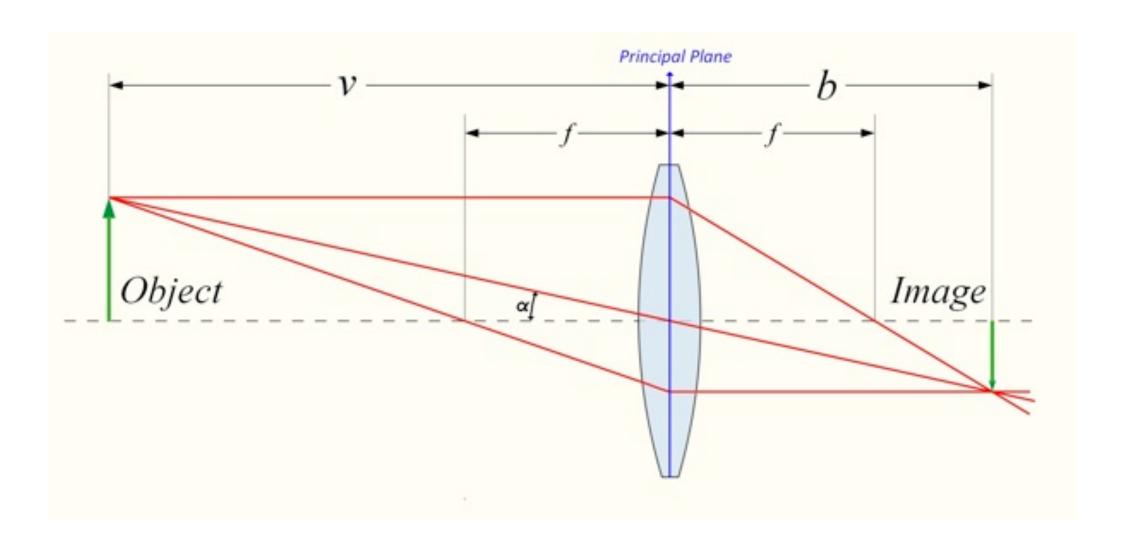
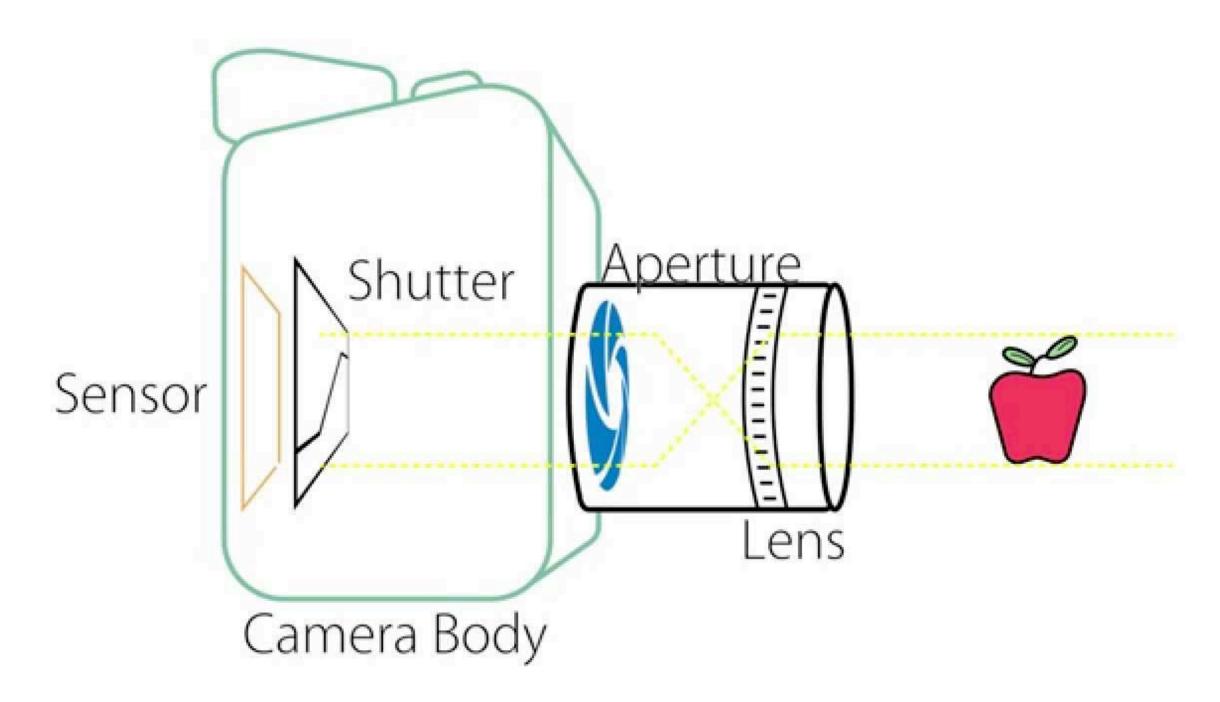
Robotica autonoma en entornos hostiles

