

$$\begin{cases} y(t) = z'(t) \\ y'(t) = -y(t) - z(t) + 1 \\ y(0) = 1 \\ z(0) = -1 \end{cases}$$

$$X = \begin{pmatrix} z \\ y \end{pmatrix}$$

$$X' = \begin{pmatrix} z' \\ y' \end{pmatrix} = \begin{pmatrix} y \\ -y - z + 1 \end{pmatrix}$$

$$\begin{pmatrix} z' \\ y' \end{pmatrix} = \begin{pmatrix} 0 & 1 \\ -1 & -1 \end{pmatrix} \begin{pmatrix} z \\ y \end{pmatrix} + \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$\begin{pmatrix} z' \\ y' \end{pmatrix} = \begin{pmatrix} y \\ -z - y + 1 \end{pmatrix}$$

Aplicar Heun a

$$\begin{pmatrix} z \\ y \end{pmatrix}' = \begin{pmatrix} y \\ -z - y + 1 \end{pmatrix}$$

$$F \begin{pmatrix} z \\ y \end{pmatrix} = \begin{pmatrix} y \\ -z - y + 1 \end{pmatrix} \quad \swarrow$$

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$$\text{(Heun)}: \begin{cases} X_{k+1}^H = X_k^H + \frac{h}{2} \left[ F(z_k, X_k^H) + F(z_{k+1}, X_k^H + h \cdot F(z_k, X_k^H)) \right] \\ X_0^H = X_0 \end{cases}$$

$$\text{(EA)}: \begin{cases} X_{k+1}^E = X_k^E + h \cdot F(z_k, X_k^E) \\ X_0^E = X_0 \end{cases}$$

$$X_1^0 = \begin{pmatrix} z_1^0 \\ y_1^0 \end{pmatrix}$$

$$\begin{pmatrix} z_1^1 \\ y_1^1 \end{pmatrix} = \begin{pmatrix} z_1^0 \\ y_1^0 \end{pmatrix} + \frac{h}{2} \left[ \begin{pmatrix} y_1^0 \\ -z_1^0 - y_1^0 + 1 \end{pmatrix} + F \left( \begin{pmatrix} z_1^0 \\ y_1^0 \end{pmatrix} + h \cdot \begin{pmatrix} y_1^0 \\ -z_1^0 - y_1^0 + 1 \end{pmatrix} \right) \right]$$