

Initialize extension field and polynomial ring over it. Syntax is `initF(p,m)` for $GF(p^m)$.

```
> initF(2,3);
```

$$\alpha^3 + \alpha + 1$$

Initialize Reed-Solomon code: `initRS(n,r)`, n = code length, r = code redundancy.

The roots of the code are α^i for $i=1,2,\dots,r$. Returns code generator polynomial $g(x) =$

$$(x - \alpha)(x - \alpha^2) \dots (x - \alpha^{(n-k-1)})$$

```
> g := initRS(7,4); # n=7, r=4, k=3
```

$$g := \alpha + 1 + \alpha x + x^2 + (\alpha + 1)x^3 + x^4$$

Generate random message

```
> u := rmsg();
```

$$u := \alpha^2 + (\alpha^2 + \alpha + 1)x + (\alpha^2 + \alpha + 1)x^2$$

Encode message using a *systematic encoder*

```
> c := encodeRS(u);
```

$$c := \alpha + x + \alpha^2 x^2 + \alpha x^3 + \alpha^2 x^4 + (\alpha^2 + \alpha + 1)x^5 + (\alpha^2 + \alpha + 1)x^6$$

Verify syndrome is zero

```
> syndrome(c);
```

$$0$$

Generate random error vector

```
> e:=rerr(2);
```

$$e := \alpha^2 + 1 + (\alpha^2 + \alpha + 1)x^6$$

Compute received word

```
> y:=P['+'](c,e);
```

$$y := \alpha^2 + \alpha + 1 + x + \alpha^2 x^2 + \alpha x^3 + \alpha^2 x^4 + (\alpha^2 + \alpha + 1)x^5$$

Decode received word

```
> decodeRS(y);
```

```
syndrome S(x) : :
```

$$\alpha + 1 + (\alpha^2 + \alpha)x + x^2 + (\alpha^2 + \alpha + 1)x^3$$

```
Running Euclidean algorithm:
```

```
iteration: -1
```

```
q : 0
```

```
r :
```

$$x^4$$

```
s :
```

$$1$$

```
t :
```

$$0$$

iteration: 0

q : 0

r :

$$\alpha + 1 + (\alpha^2 + \alpha)x + x^2 + (\alpha^2 + \alpha + 1)x^3$$

s :

0

t :

1

iteration: 1

q :

$$\alpha^2 + \alpha + \alpha^2 x$$

r :

$$1 + (\alpha^2 + 1)x + (\alpha + 1)x^2$$

s :

1

t :

$$\alpha^2 + \alpha + \alpha^2 x$$

iteration: 2

q :

$$1 + \alpha^2 x$$

r :

$$\alpha + (\alpha^2 + \alpha + 1) x$$

s :

$$1 + \alpha^2 x$$

t :

$$\alpha^2 + \alpha + 1 + x + (\alpha^2 + \alpha) x^2$$

Lambda:

$$\alpha^2 + \alpha + 1 + x + (\alpha^2 + \alpha) x^2$$

Gamma:

$$\alpha + (\alpha^2 + \alpha + 1) x$$

error word:

$$\alpha^2 + 1 + (\alpha^2 + \alpha + 1) x^6$$

codeword :

$$\alpha + x + \alpha^2 x^2 + \alpha x^3 + \alpha^2 x^4 + (\alpha^2 + \alpha + 1) x^5 + (\alpha^2 + \alpha + 1) x^6$$

syndrome :

$$0$$

[>