Vision 3D

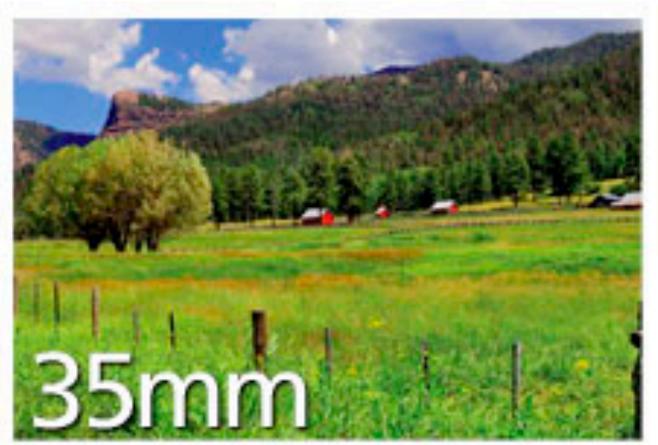
Imágenes Digitales

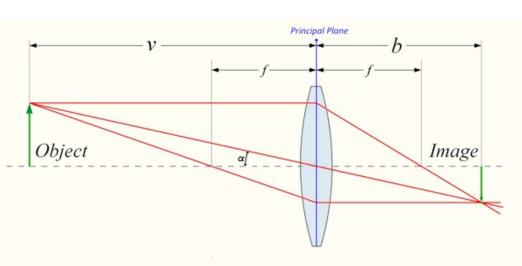






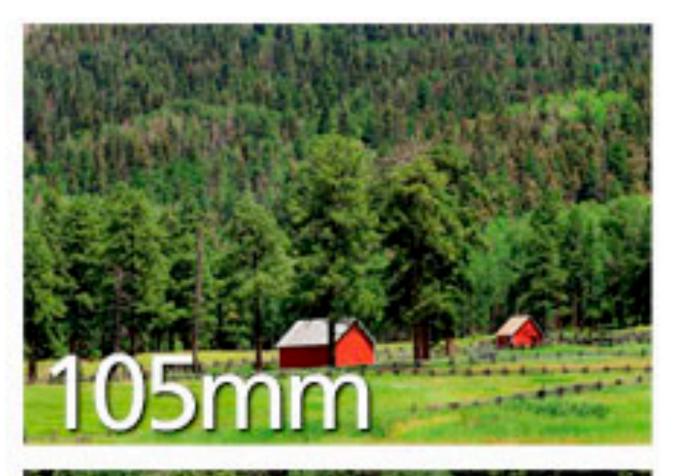


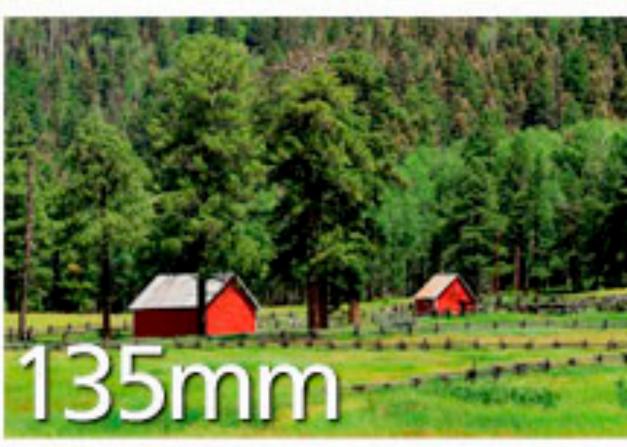


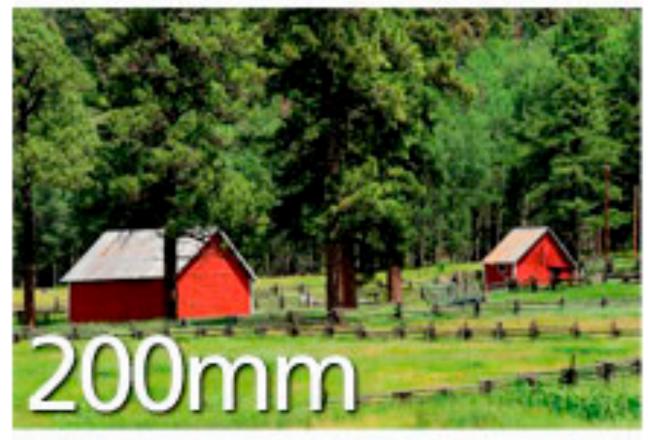


