



Characterization of the intraday variability regime of solar irradiation of climatically distinct locations

Philippe Lauret^{a,*}, Richard Perez^b, Luis Mazorra Aguiar^c, Emeric Tapachès^a,
Hadja Maimouna Diagne^a, Mathieu David^a

^a *Laboratoire de Physique et Ingénierie Mathématique pour l'Energie et l'environnement (PIMENT), University of La Réunion, Campus du Moufia
15, Avenue René Cassin, 97715 Saint Denis Messag 9, France*

^b *ASRC, The University at Albany, SUNY, United States*

^c *University Institute for Intelligent Systems and Numerical Applications in Engineering, University of Las Palmas de Gran Canaria, Edificio Central
del Parque Tecnológico, Campus de Tafira, 35017 Las Palmas de Gran Canaria, Spain*

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Abstract

This paper investigates the relationship between two parameters characterizing a given location on a given day: the daily clear sky index KT^* and the intraday variability given by the standard deviation of the changes in the hourly clear sky index $\sigma(\Delta kt_{\Delta t}^*)$. Empirical evidence assembled from twenty climatically distinct locations led us to derive a simple model to infer intraday variability from the day's clear sky index. Although the model shows little dependence on location, we did observe a systematic difference traceable to a location's prevailing cloud formation regime. Therefore, we also propose two alternative models for sites where cloud formations is influenced by local orography and sites where cloud formation is traceable to weather events only. Finally, we present a possible application of the models to enhance the informative content of day(s) ahead NWP forecasts.

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1. Introduction

The characterization of solar resource variability is an important issue for grid-connected solar PV as penetration increases because of the challenges variability poses to grid operators (Perez and Hoff, 2013).

The topic of solar energy variability has generated a considerable amount of research during these last years. In particular, much attention has been paid to the study of the short-term variability of the PV power output of a

single plant due to the cloud fluctuations (Hansen, 2007; Marcos et al., 2011; Mills et al., 2010; Perpiñán et al., 2013; Van Haaren et al., 2014).

Some authors (Perez and Hoff, 2013; Lave et al., 2012; Sengupta and Keller, 2011; Murata et al., 2009) also showed that short-term power fluctuations generated by an ensemble of geographical dispersed PV plants are considerably reduced compared to a single one, and that the reduction can be predicted on the basis of power plant interdistance, cloud or cloud system motion and considered fluctuation time scale.

Metrics describing and quantifying variability at different time scales are a key ingredient of this characterization.

* Corresponding author. Tel.: +262 692 67 48 07; fax: +262 262 93 86 65.

E-mail address: philippe.lauret@univ-reunion.fr (P. Lauret).

Van Haaren et al. (2014) proposed a quantitative metric called the Daily Aggregate Ramp Rate (DARR) which sums 1-min single Plane Of Array (POA) irradiance sensor over each day to characterize daily variability in a utility-scale plant. Lenox and Nelson (2010) proposed the Inter-Hour Variability Score (IHVS) which summed the absolute value of 1-min changes in POA irradiance and AC power output in each hour. Badosa et al. (2013) showed that solar irradiance variability at the diurnal scale can be classified in regimes based on three parameters. These parameters are the daily clear-sky index, solar irradiance morning–afternoon asymmetry and random variability of the solar irradiance.

In a previous work, Perez et al. (2011) proposed models to characterize the one-minute intra-hourly solar variability based upon hourly inputs. Short-term variability metrics can be inferred by the model using hourly insolation data from e.g., satellite-based hourly products. The trends exhibited by the models were robust and showed little site dependency (Perez et al., 2011).

Here we address the issue of intraday variability with a variability time scale of one hour. For this purpose, the daily clear sky index is used as an input to infer the standard deviation of the changes in the hourly clear sky index over the considered day.

Previous studies (Stein et al., 2012; Kang and Tam, 2013) have demonstrated that it is possible to model intraday variability from ground-based solar radiation daily time series.

Stein et al. (2012) introduced a new metric: the variability index, VI, to quantify irradiance variability over various timescales. Three sites were used to evaluate the consistency of this new metric. By pairing the VI index with the daily clear sky index, KT^* , they showed that a characteristic scatter plot named the “arrow-head” plot emerged from the data at hand. A classification scheme based on the VI index and clear sky index was used to distinguish between four types of irradiance days.

In a similar manner, Kang and Tam (2013) proposed a new characterization and classification method (the K-POP method) for daily sky conditions by using the daily clearness index K_D and a new metric called the daily probability of persistence (POP_D). POP_D observes differences between neighboring instantaneous clearness indices and calculates a probability that the differences are equal to zero (Kang and Tam, 2013). Three sites were chosen to test the consistency of the method. The authors showed that the annual distribution of data points in the K- POP_D plane for all three locations were enclosed by the same irregular nonagon. From the K- POP_D plane the authors also identified 10 classes that correspond to different sky conditions.

In his thesis, Dambreville (2014) proposed a classification scheme based on the daily mean clear sky index and daily variability quantified by the V metric (Coimbra et al., 2013). The classification was used to characterize the sky conditions experienced by a site located near Paris.

Some authors (Huang et al., 2014; Kang and Tam, 2015) also went further by deriving some prediction models of daily variability. For instance, Huang et al. (2014) studied the daily variability at four sites across Australia by using the Daily Variability Index (DVI) – which is similar to the VI (Stein et al., 2012). In addition to the persistence model, they also built three statistical models (including a machine learning technique) to predict the DVI using meteorological variables as predictors. The latter were selected from the global atmospheric reanalysis product of the European Centre for Medium-Range Weather Forecasts (ECMWF). However, as noted by the authors in their conclusion, the probability density function (PDF) of the DVI was not well reproduced by the statistical techniques and may suggest a limitation of these techniques in tackling the solar variability problem.

Kang and Tam (2015) used the National Weather Service (NWS) day-ahead total sky cover forecast to predict the day-ahead K_D and POP_D values. A multi-stage procedure (including a robust regression technique) was employed to estimate the parameters of a linear equation relating the daily fluctuation of solar irradiance (POP_D) to the daily fluctuation of total sky cover. The forecasting method was tested on one year of data from the Solar Radiation Research Laboratory Baseline Measurement System (SRRL BMS). As noted by the authors, overall, the proposed method provides acceptable predictions results but further improvement is needed in the intermediate K_D zone that corresponds to the lowest POP_D values (or conversely to the highest variability values).

