



## Diseño de Amplificadores de Microondas

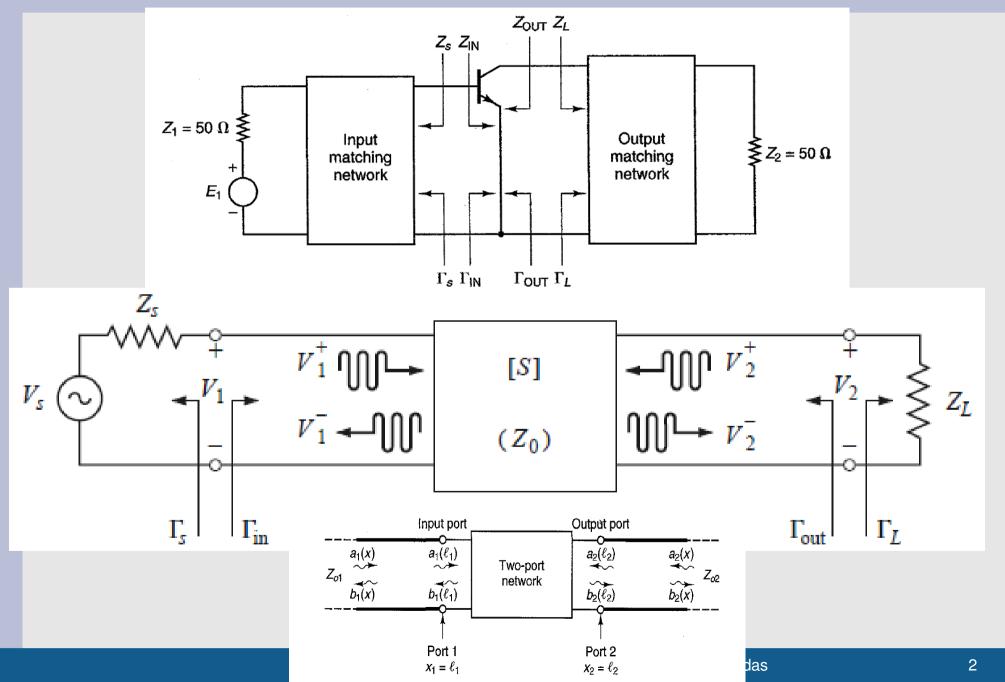
# Parte 2 Estabilidad y Métodos de Diseño

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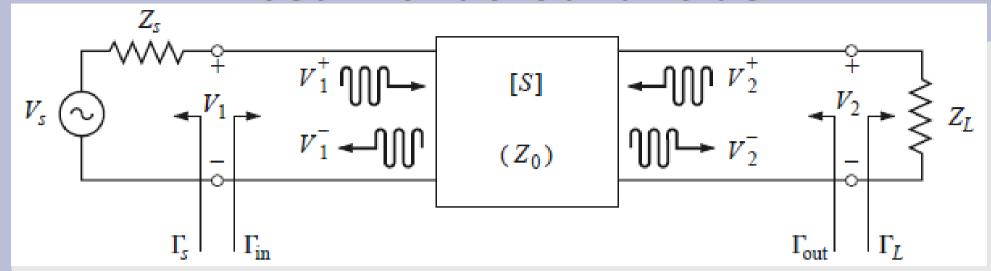
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## Estructura Basica Amplificador de Microondas



#### Resumiendo Ganancias



$$G = \frac{P_L}{P_{IN}} = f(\Gamma_L, [S])$$

$$G = \frac{P_L}{P_{IN}} = f(\Gamma_L, [S]) \qquad G = \frac{P_L}{P_{in}} = \frac{|S_{21}|^2 (1 - |\Gamma_L|^2)}{(1 - |\Gamma_{in}|^2) |1 - S_{22}\Gamma_L|^2}$$

$$G_T = \frac{P_L}{P_{AVS}} = f(\Gamma_S, \Gamma_L, [S]) \qquad G_T = \frac{1 - |\Gamma_S|^2}{|1 - \Gamma_{IN}\Gamma_S|^2} |S_{21}|^2 \frac{1 - |\Gamma_L|^2}{|1 - S_{22}\Gamma_L|^2} \qquad \text{Transducer Gain}$$

$$G_A = \frac{P_{AVN}}{P_{AVS}} = f(\Gamma_S, [S])$$

$$G_A = \frac{P_{AVN}}{P_{AVS}} = f(\Gamma_S, [S])$$
  $G_A = \frac{1 - |\Gamma_S|^2}{|1 - S_{11}\Gamma_S|^2} |S_{21}|^2 \frac{1}{1 - |\Gamma_{OUT}|^2}$  Available Power