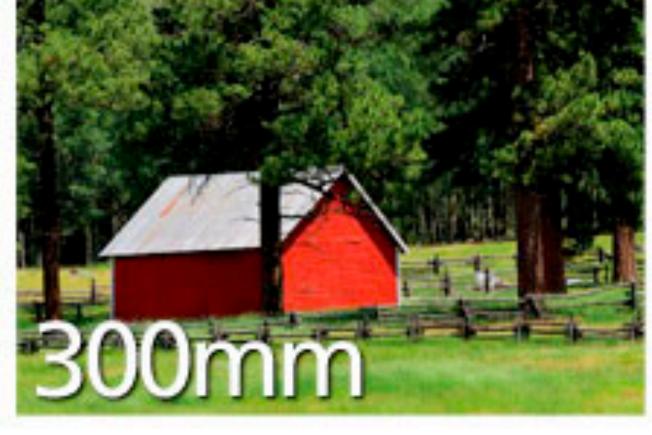






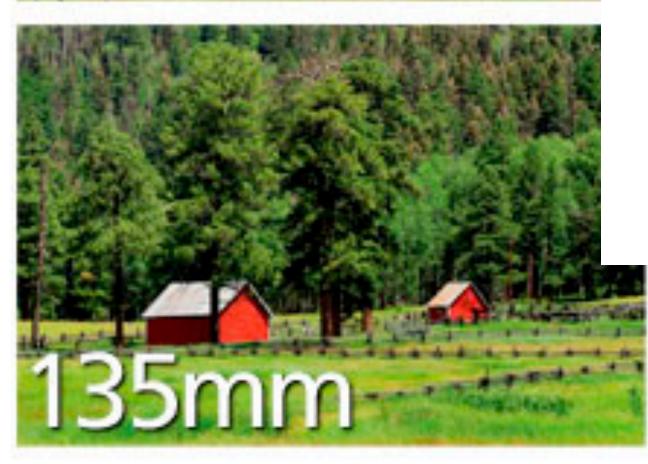


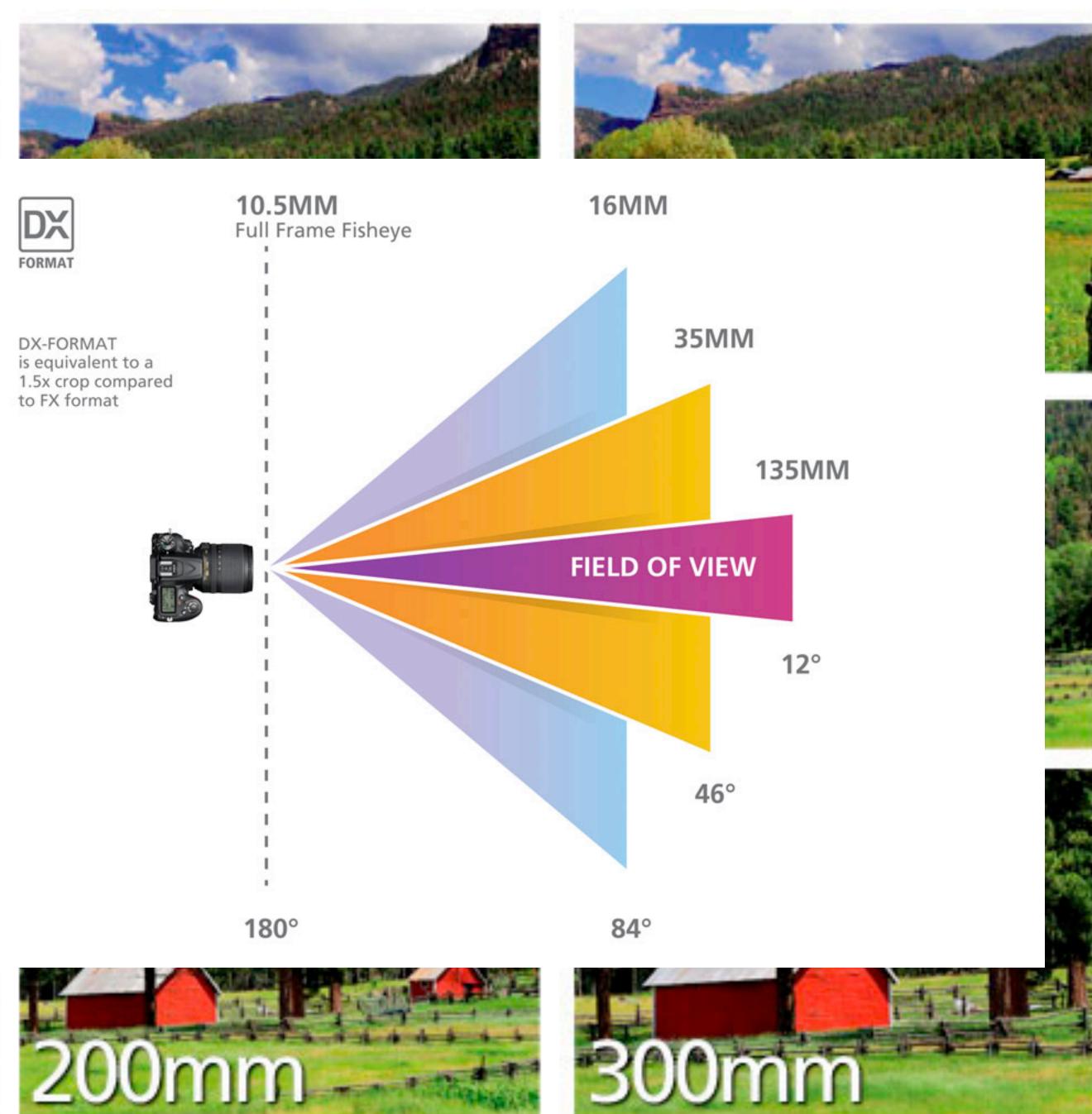


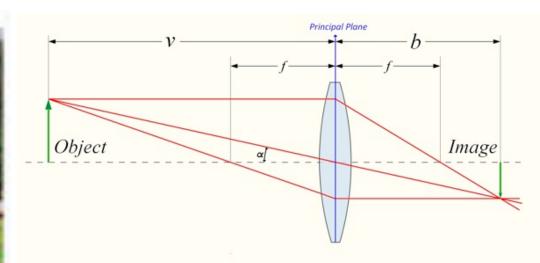






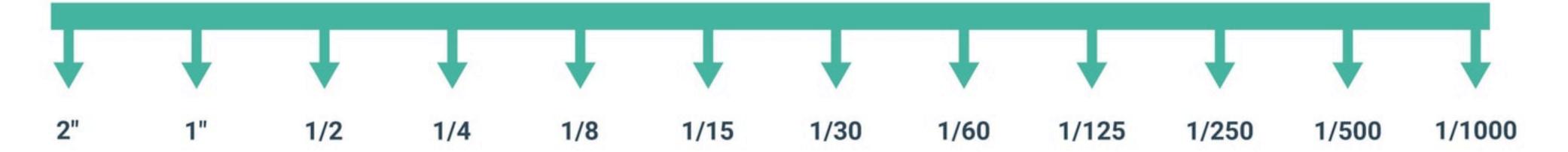