In this study, we make a step further by analyzing intraday solar variability of twenty sites that exhibit different types of climate. For this purpose, we select 14 climatically distinct regions of North America as well as 6 subtropical/tropical island territories.

First, we propose a simple site characterization based on 2 criteria: (1) the daily clear sky index is used as an input to define a given day’s meteorological conditions and (2) hourly intraday variability measured by a well-established metric – the standard deviation of the changes in the clear sky index (Perez and Hoff, 2013) – is used to quantify variability.

Second, based on a strong empirical evidence, we propose a parameterization of the intraday solar variability stating that intraday variability is a predictable function of daily clear sky index.

It must be stressed however that contrary to (Huang et al., 2014; Kang and Tam, 2015) our aim here is to propose a simple but yet effective and actionable approach.

Such a characterization would be helpful in an operational context. Predicted intraday variability enhances the informative content of day(s) ahead Numerical Weather Prediction (NWP) forecasts – operational forecasts such as ECMWF have a limited time resolution and tend to underestimate intraday dynamics. This information could be of particular relevance to grid operators’ decision

making, particularly in non-interconnected insular networks. For instance, a predicted high variability day may suggest an adaptation of the operational planning with ready deployment of stand-by generation capability.

2. Metrics, model derivation and data

The two quantities used in the proposed parameterization are the daily clear sky index KT^* (the variability predictor) and the intraday variability per se given by the standard deviation of the change in the clear sky index, over the considered day.

2.1. Daily clear sky index

The parameter used to characterize the daily solar conditions is the daily clear sky index (KT^*). The daily clear index KT^* is defined by:

$$KT^* = \frac{\sum_{i=1}^{N_h} GHI(i)}{\sum_{i=1}^{N_h} GHI_{clear}(i)} \quad (1)$$

where N_h represents the number of daylight hours (i.e. for which the solar zenith angle $SZA < 85^\circ$) in a day.

GHI is the hourly global horizontal irradiance and GHI_{clear} represents the clear sky global irradiance for the considered hour and can be obtained from (Bird and Hulstrom, 1981) or Ineichen, 2006). The Bird model (Bird and Hulstrom, 1981) was used for the six insular sites while the simplified SOLIS model (Ineichen, 2008) was used for the US locations, noting that the choice of model would have virtually no impact on the present observations.

2.2. Intraday variability

The intradaily variability is given by the standard deviation of the change in the clear sky index over the considered day i.e. $\sigma(\Delta kt_{\Delta t}^*)$. (Perez et al., 2015) called this metric the nominal variability. Nominal variability refers to the variability of the dimensionless clear sky index kt^* which is directly correlated with the ramp rates' magnitude.

Other metrics have been proposed to characterize the variability (e.g., Perez et al., 2011; Coimbra et al., 2013). However, most authors prefer using the nominal variability over a given time span as the metric for variability. We retain this definition of nominal variability:

$$Nominal\ Variability = \sigma(\Delta kt_{\Delta t}^*) = \sqrt{Var[\Delta kt_{\Delta t}^*]} \quad (2)$$

In this application, the time scale $\Delta t = 1$ h and the time span is N_h hours.

Let us also recall that the clear sky index kt^* is defined as the ratio of GHI to clear sky GHI.

We also provide two complementary metrics: the maximum absolute clear sky index change occurring within the day i.e. $\max(|\Delta kt_{\Delta t}^*|)$ and the median absolute deviation (MAD) of the $(\Delta kt_{\Delta t}^*)$ series for the considered day

i.e. $mad[\Delta kt_{\Delta t}^*]$. These two metrics enhance the information contained in $\sigma(\Delta kt_{\Delta t}^*)$. The first metric should be relevant for the grid operators as it quantifies an upper limit of the intraday variability while the second metric, contrary to the standard deviation, is less sensitive to extremes and/or outliers.

2.3. Model derivation and structure

As mentioned above, the objective of this paper is two-fold. First, it proposes a simple site characterization and second a model that parameterizes the intraday solar variability. Regarding the structure of the model, the known input to the model is the daily clear sky index. The unknown output of the model consists of the metric that estimates the site intraday variability $\sigma(\Delta kt_{\Delta t}^*)$.

The model is built empirically from hourly GHI ground measurements at several climatically distinct locations. The model consists of one lookup table defined by KT^* and returning the intradaily variability metric (the lookup table is given in section results).

2.4. Experimental data

Seven stations, part of NOAA's SURFRAD network (SURFRAD, 2010), seven stations from the NOAA's ISIS network (ISIS, 2010), and six insular sites are selected for the empirical analysis. Each station provides one year of GHI observations at hourly time scale. This leads to a total of 7110 days or 170,640 hourly measurements. The experimental data are further detailed in Table 1.

Two locations have been chosen for the islands of La Reunion (Saint-Pierre – coastal site and Le Tampon-inland site) and Gran Canaria (Las Palmas and Pozo Izquierdo).

In the case of La Réunion, the two aforementioned sites are quite representative of a tropical island with a complex orography. Hence, although distant of only 10 km, these two sites exhibit very different sky conditions (Diagne, 2015).

For Gran Canaria island, we chose two representative stations that take into account the climatic variability of the island (Mazorra Aguiar et al., 2010). Pozo Izquierdo is situated in the south of the Island and presents a large amount of clear days, while Las Palmas, northern station, is affected by clouds formation during summer due to the trade winds effect.

3. Results

3.1. Site characterization

The proposed parameterization scheme delineates a 2-dimensional space illustrated in Fig. 1 for the site of Sterling. It is clear from this illustration that intraday variability is a robust function of the daily clear sky index,

Table 1
Sites under study.