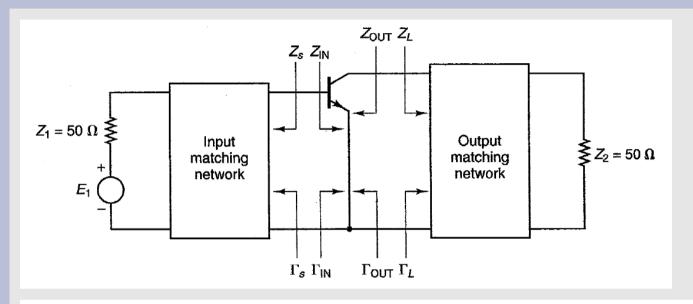
Power Gain

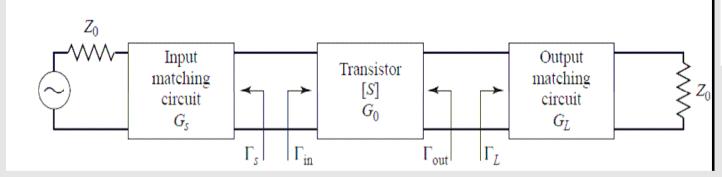
$$\Gamma_{\text{in}} = S_{11} + \frac{S_{12}S_{21}\Gamma_L}{1 - S_{22}\Gamma_L} = \frac{Z_{\text{in}} - Z_0}{Z_{\text{in}} + Z_0} \quad \Gamma_{\text{out}} = S_{22} + \frac{S_{12}S_{21}\Gamma_S}{1 - S_{11}\Gamma_S} \quad \Gamma_S = \frac{Z_S - Z_0}{Z_S + Z_0} \quad \Gamma_L = \frac{Z_L - Z_0}{Z_L + Z_0}$$

$$\Gamma_{\text{out}} = S_{22} + \frac{S_{12}S_{21}\Gamma_S}{1 - S_{11}\Gamma_S}$$

$$\Gamma_S = \frac{Z_S - Z_0}{Z_S + Z_0} \mid_{\Gamma_L = \frac{1}{2}}$$

#### Ganancias en estructura de amplificador





$$G_T = G_S G_0 G_L$$

G<sub>S</sub>, G<sub>L</sub> pueden ser >1 al reducir las pérdidas que habría debido a desadaptación

$$G_S = \frac{1 - |\Gamma_S|^2}{|1 - \Gamma_{\text{in}} \Gamma_S|^2}$$

$$G_0 = |S_{21}|^2,$$

$$G_L = \frac{1 - |\Gamma_L|^2}{|1 - S_{22} \Gamma_L|^2}$$

$$\Gamma_{\text{in}} = S_{11} + \frac{S_{12}S_{21}\Gamma_L}{1 - S_{22}\Gamma_L}$$

Si transistor "unilateral" (S12=0 o despreciable)

 $\Gamma_{\rm in} = S_{11}$ 

#### **Estabilidad: Previo**

Previo: 
$$\Gamma = \frac{Z - Z_0}{Z + Z_0} \Rightarrow |\Gamma| < 1 \Leftrightarrow \text{Re}(Z) > 0$$

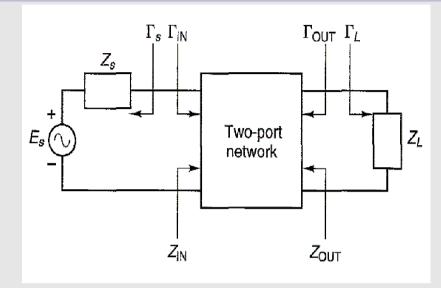
# Estabilidad: Incondicional y Condicional

