

Ej 1: $P_A = 100 \text{ kPa}$
 $V_A = 2 \times 10^{-3} \text{ m}^3$
 $T_A = 200 \text{ K}$

$$\frac{P_A V_A}{T_A} = nR = 1,5 \frac{(\text{kPa})(\text{l})}{\text{K}}$$

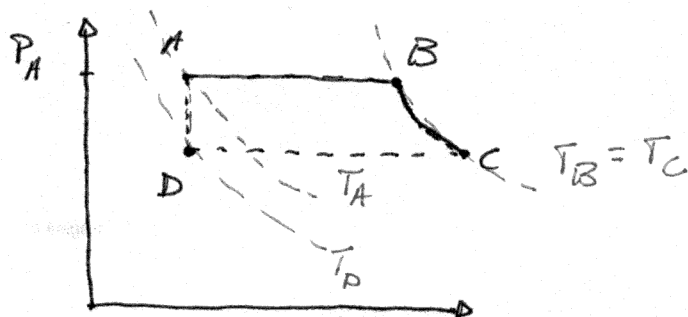
$T_B = 60 \text{ K}$, $P_C = 120 \text{ kPa}$

a) Proceso A-B, C-D a Pcte

BC, T = cte

DA $\Rightarrow P = \alpha T$ $\alpha = \frac{nR}{V} = \text{cte}$

DA $\rightarrow V$ cte !



A-B $\Rightarrow \frac{V_A}{T_A} = \frac{V_B}{T_B} \Rightarrow V_B = 3V_A = 6 \text{ l}$

B-C $\Rightarrow P_B V_B = P_C V_C \Rightarrow V_C = 1,25 V_B = 3,75 V_A = 7,5 \text{ l}$

C-D $\Rightarrow \frac{V_C}{T_C} = \frac{V_D}{T_A} \Rightarrow V_D = \frac{T_A}{T_C} V_C \Rightarrow V_D = V_A$

D-A $\Rightarrow \frac{P_D}{T_D} = \frac{P_A}{T_A} \Rightarrow T_D = \frac{P_D}{P_A} T_A \Rightarrow T_D = 0,8 T_A = 160 \text{ K}$

b) Ciclo horario $\Rightarrow W < 0 \Rightarrow$ Maq. Térmica

$\eta = 1 - \frac{Q_L}{Q_H}$ $Q_L = \sum_{<0} Q_i$; $Q_H = \sum_{>0} Q_i$

$Q_{AB} = n C_p (T_B - T_A) = 2400 \text{ J}$

$Q_{BC} = -W = \int_{V_B}^{V_C} P dV = nR T_B \ln \frac{V_C}{V_B} \Rightarrow Q_{BC} = 200 \text{ J}$

$Q_{CD} = n C_p (T_D - T_C) \Rightarrow Q_{CD} = -2340$

DA: $Q_{DA} = n C_v (T_A - T_D) = 150 \text{ J}$

$|Q_L| = 2340$

$|Q_H| = 2450$

$\eta = 5,7\%$

$$\eta_c = 1 - \frac{T_L}{T_H} = 1 - \frac{160}{600} \Rightarrow \boxed{\eta_c = 73,3\%}$$

2/3

Ej 2: $v = \lambda f$ $v = \sqrt{\frac{F}{\mu}}$ $F = F_0 + \beta(L - L_0)$
 (cuerda)

a) $\Delta L = \alpha L_0 (T - T_0)$ (barra) ; $\Delta L = L - L_0$

Si $T = 20^\circ\text{C} \Rightarrow L = L_0 = 4\text{ m}$, y $\lambda_n = \frac{2L}{n}$

$n = 1$, (modo fundamental) $f_n = \frac{n}{2L} \sqrt{\frac{F}{\mu}}$;

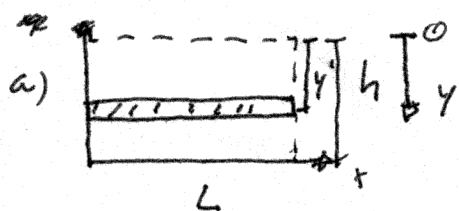
$f_0 = \frac{1}{2L_0} \sqrt{\frac{F_0}{\mu}} \Rightarrow \boxed{F_0 = \mu(2L_0 f_0)^2} \Rightarrow \boxed{F_0 = 929,3\text{ N}}$

b) $\Delta L = \alpha L_0 (T - T_0) \Rightarrow \Delta L = 6 \times 10^{-2}\text{ m}$
 $T = 80$ $L_0 = 4$
 $T_0 = 20$ $\alpha = 50^{-3}$