Station	Latitude	Longitude	Elevation (m)	Climate	Year
<i>Surfrad network</i>					
Goodwin Creek	34.25	−89.87	98	Subtropical	2013
Desert Rock	36.63	−116.02	1007	Arid	2013
Bondville	40.05	−88.37	213	Continental	2013
Boulder	40.13	−105.24	1689	Semi-arid	2013
Penn State	40.72	−77.93	376	Humid continental	2013
Sioux Falls	43.73	−96.62	473	Continental	2013
Fort Peck	48.31	−105.10	634	Continental	2013
<i>ISIS network</i>					
Sterling	38.95	−77.45	85	Humid continental	2013
Seattle	47.65	−122.25	20	Temperate maritime	2013
Salt Lake City	40.75	−111.95	1288	Semi-arid	2013
Madison	43.15	−89.35	271	Continental	2013
Handford	36.35	−119.65	73	Mediterranean	2013
Bismarck	46.75	−100.75	503	Continental	2013
Albuquerque	35.05	−106.65	18	Subtropical	2013
<i>Insular sites</i>					
Raizet (Guadeloupe)	16.264	−61.516	11	Tropical	2012
Oahu (Hawaii)	21.312	−158.084	11	Tropical	2011
Saint-Pierre (Réunion)	−21.340	55.491	75	Tropical	2012
Tampon (Réunion)	−21.269	55.506	550	Tropical	2013
Pozo Izquierdo (Gran canaria)	27.817	−15.424	47	Subtropical	2005
Las Palmas (Gran Canaria)	28.110	−15.426	17	Subtropical	2005

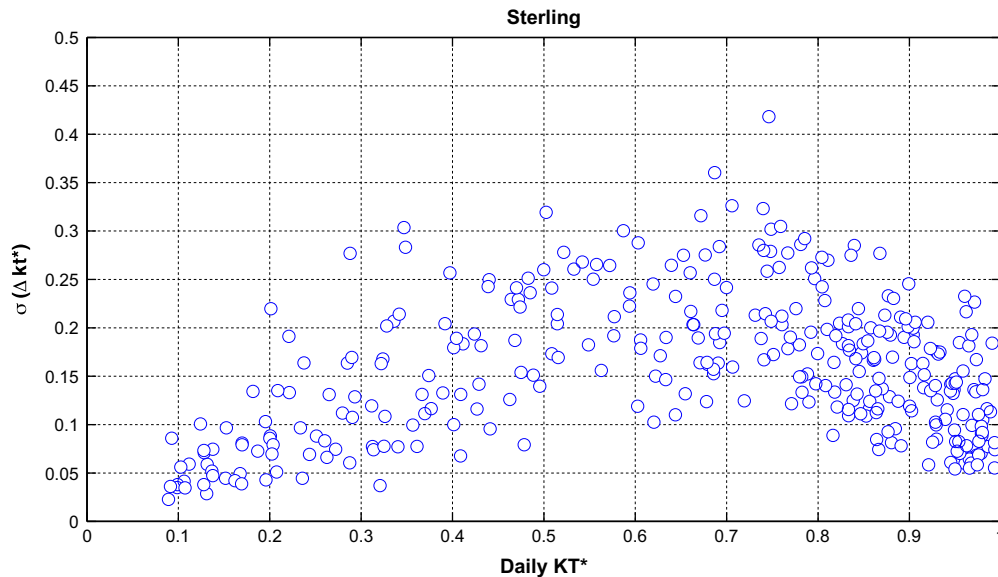


Fig. 1. Two-dimensional space $KT^* - \sigma(\Delta kt_{\Delta t}^*)$ – Sterling site.

ranging from little to no variability for dark overcast and very clear conditions to maximum variability for intermediate conditions. Remarkably, the trend illustrated for Sterling is very similar to the trends observed at all other locations as shown in Fig. 2. Although the distribution of occurrences in the 2-dimensional space varies from location to location depending on climate (e.g., compare Desert Rock and Sterling) the trends linking KT^* and $\sigma(\Delta kt_{\Delta t}^*)$ exhibit only a minor influence of the local climatic environment. These similarities as also noted by Stein et al. (2012)

have a physical basis due to the cloud-induced fluctuations processes. Indeed, in a very interesting article, Reno and Stein (2013) showed that the variability represented either by the VI index or the standard deviation of the clear sky index time series was dependent upon the cloud category.

The composite $\sigma(\Delta kt_{\Delta t}^*)$ vs. KT^* trend for all locations is shown in Fig. 3. The dark line represents the global mean trend calculated with data of all sites. This global mean trend was derived by taking the mean of the probability density of the variability for each bin of KT^* . This method

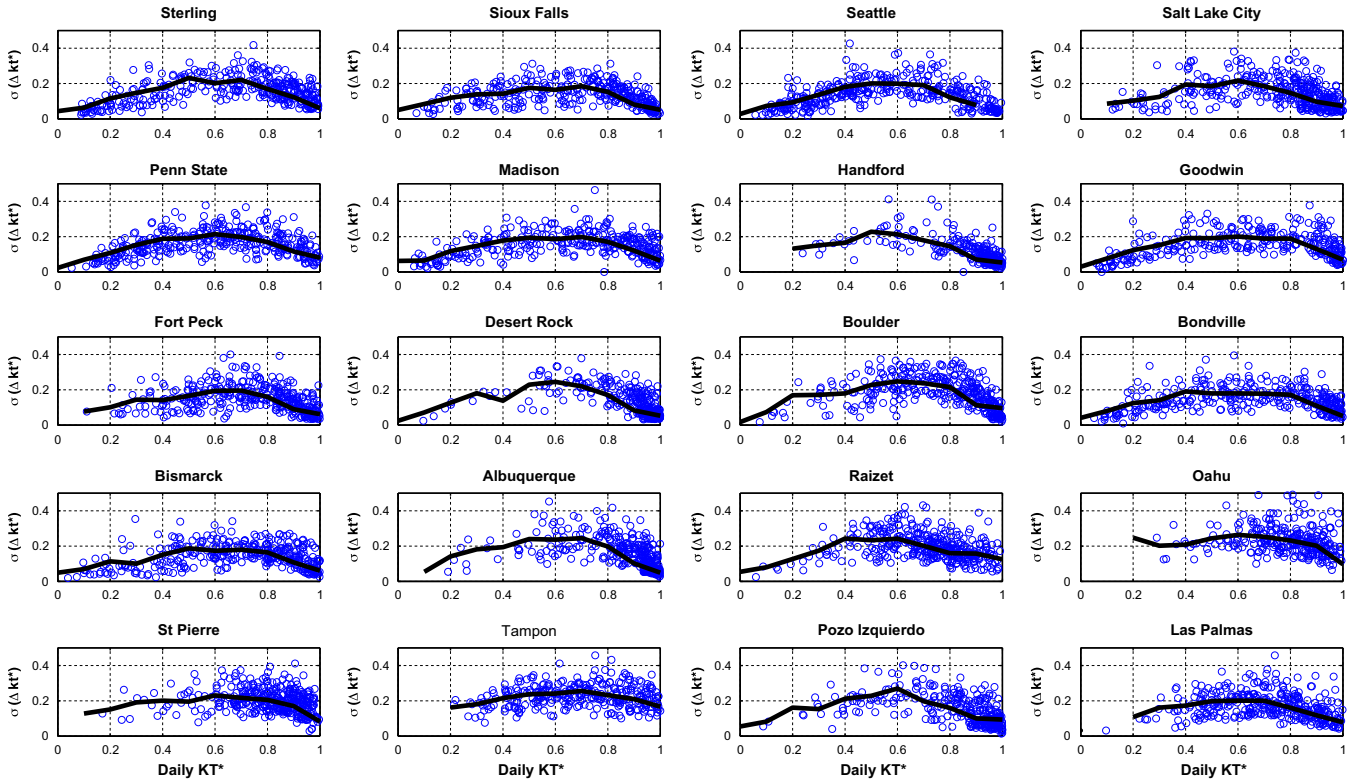


Fig. 2. Distribution of points in the plane $KT^*-\sigma(\Delta kt^*_M)$ for all sites. The black line represents the mean trend of each site.