Estabilidad Incondicional =

Estable para todo  $Z_S$ ,  $Z_L$  pasivo (es decir para todo  $\Gamma_S$ ,  $\Gamma_L$  que cumple  $\mid \Gamma_S \mid <1$ ,  $\mid \Gamma_I \mid <1$ )  $\Leftrightarrow$ 

$$\left|\Gamma_{\text{IN}}\right| = \left|S_{11} + \frac{S_{12}S_{21}\Gamma_L}{1 - S_{22}\Gamma_L}\right| < 1$$

$$\left|\Gamma_{\text{OUT}}\right| = \left|S_{22} + \frac{S_{12}S_{21}\Gamma_{s}}{1 - S_{11}\Gamma_{s}}\right| < 1$$



y parámetros S no tienen polos en el semiplano derecho ("Rollett proviso"). Asegurado al poderse medir por ej.

R. Jackson, Rollett Proviso in the Stability of Linear Microwave Circuits—A Tutorial, IEEE TRANSACTIONS ON MICROWAVE THEORY AND TECHNIQUES, VOL. 54, NO. 3, MARCH 2006

Estabilidad Condicional = "Potencialmente inestable" si estable solo para cierto rango de valores  $Z_S$ ,  $Z_L$  pasivos

## Círculos de Estabilidad (1)

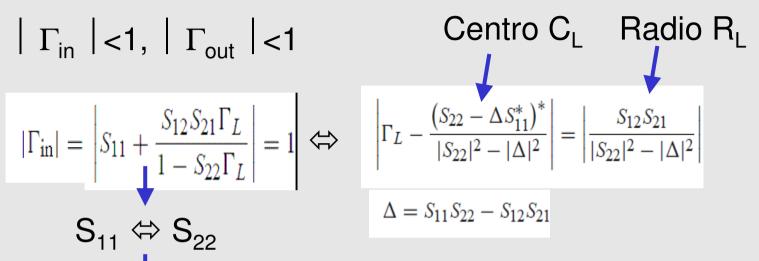
$$\mid \Gamma_{\rm in} \mid <1, \mid \Gamma_{\rm out} \mid <1$$

$$|\Gamma_{\text{in}}| = \left| S_{11} + \frac{S_{12}S_{21}\Gamma_L}{1 - S_{22}\Gamma_L} \right| = 1 \iff$$

$$S_{11} \Leftrightarrow S_{22}$$

$$|\Gamma_{\text{out}}| = \left| S_{22} + \frac{S_{12}S_{21}\Gamma_{S}}{1 - S_{11}\Gamma_{S}} \right| = 1 \iff \Gamma_{\text{S}} \text{ en círculo de centro } C_{\text{S}} \text{ y radio } R_{\text{S}}$$

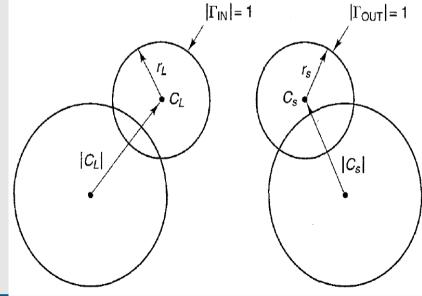
$$C_{S} = \frac{\left(S_{11} - \Delta S_{22}^{*}\right)^{*}}{|S_{11}|^{2} + |\Delta|^{2}}$$