$L' = L_0 + \Delta L \Rightarrow f_2 = \frac{2}{2L'} \sqrt{\frac{F'}{\mu}}$

$F' = F_0 + \beta \Delta L \Rightarrow F' = 1019,3 \Rightarrow \boxed{f_2 = 869,5\text{ Hz}}$

Ej 3: Fuerza hidrostática sobre una pared vertical.



$$F_{hid} = \int P(y) dA = L \int_0^h P_0(y') dy'$$

$P(y') = P_0 + \rho g y' \Rightarrow \boxed{F_{hid} = L P_0 h + \rho g L \frac{h^2}{2}}$ *

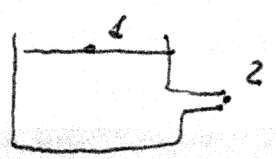
b) Como la atmósfera está tb del otro lado del tapón,
 $F_{fic} = (P_0 - P(h')) \cdot A_{tapón}$; $A_{tapón} = \frac{\pi d^2}{4}$; $d = 4\text{ cm}$
 $h' = 6\text{ m}$

$F_{fic} = \rho g h' \frac{\pi d^2}{4} \Rightarrow \boxed{F_{fic} = 73,8\text{ N}}$

a) $\boxed{* F_{hid} = 52,35 \times 10^6\text{ N}}$

c) $\frac{\Delta m}{\Delta t} = \rho v_s A_{tap}$

$P_1 + \frac{1}{2} \rho v_1^2 + \rho g h' = P_2 + \frac{1}{2} \rho v_2^2$



$v_1 A_1 = v_2 A_2 \Rightarrow v_1 \ll A_2 \quad \rho g \quad A_1 \gg A_2 !$

$P_1 = P_2 = P_0$ $v_s = v_2 = \sqrt{2gh'} = 10,8 \text{ m/s}$

$\Delta t = \frac{\Delta m}{\rho A_{tap} \sqrt{2gh'}} \Rightarrow \Delta t = 73,4 \text{ seg}$

Ej 4: a) Expansión libre, recipiente adiabático
 $dW = 0$ $dQ = 0$

$\Rightarrow \Delta U = 0$; como es un gas ideal $T_1 = T_2 !$

$P_1 V_1 = P_2 V_2 \Rightarrow P_2 = \frac{P_1}{2}$; $P_1 = \frac{R T_1}{V_1} \Rightarrow P_1 = 2,43 \text{ MPa}$

$V_2 = 2V_1$ $P_2 = 1,215 \text{ MPa}$ (Proc. Irreversible)

b) Compresión adiabática reversible

$P_3 V_3^\gamma = P_2 V_2^\gamma \Rightarrow P_3 = P_2 \left(\frac{V_2}{V_3}\right)^\gamma = \frac{P_1}{2} 2^\gamma = P_1 2^{\gamma-1}$

$\gamma = \frac{C_p}{C_v} = \frac{5/2}{3/2} = \frac{5}{3} \Rightarrow P_3 = 4 \text{ MPa}$ $T_3 = \frac{P_3 V_3}{nR}$

$T_3 = 477,6 \text{ K}$

c) $W_{ad} = - \int_{V_3}^{V_2} P dV = - CTE \int V^{-\gamma} dV = - \frac{CTE}{1-\gamma} (V_3^{1-\gamma} - V_2^{1-\gamma})$

$W_{ad} = \frac{nR}{\gamma-1} (T_3 - T_2) \Rightarrow W_{ad} = 2243 \text{ J} > 0$

d) $\Delta S_u = \Delta S_{gas} + \Delta S_{rod}$

$\Delta S_{gas} = n C_v \ln\left(\frac{T_{amb}}{T_4}\right) + nR \ln\left(\frac{V_4}{V_1}\right) \Rightarrow \Delta S_{gas} = -0,035 \frac{\text{J}}{\text{K}}$

$\Delta S_r = -\frac{Q}{T_{amb}}$; $Q = n C_v (T_4 - T_3) \Rightarrow Q = -213 \text{ J}$

$\Delta S_r = 7,85 \text{ J/K} \Rightarrow \Delta S_u = 7,82 \text{ J/K}$