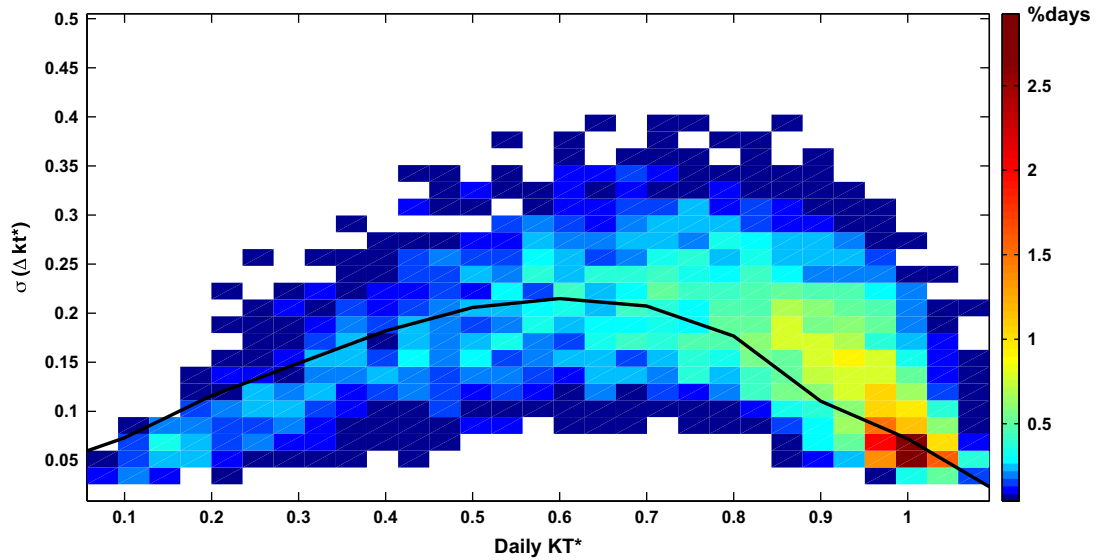


Fig. 3. Scatter density plot for all locations representing 7110 days. The black line represents the global mean trend.

was applied after checking that the distribution estimates were unimodal. This well-defined trend suggests that intra-daily variability can be conjectured from daily clear sky index.

In an attempt to explain the scattering of the data that appear in Figs. 1 and 2, similarly to (Huang et al., 2014),

we did investigate the correlation between intra-day variability and other meteorological variables provided by ECMWF such as Total Cloud Cover (TCC), Air Temperature (AT), 700 hPa Geopotential (GP700), 850 hPa Geopotential (GP850), Cloud Base Height (CBH), Zonal wind velocity (U), Meridional wind velocity (V). Apart

TCC, which behaves very much like the daily clear sky index (KT^*), none of these variables produced measurable correlations with the intra-day variability.

Individual site trends are intercompared in Fig. 4. Trends are comparable, but some differences are nevertheless apparent, with some locations systematically over the global trend and others systematically below the global trend. Fig. 5 present the trends obtained for the $\max(|\Delta kt_{\Delta t}^*|)$ metric.

Fig. 6 plots the average deviation between the global mean trend and each individual site's trend. This figure reveals that sites above the trend – Albuquerque, Boulder, both Reunion Island sites, Hawaii, Guadeloupe, and one of the Canary Islands site – tend to be sites where cloud

buildup is influenced by nearby orography. The sites below the trend are locations where cloud regimes are driven primarily by the passage of weather systems. The one exception is Las Palmas, however this site is on the windward side of the island and often experience a low level stable cloud layer more representative of the ocean mass ahead unlike the typical orography-driven cloud build-up characterizing partly cloudy events at the other sites.

Although the individual trends do not deviate substantially from the average trend, suggesting that the proposed parameterization is robust, Figs. 7 and 8 propose two separate trends for sites where cloud regimes are, and are not influenced by orographic build up, denoted respectively as type B and type A.

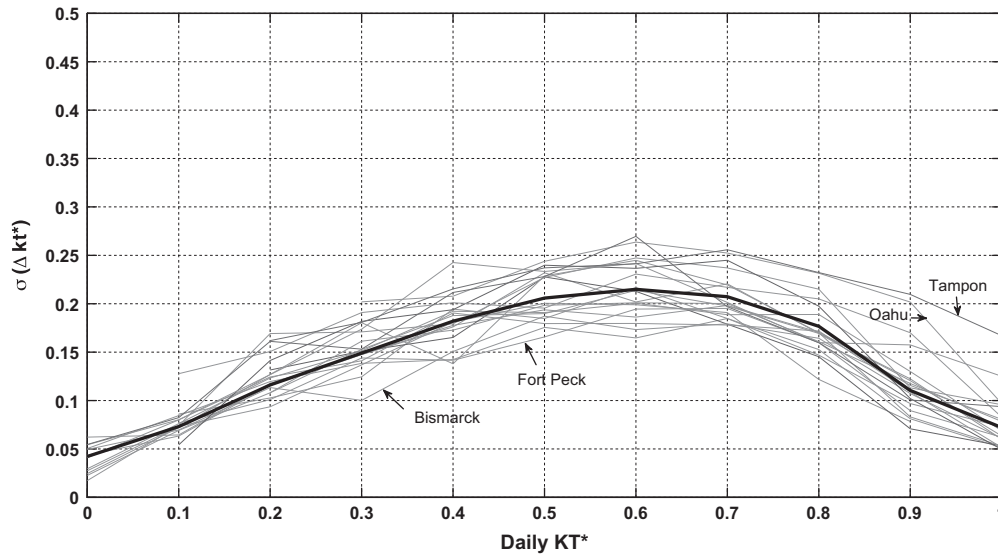


Fig. 4. Average trends of each site. The black line represents the global average trend.