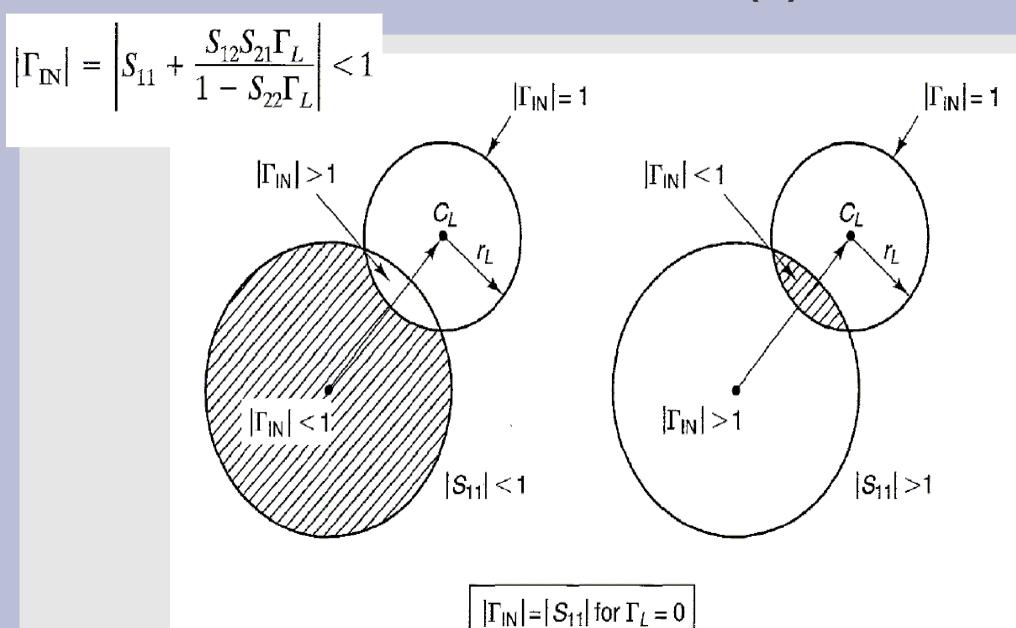
$$\Delta = S_{11}S_{22} - S_{12}S_{21}$$

$$C_S = \frac{\left(S_{11} - \Delta S_{22}^*\right)^*}{|S_{11}|^2 - |\Delta|^2}$$

$$R_S = \left|\frac{S_{12}S_{21}}{|S_{11}|^2 - |\Delta|^2}\right|$$

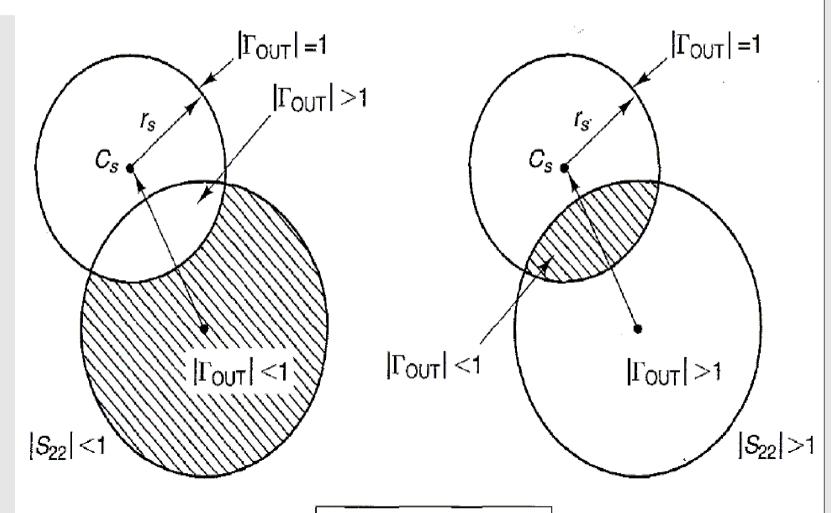


## Círculos de Estabilidad (2)



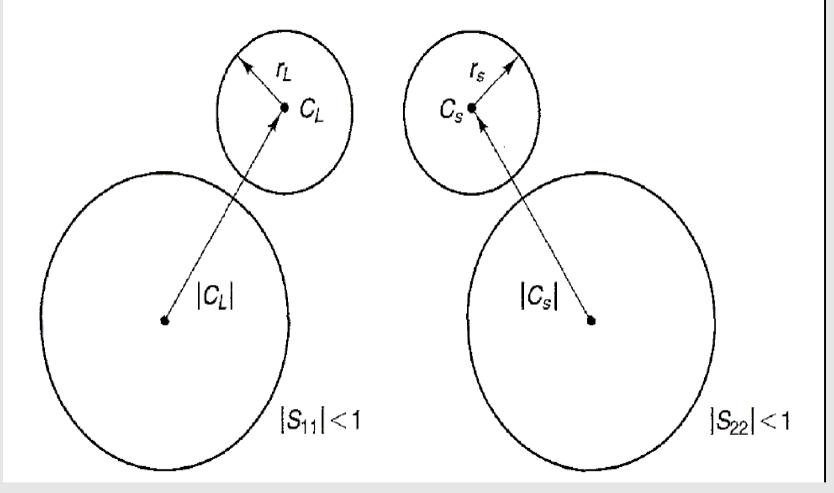
## Círculos de Estabilidad (3)