SHUTTER SPEED

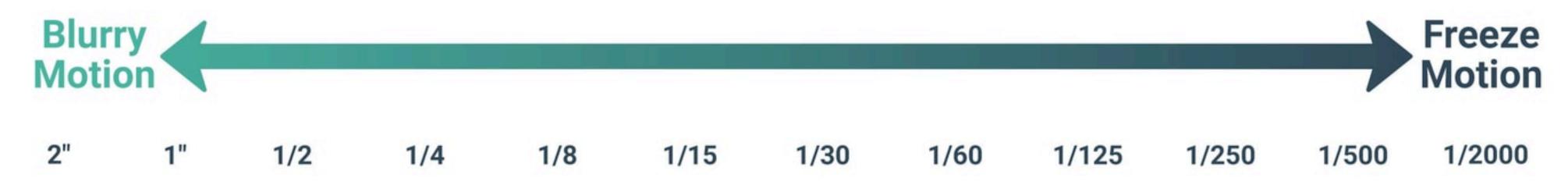


MOTION



Shutter Speed and Motion

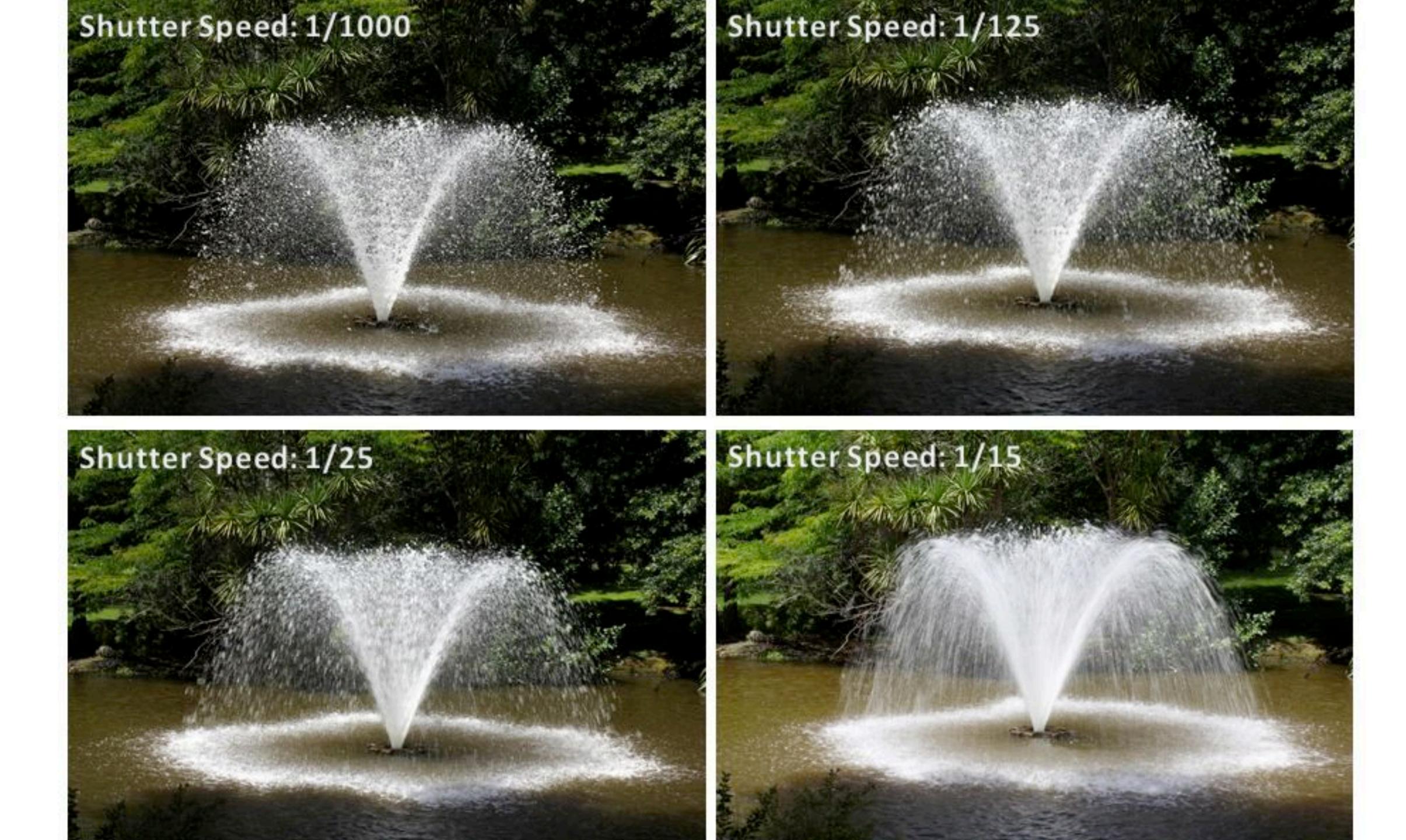


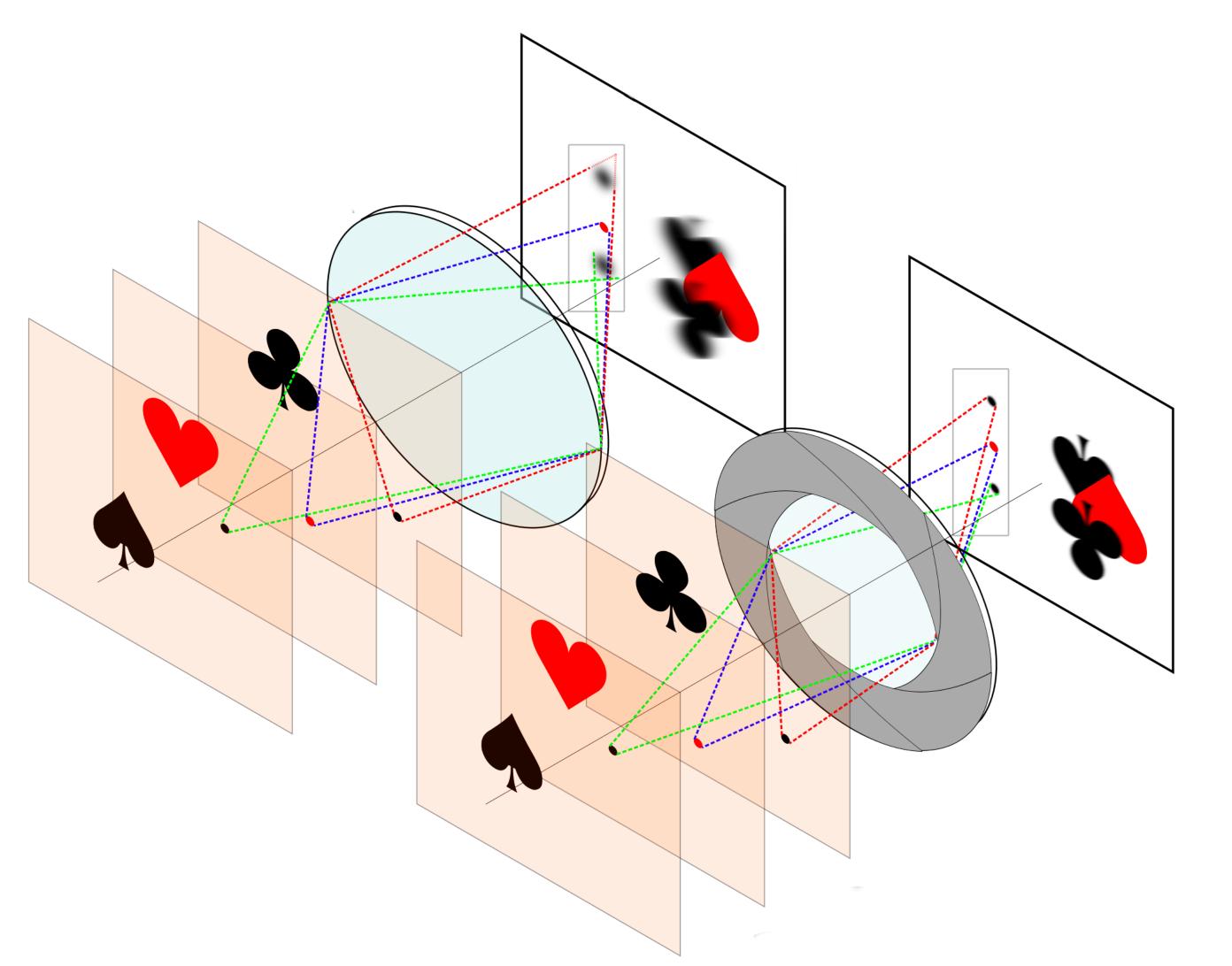




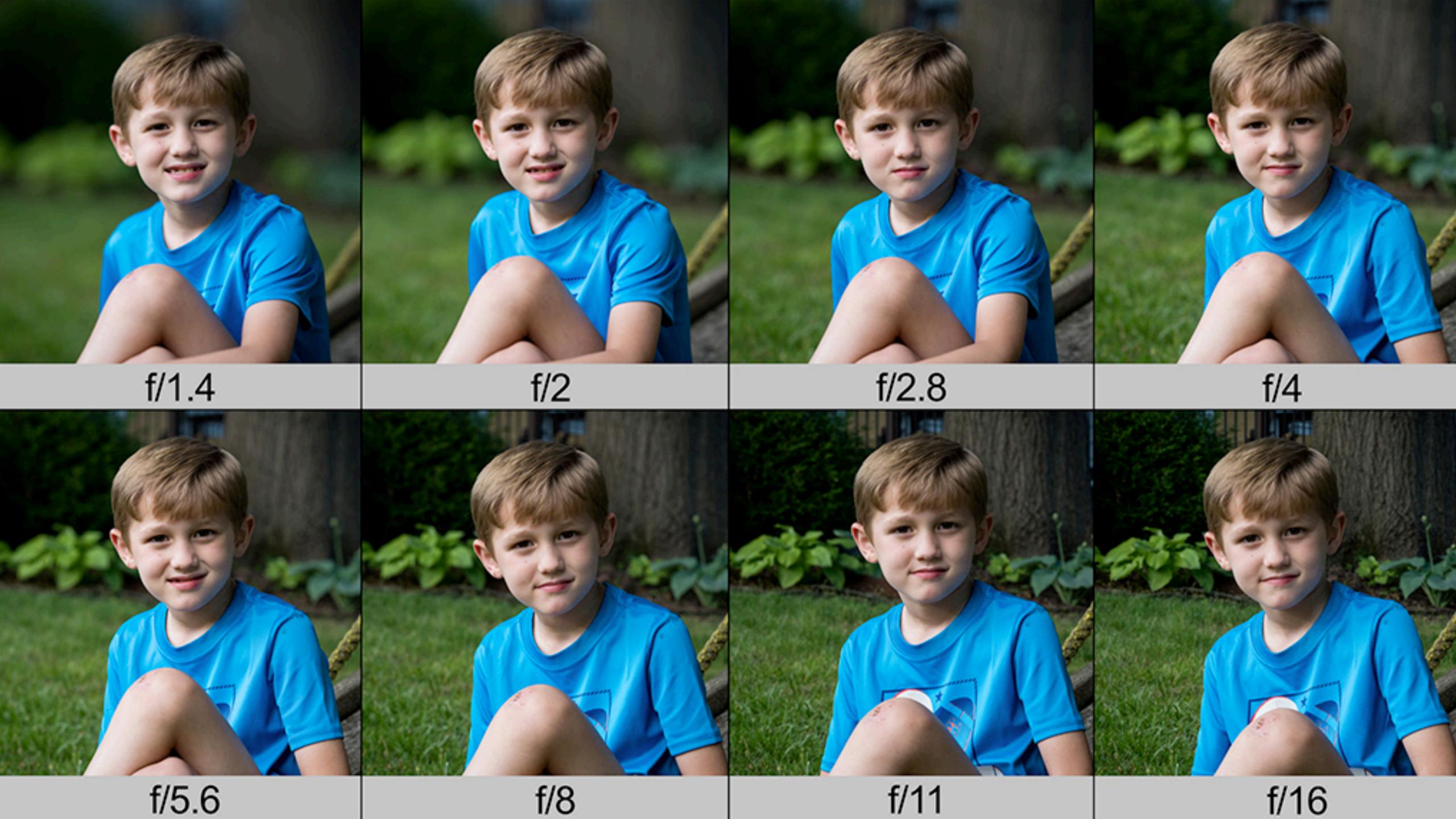