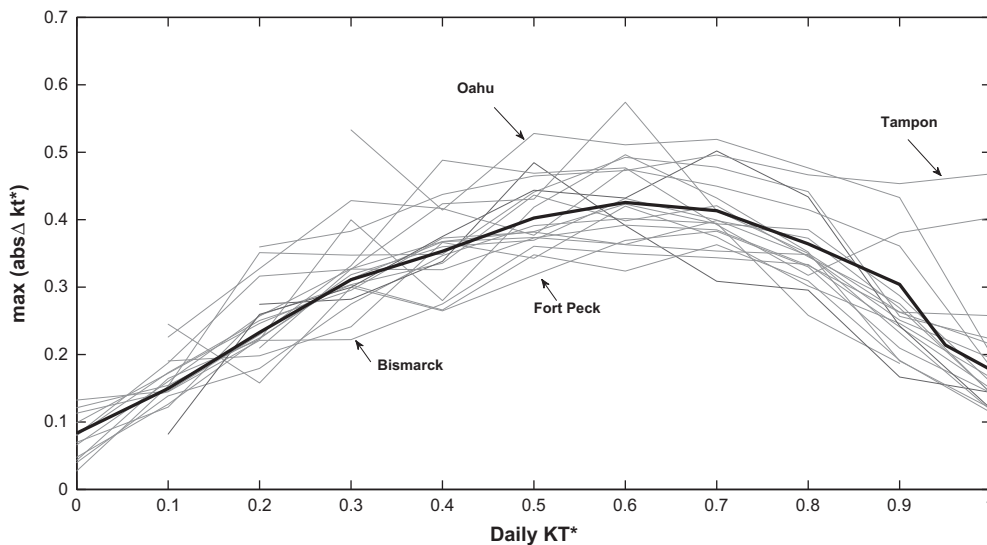


Fig. 5. Same as Fig. 4 but for the $\max(|\Delta kt_{\Delta t}^*|)$ metric.

Figs. 9 and 10 are analogous to Figs. 7 and 8, but present the trends calculated for the maximum clear sky index change metric i.e. $\max(|\Delta kt_{\Delta t}^*|)$.

3.2. Parameterization of intraday variability

The above observations led us to propose a simple model that quantifies intraday variability as a function of the daily clear sky index.

Although it would be possible to fit a continuous function (say for instance a polynomial of order 4) to the data, we propose here a modeling approach based on a look-up conversion table. Indeed, this technique has proven effective both in the case of solar irradiation transposition models (Perez et al., 1990) and solar irradiation fluctuations models (Perez et al., 2011). The Lookup table is given in Table 2. Table 2 reports the three intraday variability metrics derived for all observations falling in a particular KT*

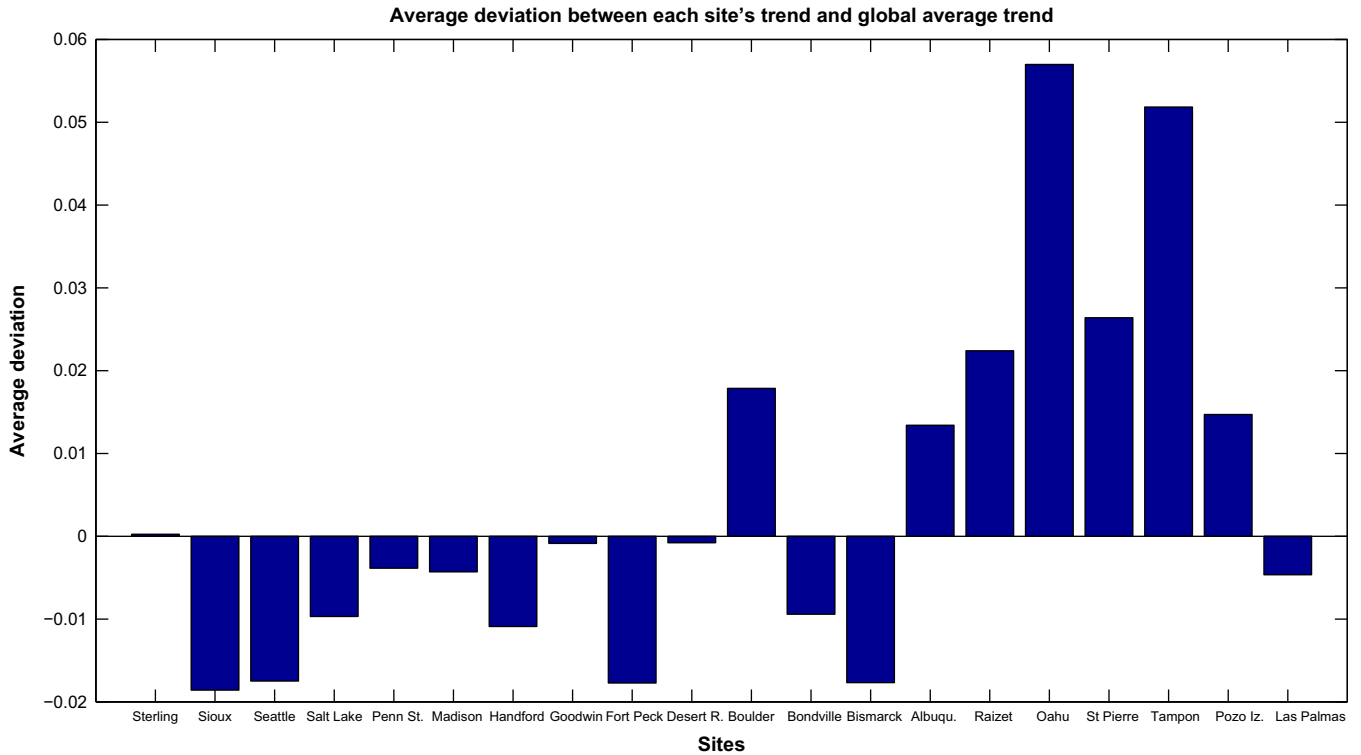


Fig. 6. Average deviation between each site's trend and global average trend.