$$\left| \Gamma_{\text{OUT}} \right| = \left| S_{22} + \frac{S_{12} S_{21} \Gamma_s}{1 - S_{11} \Gamma_s} \right| < 1$$



$$|\Gamma_{\mathsf{OUT}}| = |S_{22}|$$
 for  $\Gamma_{s} = 0$ 

#### Círculos de Estabilidad: Estabilidad Incondicional



$$||C_L| - R_L| > 1$$
 for  $|S_{11}| < 1$   
 $||C_S| - R_S| > 1$  for  $|S_{22}| < 1$ 

#### Tests para estabilidad incondicional:

$$K = \frac{1 - |S_{11}|^2 - |S_{22}|^2 + |\Delta|^2}{2|S_{12}S_{21}|} > 1$$

$$|\Delta| = |S_{11}S_{22} - S_{12}S_{21}| < 1$$

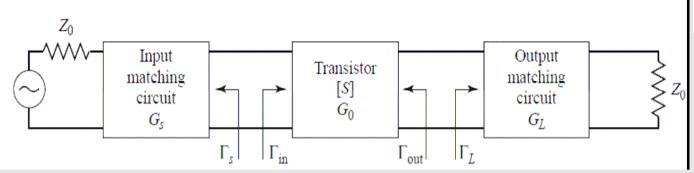
Para todo w, (Woods, 1976)

$$\mu = \frac{1 - |S_{11}|^2}{\left|S_{22} - \Delta S_{11}^*\right| + |S_{12}S_{21}|} > 1$$
 Para todo w, (Edwards y Sinksy, 1992)

y parámetros S no tienen polos en el semiplano derecho ("Rollett proviso"). Asegurado al poderse medir por ej.

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## Diseño para máxima ganancia (Adaptación Conjugada)



$$\Gamma_{\text{in}} = \Gamma_S^*$$
  $\Gamma_{\text{out}} = \Gamma_L^*$ 

$$G_{T_{\text{max}}} = \frac{1}{1 - |\Gamma_S|^2} |S_{21}|^2 \frac{1 - |\Gamma_L|^2}{|1 - S_{22}\Gamma_L|^2}$$

Además: 
$$G_{Tmax} = G_{pmax} = G_{Amax}$$

$$G_T = G_S G_0 G_L$$

$$G_0 = |S_{21}|^2,$$

$$G_L = \frac{1 - |\Gamma_L|^2}{|1 - S_{22}\Gamma_L|^2}$$

$$\Gamma_{\text{in}} = S_{11} + \frac{S_{12}S_{21}\Gamma_L}{1 - S_{22}\Gamma_L} = \frac{Z_{\text{in}} - Z_0}{Z_{\text{in}} + Z_0}$$

$$\Gamma_{\text{out}} = S_{22} + \frac{S_{12}S_{21}\Gamma_S}{1 - S_{11}\Gamma_S}$$