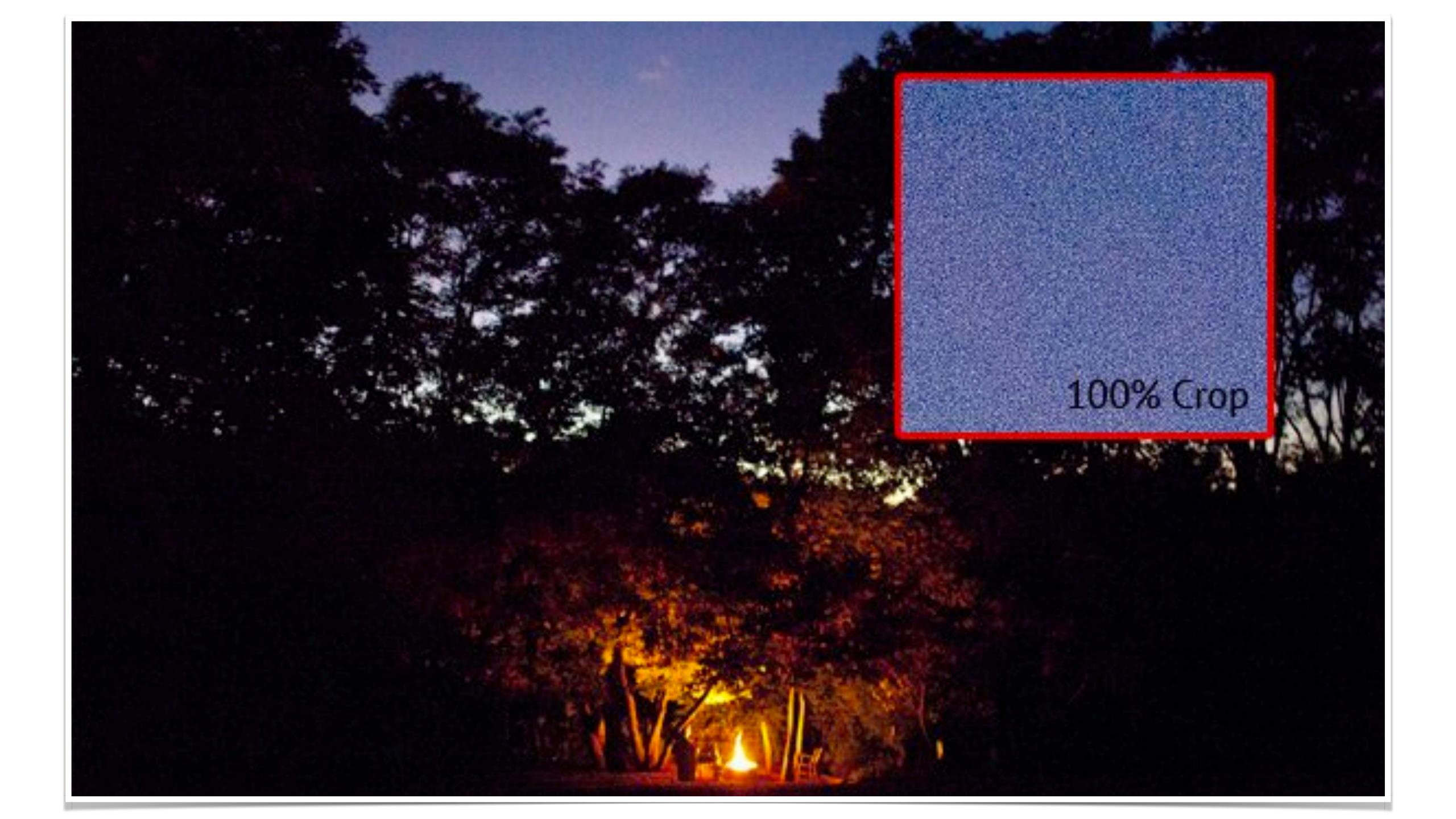


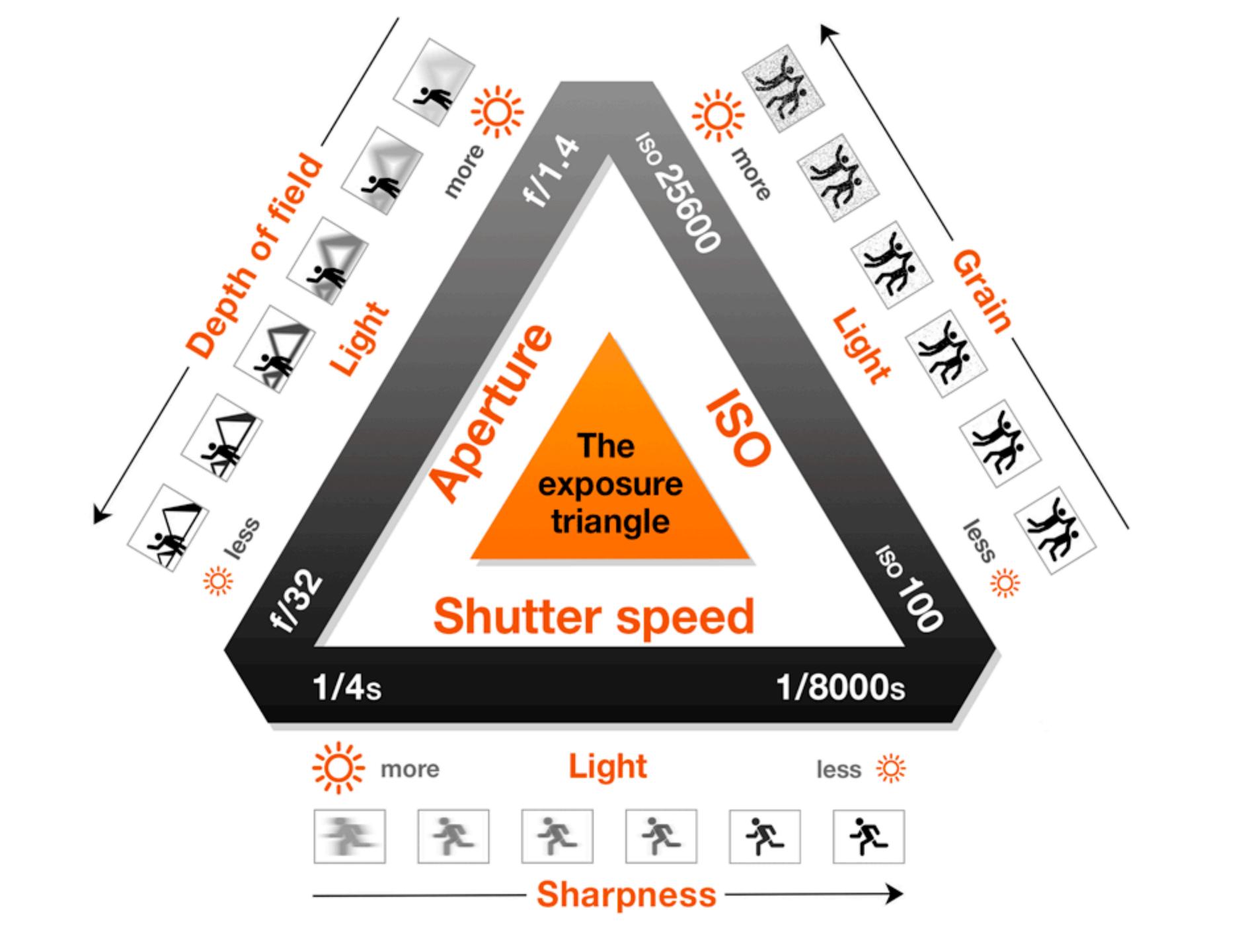




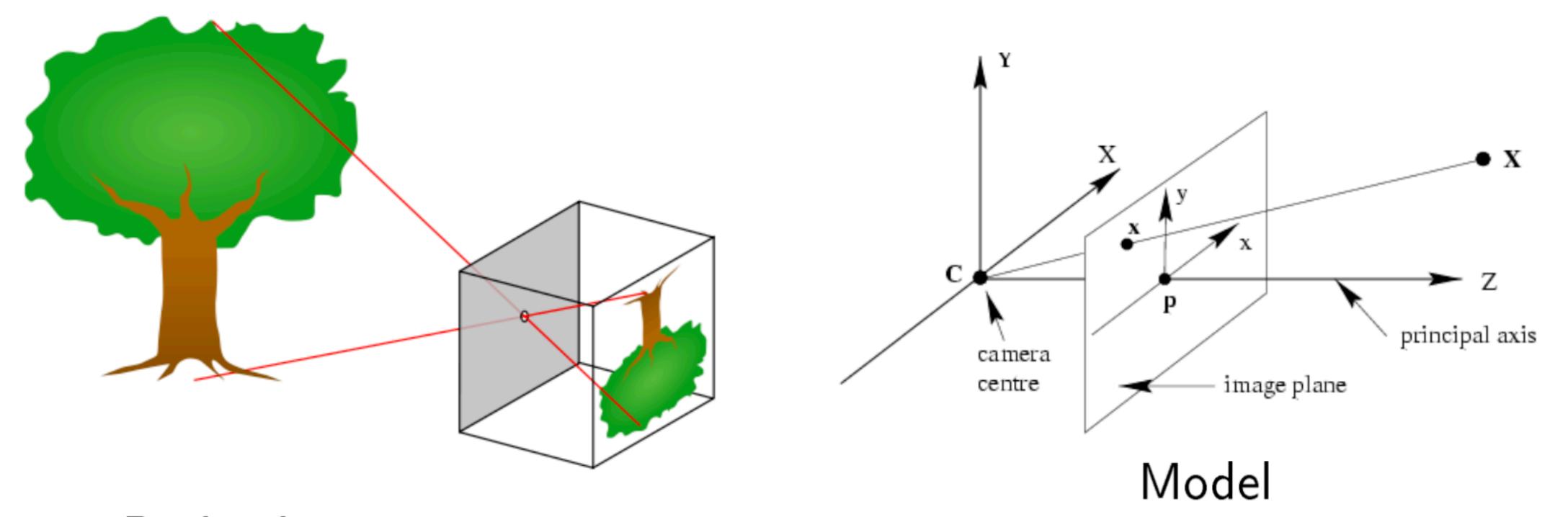








Como modelamos una cámara?



Projection (Source: Wikipedia)
The 'pinhole' camera (French: sténopé):

- Ideal model with an aperture reduced to a single point.
- No account for blur of out of focus objects, nor for the lens geometric distortion.

Central projection in camera coordinate frame

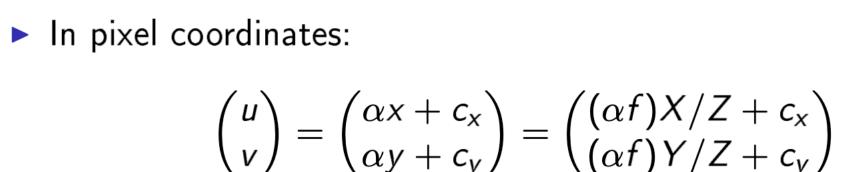
- Rays from C are the same: $\vec{Cx} = \lambda \vec{CX}$
- ▶ In the camera coordinate frame *CXYZ*:

$$\begin{pmatrix} x \\ y \\ f \end{pmatrix} = \lambda \begin{pmatrix} X \\ Y \\ Z \end{pmatrix}$$