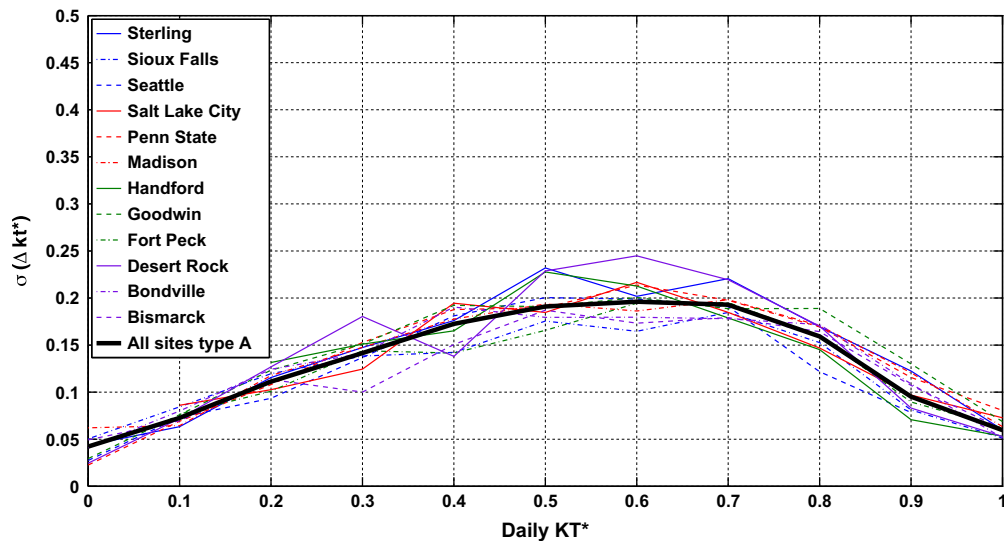


Fig. 7. Average trends for sites where cloud formation is traceable to weather events only. The black line represents the mean trend of the sites type A.

bin as well as the standard deviations around these means. The number of observations in each bin is also reported in Table 2. The number of observations should provide an indication of the robustness of any particular bin value. Tables 3 and 4 propose two complementary models for sites with cloud formations influenced by orography (type B) and sites where cloud formation is traceable to weather events only (type A).

3.3. Model application example: day-ahead forecasts paired with intradaily variability

Day ahead solar irradiance forecasting is essential for an efficient integration of large shares of solar energy into the

electricity grid. In addition to the day ahead forecasts, an information related to the expected intraday variability could be a great help for the grid operator in such a context of decision-making. Day ahead forecasts are produced by numerical weather prediction (NWP) models (e.g., ECMWF). Although these forecasts are increasingly accurate (Perez et al., 2013) especially in terms of daily KT^* prediction, they generally produce smoothed irradiance profiles and lack in hour to hour dynamics. Using the predicted KT^* , one could apply the proposed parameterization (Table 2) to estimate intraday variability.

Fig. 11 shows the intraday variability inferred from the ECMWF forecasts at the site of Saint-Pierre with two variants. The first case (Fig. 11a) plots the predicted intraday

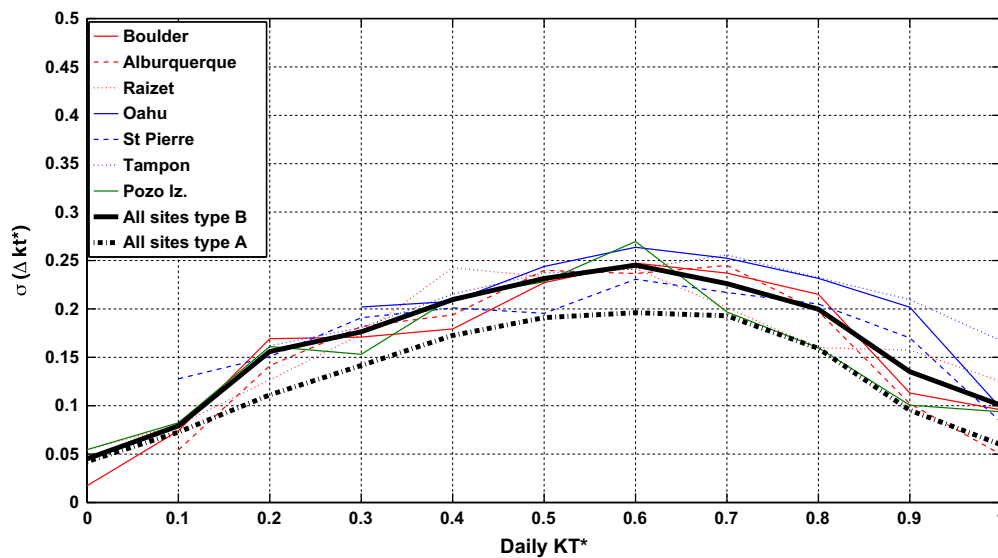


Fig. 8. Average trends for sites with cloud formations influenced by orography (type B). The black line represents the average trend of the concerned sites. For ease of comparison, we also add the average trend of sites type A as a dotted dark line.

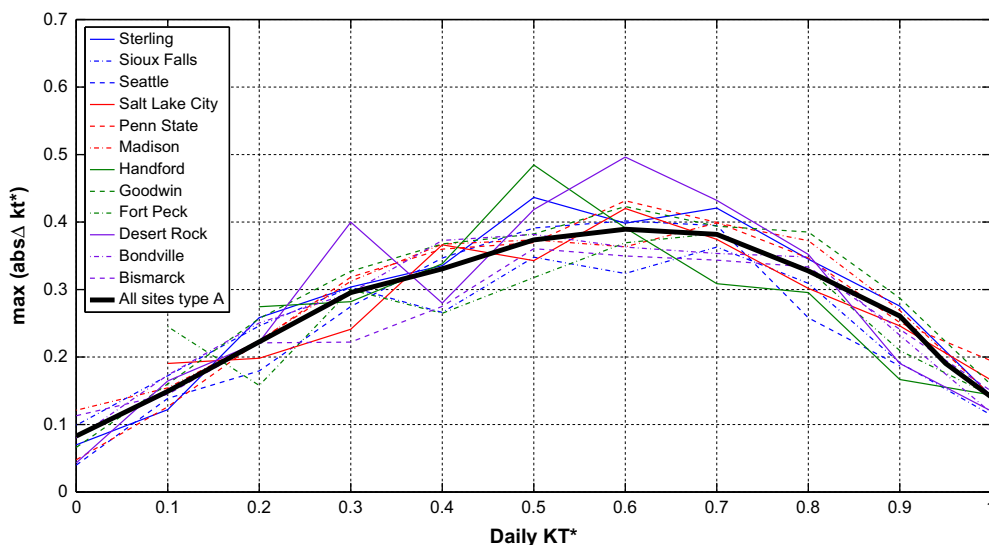


Fig. 9. Same as Fig. 7 but for the $\max(|\Delta kt^*_{\Delta t}|)$ metric.

