{2\pi f_0}{k_1} = 425 \text{ m/s} = \sqrt{\frac{\tau}{\mu}}$$

$$\mu = 3,6 \text{ g/m}$$

EFFECTO DOPPLER

$$f_0 = \frac{f_R}{(1 - v_R/v_s)}$$

$$f_0 = \frac{430}{1 - \frac{3}{343}} = 434 \text{ Hz}$$

PARTE C

Por la parte A:  $f_{\text{BAT}} = f_0 - f_0' = \frac{1}{\tau_{\text{BAT}}} \rightarrow f_0 = f_0' \pm \frac{1}{\tau_{\text{BAT}}} = \begin{cases} 424 \text{ Hz} \\ 444 \text{ Hz} \end{cases}$

$$f_0' = \frac{\omega_0}{2\pi} = \frac{v_s k_{1F}}{2\pi} \rightarrow k_{1F} = \frac{2\pi f_0'}{v_s} = \frac{\pi}{L_F} \rightarrow L_F = \frac{v_s}{2f_0'} = \begin{cases} 40,4 \text{ cm} \\ 38,6 \text{ cm} \end{cases}$$

PROB 3.

$$\frac{P_B}{P_A} = 12 = \frac{P_C}{P_D}$$

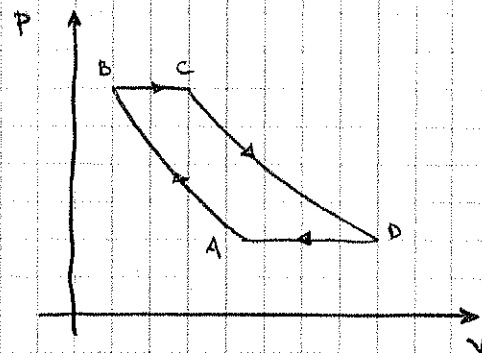
$$T_C = 1250 \text{ K}$$

$$T_A = 300 \text{ K}$$

$$P V^\gamma = \text{cte} \quad \gamma = 7/5 \quad \text{AIRE}$$

$$P_C V_C^\gamma = P_D V_D^\gamma \rightarrow \frac{V_D}{V_C} = 12^{5/4}$$

$$P_A V_A^\gamma = P_B V_B^\gamma \rightarrow \frac{V_A}{V_B} = 12^{5/4}$$



$$nR = \frac{P_A V_A}{T_A} = \frac{P_B V_B}{T_B} \rightarrow T_B = \frac{P_B}{P_A} \frac{V_B}{V_A} T_A = \frac{12}{12^{5/4}} T_A = 12^{2/4} T_A = 610 \text{ K}$$

$$nR = \frac{P_D V_D}{T_D} = \frac{P_C V_C}{T_C} \rightarrow T_D = \frac{1}{12^{5/4}} T_C = 614,6 \text{ K}$$

$$\textcircled{A} \quad Q = n c_p (T_A - T_D) + n c_p (T_C - T_B) = 9,46 \text{ KJ}$$

$$\Delta U = W + Q = 0$$

$$W = -Q = 9,46 \text{ KJ}$$

$$n = 1 \text{ mol}$$

$$R = 8,3145 \text{ J/mol K}$$

$$c_p = \frac{7}{2} R$$

$$\textcircled{B} \quad \eta = \frac{W}{Q_H} = \frac{9,46 \text{ KJ}}{c_p (T_C - T_B)} = 50,8\%$$

$$\textcircled{C} \quad \Delta S_u = \Delta S_{\text{ciclo}} + \Delta S_H + \Delta S_L$$

$$\Delta S_u = -\frac{Q_H}{T_H} + \frac{Q_L}{T_L} = -14,9 + 30,5$$

$$\Delta S_{\text{ciclo}} = 0$$

$$\Delta S_u = 15,6 \text{ J/K}$$