## Diseño para máxima ganancia (Adaptación Conjugada): $\Gamma_{s}$ , $\Gamma_{l}$

$$\Gamma_{\rm in} = \Gamma_S^*$$
  $\Gamma_{\rm out} = \Gamma_L^*$ 

$$Z_0$$

$$Coutput matching circuit G_S$$

$$C_S \qquad \Gamma_{in} \qquad \Gamma_{out} \qquad \Gamma_L$$

$$C_L \qquad C_L \qquad C_L$$

$$C_L \qquad C_L \qquad C_L$$

$$\Gamma_{\text{in}} = S_{11} + \frac{S_{12}S_{21}\Gamma_L}{1 - S_{22}\Gamma_L} = \frac{Z_{\text{in}} - Z_0}{Z_{\text{in}} + Z_0}$$

$$\Gamma_{\text{out}} = S_{22} + \frac{S_{12}S_{21}\Gamma_S}{1 - S_{11}\Gamma_S}$$

$$\Gamma_{\text{out}} = S_{22} + \frac{S_{12}S_{21}\Gamma_S}{1 - S_{11}\Gamma_S}$$

$$\Gamma_{S}^{*} = S_{11} + \frac{S_{12}S_{21}\Gamma_{L}}{1 - S_{22}\Gamma_{L}}$$

$$\Gamma_{L}^{*} = S_{22} + \frac{S_{12}S_{21}\Gamma_{S}}{1 - S_{11}\Gamma_{S}}$$

$$\Gamma_{L}^{*} = \frac{S_{22} - \Delta\Gamma_{S}}{1 - S_{11}\Gamma_{S}},$$
Sustituyendo y hacien cuentas, usando que:

$$\Gamma_S = S_{11}^* + \frac{S_{12}^* S_{21}^*}{1/\Gamma_L^* - S_{22}^*},$$

$$\Gamma_L^* = \frac{S_{22} - \Delta \Gamma_S}{1 - S_{11} \Gamma_S},$$



Sustituyendo y haciendo

$$\Delta \left( S_{11}^* S_{22}^* - S_{12}^* S_{21}^* \right) = |\Delta|^2$$

$$(S_{11} - \Delta S_{22}^*)\Gamma_S^2 + (|\Delta|^2 - |S_{11}|^2 + |S_{22}|^2 - 1)\Gamma_S + (S_{11}^* - \Delta^* S_{22}) = 0$$

## Diseño para máxima ganancia (Adaptación Conjugada): $\Gamma_S$ , $\Gamma_I$



$$(S_{11} - \Delta S_{22}^*)\Gamma_S^2 + (|\Delta|^2 - |S_{11}|^2 + |S_{22}|^2 - 1)\Gamma_S + (S_{11}^* - \Delta^* S_{22}) = 0$$

$$\Gamma_{Ms} = \frac{B_1 \pm \sqrt{B_1^2 - 4|C_1|^2}}{2C_1}$$

$$B_1 = 1 + |S_{11}|^2 - |S_{22}|^2 - |\Delta|^2,$$

$$B_2 = 1 + |S_{22}|^2 - |S_{11}|^2 - |\Delta|^2,$$

$$C_1 = S_{11} - \Delta S_{22}^*,$$

$$C_2 = S_{22} - \Delta S_{11}^*.$$

$$B_1 = 1 + |S_{11}|^2 - |S_{22}|^2 - |\Delta|^2,$$

$$B_2 = 1 + |S_{22}|^2 - |S_{11}|^2 - |\Delta|^2,$$

$$C_1 = S_{11} - \Delta S_{22}^*,$$

$$C_2 = S_{22} - \Delta S_{11}^*.$$

Se puede mostrar (Ver libro G. Gonzalez) que:

- si los términos dentro de la raices son positivos => K>1
- si  $|\Delta| < 1 => B1>0 y B2 > 0$

=> si K>1 y  $|\Delta|$  <1 (incondicionalmente estable) existe una solución para tener  $\Gamma_{ML}$  y  $\Gamma_{MS}$  con  $|\Gamma_{ML}| < 1$  y  $|\Gamma_{MS}| < 1$ , que es la solución con signo menos

$$G_{T_{\text{max}}} = \frac{1}{1 - |\Gamma_S|^2} |S_{21}|^2 \frac{1 - |\Gamma_L|^2}{|1 - S_{22}\Gamma_L|^2} \qquad G_{T,\text{max}} = \frac{|S_{21}|}{|S_{12}|} (K - \sqrt{K^2 - 1})$$

$$G_{T,\text{max}} = \frac{|S_{21}|}{|S_{12}|} (K - \sqrt{K^2 - 1})$$

## Diseño para máxima ganancia (Adaptación Conjugada): Caso unilateral

$$S_{12} = 0$$
  $\Gamma_{\text{in}} = S_{11} + \frac{S_{12}S_{21}\Gamma_L}{1 - S_{22}\Gamma_L} = \frac{Z_{\text{in}} - Z_0}{Z_{\text{in}} + Z_0}$   $\Gamma_S = S_{11}^*$   $\Gamma_L = S_{22}^*$ 