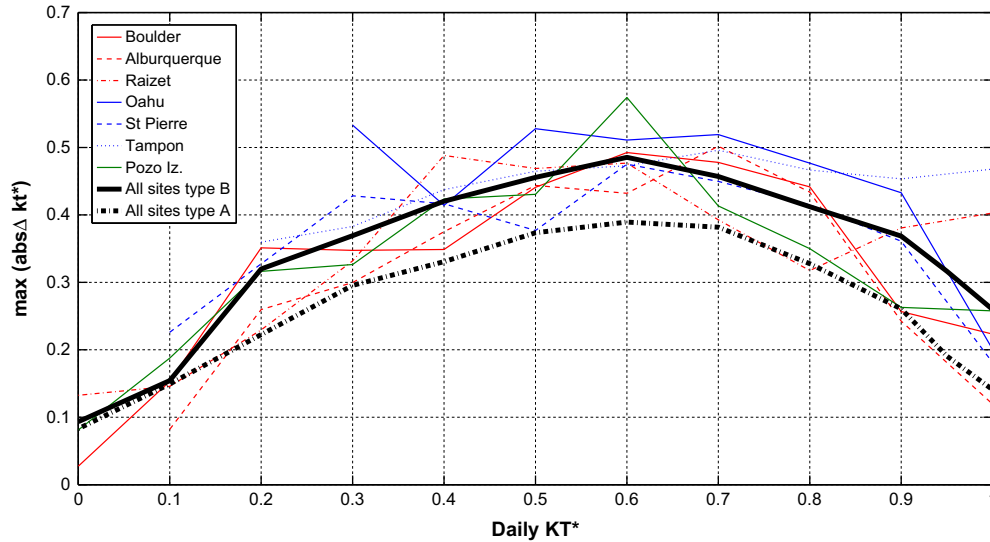


Fig. 10. Same as Fig. 8 but for the $\max(|\Delta kt_{\Delta t}^*|)$ metric.

Table 2
Lookup table global model.

KT*	$\sigma(\Delta kt_{\Delta t}^*)$	$\max(\Delta kt_{\Delta t}^*)$	$mad[\Delta kt_{\Delta t}^*]$	Number of observations
<0.1	0.04 ± 0.02	0.08 ± 0.05	0.03 ± 0.01	42
0.1–0.2	0.07 ± 0.04	0.15 ± 0.10	0.05 ± 0.02	192
0.2–0.3	0.11 ± 0.06	0.23 ± 0.13	0.09 ± 0.04	256
0.3–0.4	0.15 ± 0.06	0.31 ± 0.14	0.11 ± 0.04	320
0.4–0.5	0.18 ± 0.07	0.35 ± 0.15	0.14 ± 0.05	464
0.5–0.6	0.20 ± 0.07	0.40 ± 0.15	0.15 ± 0.05	545
0.6–0.7	0.21 ± 0.07	0.42 ± 0.16	0.16 ± 0.05	712
0.7–0.8	0.20 ± 0.07	0.41 ± 0.15	0.15 ± 0.05	863
0.8–0.9	0.17 ± 0.07	0.36 ± 0.15	0.13 ± 0.05	1236
0.9–0.95	0.14 ± 0.07	0.30 ± 0.16	0.10 ± 0.04	851
0.95–1	0.09 ± 0.06	0.21 ± 0.14	0.06 ± 0.03	1125
<1.1	0.07 ± 0.05	0.18 ± 0.13	0.05 ± 0.03	506

Table 3
Lookup table model for sites with cloud formations influenced by orography (type B).

KT*	$\sigma(\Delta kt_{\Delta t}^*)$	$\max(\Delta kt_{\Delta t}^*)$	$mad[\Delta kt_{\Delta t}^*]$	Number of observations
<0.1	0.05 ± 0.03	0.10 ± 0.08	0.03 ± 0.02	4
0.1–0.2	0.08 ± 0.03	0.16 ± 0.08	0.06 ± 0.02	12
0.2–0.3	0.16 ± 0.06	0.32 ± 0.16	0.12 ± 0.04	28
0.3–0.4	0.18 ± 0.06	0.37 ± 0.17	0.13 ± 0.04	62
0.4–0.5	0.21 ± 0.07	0.42 ± 0.15	0.16 ± 0.05	118
0.5–0.6	0.23 ± 0.07	0.46 ± 0.17	0.17 ± 0.05	192
0.6–0.7	0.25 ± 0.07	0.48 ± 0.16	0.18 ± 0.05	267
0.7–0.8	0.23 ± 0.07	0.46 ± 0.15	0.17 ± 0.05	359
0.8–0.9	0.20 ± 0.07	0.41 ± 0.16	0.14 ± 0.05	531
0.9–0.95	0.16 ± 0.07	0.37 ± 0.17	0.11 ± 0.05	340
0.95–1	0.11 ± 0.07	0.26 ± 0.17	0.07 ± 0.04	375
<1.1	0.10 ± 0.06	0.26 ± 0.17	0.06 ± 0.04	152

variability in case of a perfect forecast of the daily KT^* (i.e. forecasted $KT^* = \text{measured } KT^*$) while Fig. 11b displays the case where both KT^* and intraday variability are inferred from the ECMWF forecasts. In Fig. 11, intraday variability points are randomly drawn from a Gaussian

distribution whose mean and standard deviation are given by the look-up table. In this example, we simply used the look-up table given by Table 2 which represents the ‘general’ model. Since this example is for the site of Saint-Pierre (Réunion island), one could have used Table 3 (local

Table 4
Lookup table model for sites where cloud formation is traceable to weather events only (type A).