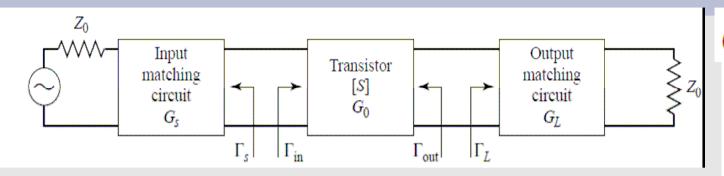
$$\Gamma_{\text{out}} = S_{22} + \frac{S_{12}S_{21}\Gamma_S}{1 - S_{11}\Gamma_S}$$

$$\Gamma_S = S_{11}^*$$

$$\Gamma_L = S_{22}^*$$

$$G_{TU_{\text{max}}} = \frac{1}{1 - |S_{11}|^2} |S_{21}|^2 \frac{1}{1 - |S_{22}|^2}.$$

## Diseño para Ganancia Específica



- $G_0$  dado por transistor => modificar  $G_S$  o  $G_1$  con adaptación no óptima
- Mejora ancho de banda también.
- Veremos caso Unilateral (=> S<sub>12</sub>= 0),

#### incondicionalmente estable

(Caso Bilateral y caso unilat. Cond estable tratados en libro G. Gonzalez)

Para ver si se puede considerar aprox. unilateral

Para ver si se puede considerar aprox. unilateral 
$$\frac{1}{(1+U)^2} < \frac{G_T}{G_{TU}} < \frac{1}{(1-U)^2}$$
 
$$U = \frac{|S_{12}||S_{21}||S_{11}||S_{22}|}{(1-|S_{11}|^2)(1-|S_{22}|^2)}$$
 
$$< 0.2...0.3 \text{ dB}$$
 U:

$$G_{T} = G_{S}G_{0}G_{L}$$

$$G_{S} = \frac{1 - |\Gamma_{S}|^{2}}{|1 - \Gamma_{\text{in}}\Gamma_{S}|^{2}}$$

$$G_{0} = |S_{21}|^{2},$$

$$G_{L} = \frac{1 - |\Gamma_{L}|^{2}}{|1 - S_{22}\Gamma_{L}|^{2}}$$

U: "unilateral

## Diseño para Ganancia Específica Círculos de Ganancia Constante (1)

$$S_{12} = 0 \Rightarrow \Gamma_{in} = S_{11} \text{ y } \Gamma_{out} = S_{22}$$
 $G_T = G_S G_0 G_L$ 

Incond. estable =>  $|S_{11}|<1$ ,  $|S_{22}|<1$ 

$$G_S = \frac{1 - |\Gamma_S|^2}{|1 - S_{11}\Gamma_S|^2}$$

$$G_{S} = \frac{1 - |\Gamma_{S}|^{2}}{|1 - S_{11}\Gamma_{S}|^{2}} \qquad G_{S_{\text{max}}} = \frac{1}{1 - |S_{11}|^{2}} \qquad \bigoplus_{T_{S} = S_{11}^{*}} G_{L} = \frac{1 - |\Gamma_{L}|^{2}}{|1 - S_{22}\Gamma_{L}|^{2}} \qquad G_{L_{\text{max}}} = \frac{1}{1 - |S_{22}|^{2}}$$

$$\square S = S_{11}^*$$

$$\square \Gamma_L = S_{22}^*$$

$$g_S = \frac{G_S}{G_{S_{\text{max}}}} = \frac{1 - |\Gamma_S|^2}{|1 - S_{11}\Gamma_S|^2} (1 - |S_{11}|^2), \quad g_S, g_L \text{ constantes:}$$
 círculos en plano  $\Gamma_S, \Gamma_L$ 

$$g_L = \frac{G_L}{G_{L_{\text{max}}}} = \frac{1 - |\Gamma_L|^2}{|1 - S_{22}\Gamma_L|^2} (1 - |S_{22}|^2)$$

círculos en plano 
$$\Gamma_{\rm S}$$
,  $\Gamma_{\rm L}$ 

 $0 \le g_S \le 1$  and  $0 \le g_L \le 1$ .