KT*	$\sigma(\Delta kt_{\Delta t}^*)$	$\max(\Delta kt_{\Delta t}^*)$	$mad[\Delta kt_{\Delta t}^*]$	Number of observations
<0.1	0.04 ± 0.02	0.08 ± 0.05	0.03 ± 0.01	37
0.1–0.2	0.07 ± 0.04	0.15 ± 0.09	0.05 ± 0.03	180
0.2–0.3	0.11 ± 0.06	0.22 ± 0.13	0.08 ± 0.04	223
0.3–0.4	0.14 ± 0.06	0.29 ± 0.13	0.10 ± 0.04	245
0.4–0.5	0.17 ± 0.07	0.33 ± 0.14	0.13 ± 0.05	313
0.5–0.6	0.19 ± 0.06	0.37 ± 0.13	0.14 ± 0.05	310
0.6–0.7	0.20 ± 0.06	0.39 ± 0.14	0.15 ± 0.05	387
0.7–0.8	0.19 ± 0.06	0.38 ± 0.14	0.14 ± 0.05	441
0.8–0.9	0.16 ± 0.06	0.32 ± 0.13	0.12 ± 0.04	644
0.9–0.95	0.12 ± 0.05	0.26 ± 0.13	0.08 ± 0.04	475
0.95–1	0.08 ± 0.04	0.19 ± 0.12	0.05 ± 0.03	724
<1.1	0.06 ± 0.03	0.14 ± 0.08	0.04 ± 0.02	349

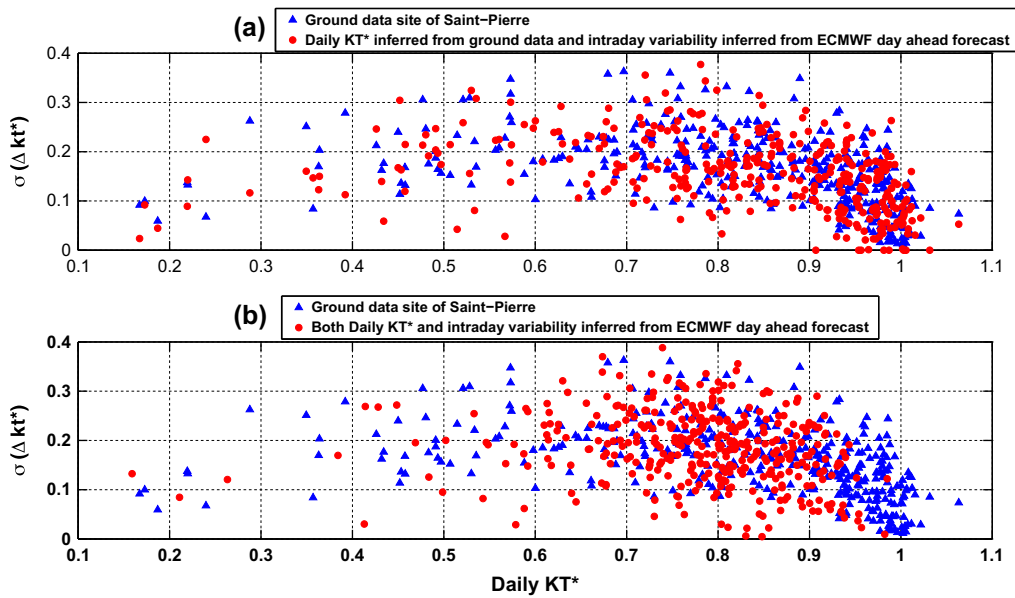


Fig. 11. Intradaily variability inferred from day-ahead ECMWF forecasts.

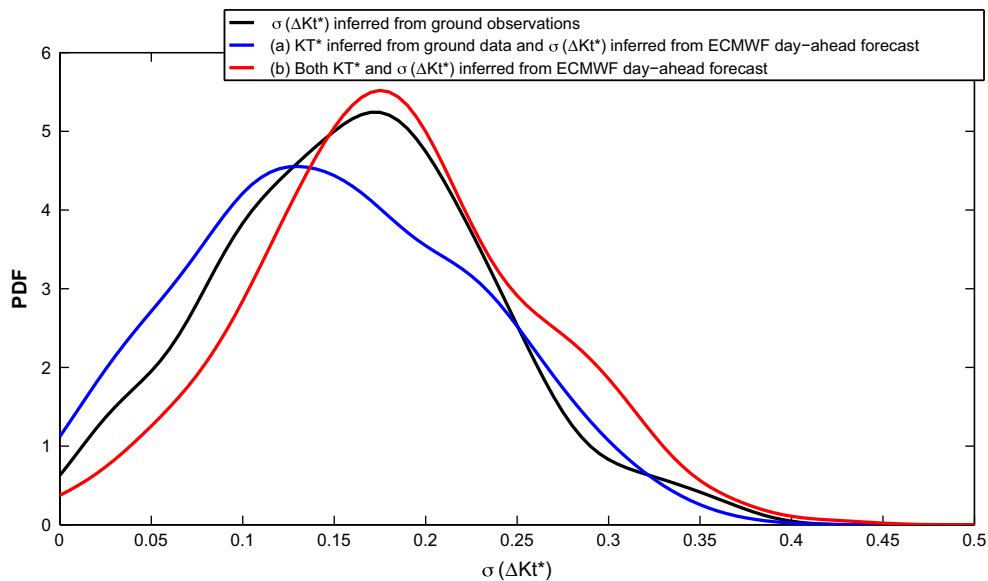


Fig. 12. PDFs of the intradaily variability $\sigma(\Delta kt_{\Delta t}^*)$.

orographic influence) but this would not fundamentally change our illustrative example. Fig. 11a shows the performance of the proposed model in the ideal case of a perfect forecast of KT^* . As seen, the model reproduces quite well the density of the measured variability. In an operational environment where KT^* is predicted with a degree of uncertainty (day-ahead ECMWF for the purpose of illustration), Fig. 11b shows that the proposed parameterization could be valuable; indeed the most interesting zone that corresponds to the maximum variability (intermediate KT^* values) is rather well reproduced. Future improvements of NWP forecasts will make Fig. 11b tend to Fig. 11a.

In order to quantitatively illustrate the previous statements, Fig. 12 plots the probability density functions (PDFs) of the $\sigma(\Delta kt_{\Delta t}^*)$ for the site of St Pierre resulting from the application of our method. As seen, the PDFs (cases (a) and (b) of Fig. 11) are comparable to the PDF of the $\sigma(\Delta kt_{\Delta t}^*)$ ground observations.

4. Conclusions

We presented a site characterization based on 2 parameters: the daily clear sky index KT^* and the intraday variability given by a commonly accepted metric: the standard deviation of the changes in the clear sky index $\sigma(\Delta kt_{\Delta t}^*)$. We showed that the relationship between these two quantities had little dependence on location – suggesting that intraday variability could be inferred from the day's mean clear sky index. However we noted some influence on the relationship that could be traced on a site's orography and its influence on cloud formation. Sites where orographic cloudiness might be expected tend to exhibit more variability for a given mean daily clear index than sites where cloud regimes are driven by weather.

We used the empirical evidence assembled from 20 locations to propose a simple model to infer intraday variability from a day's clear sky index. Such a simple model could be used to enhance the informative content of day(s) ahead NWP forecasts.

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