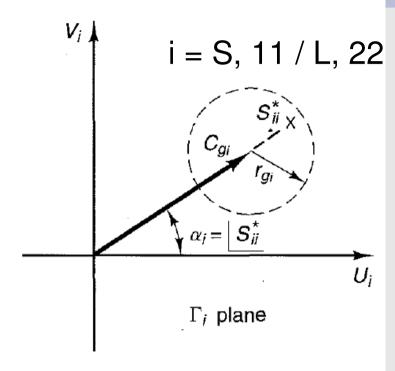
# Diseño para Ganancia Específica Círculos de Ganancia Constante (2)

$$C_S = \frac{g_S S_{11}^*}{1 - (1 - g_S)|S_{11}|^2},$$

$$R_S = \frac{\sqrt{1 - g_S} \left( 1 - |S_{11}|^2 \right)}{1 - (1 - g_S)|S_{11}|^2}$$

$$C_L = \frac{g_L S_{22}^*}{1 - (1 - g_L)|S_{22}|^2},$$

$$R_L = \frac{\sqrt{1 - g_L} \left( 1 - |S_{22}|^2 \right)}{1 - (1 - g_L)|S_{22}|^2}.$$

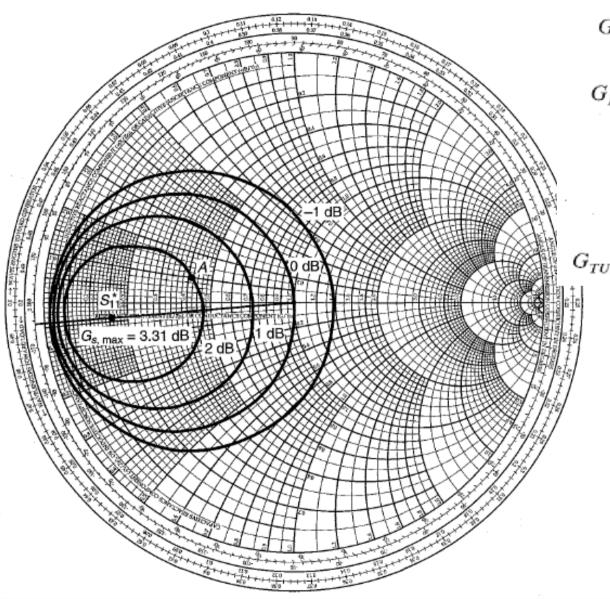


$$g_S = \frac{G_S}{G_{S \text{ max}}} = 1 \Leftrightarrow G_S = G_{S \text{ max}} \Leftrightarrow \Gamma_S = \Gamma_{in}^* = S_{11}^*$$

$$g_L = \frac{G_L}{G_{L \max}} = 1 \Leftrightarrow G_L = G_{L \max} \Leftrightarrow \Gamma_L = \Gamma_{out}^* = S_{22}^*$$

$$G_S$$
,  $G_L = 1$  (0 dB) => círculos pasan por origen  $(\Gamma_S = \Gamma_L = 0 => G_T = |S_{21}|^2 = G_0)$ 

#### Εj.



$$G_{s, \text{max}} = \frac{1}{1 - |S_{11}|^2} = 2.141$$
 or 3.31 dB

$$G_{L, \text{max}} = \frac{1}{1 - |S_{22}|^2} = 1.046$$
 or 0.195 dB

$$G_o = |S_{21}|^2 = 19.8$$
 or 12.97 dB

$$G_{TU, \max}(dB) = 3.31 + 12.97 + 0.195 = 16.47 dB$$