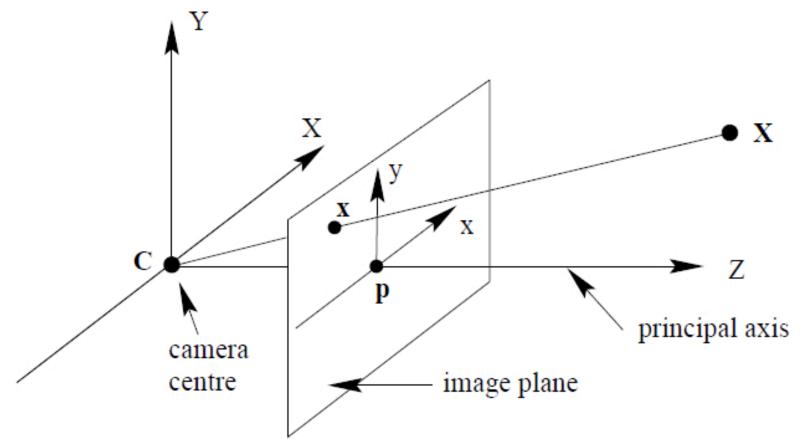
▶ Thus $\lambda = f/Z$ and

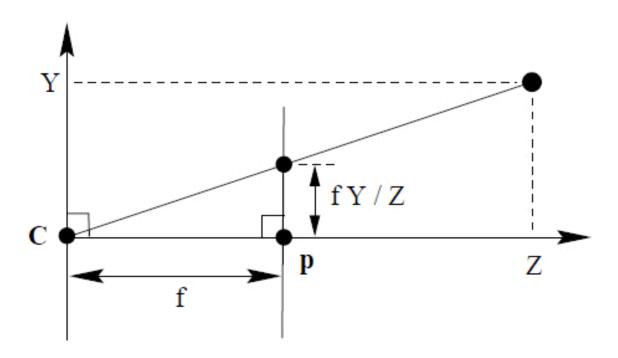
$$\begin{pmatrix} x \\ y \end{pmatrix} = f \begin{pmatrix} X/Z \\ Y/Z \end{pmatrix}$$





▶ αf : focal length *in pixels*, (c_x, c_y) : position of principal point P in pixels.





Calibration matrix

► Let us get back to the projection equation:

$$\begin{pmatrix} u \\ v \end{pmatrix} = \begin{pmatrix} fX/Z + c_x \\ fY/Z + c_y \end{pmatrix} = \frac{1}{Z} \begin{pmatrix} fX + c_x Z \\ fY + c_y Z \end{pmatrix}$$

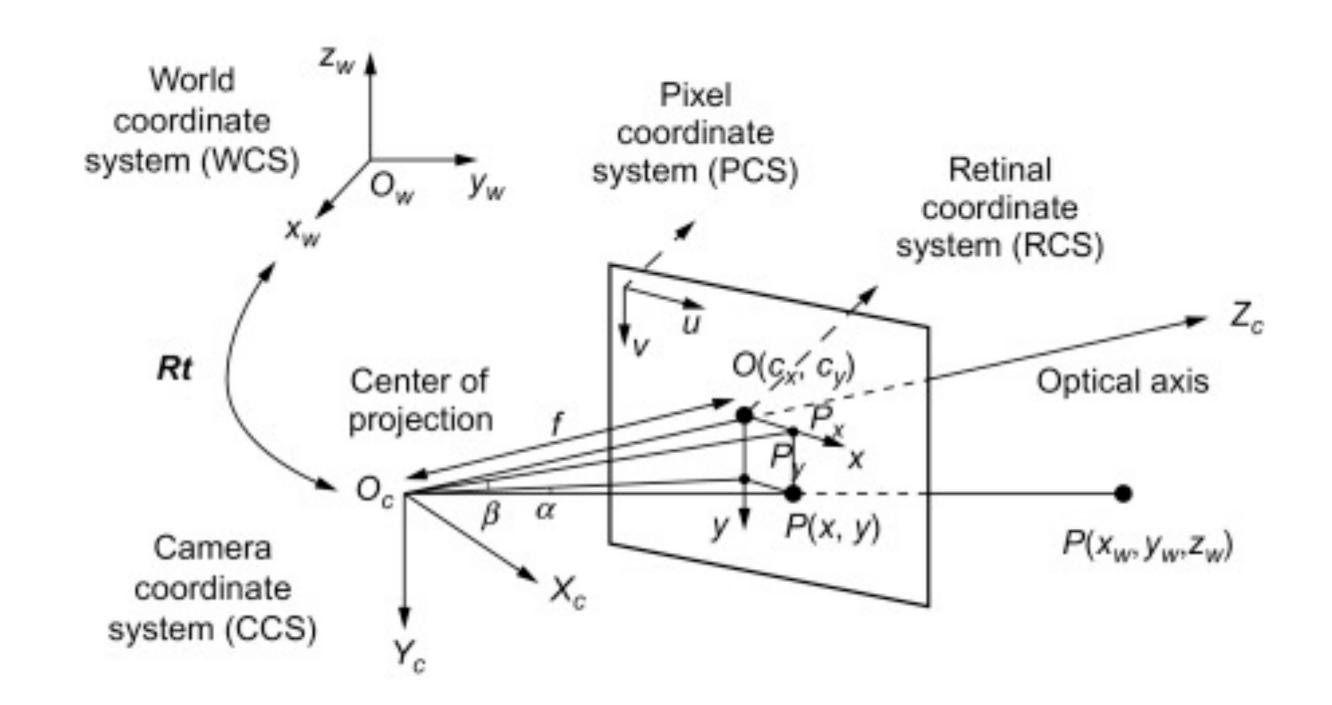
(replacing αf by f)

► We rewrite:

$$Z\begin{pmatrix} u \\ v \\ 1 \end{pmatrix} := x = \begin{pmatrix} f & c_x \\ f & c_y \\ 1 \end{pmatrix} \begin{pmatrix} X \\ Y \\ Z \end{pmatrix}$$

► The 3D point being expressed in another orthonormal coordinate frame:

$$x = \begin{pmatrix} f & c_x \\ f & c_y \\ 1 \end{pmatrix} \begin{pmatrix} R & T \end{pmatrix} \begin{pmatrix} X \\ Y \\ Z \\ 1 \end{pmatrix}$$



Calibration matrix

► Let us get back to the projection equation:

$$\begin{pmatrix} u \\ v \end{pmatrix} = \begin{pmatrix} fX/Z + c_x \\ fY/Z + c_y \end{pmatrix} = \frac{1}{Z} \begin{pmatrix} fX + c_x Z \\ fY + c_y Z \end{pmatrix}$$

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$$x = \begin{pmatrix} f & c_x \\ f & c_y \\ & 1 \end{pmatrix} \begin{pmatrix} R & T \end{pmatrix} \begin{pmatrix} X \\ Y \\ Z \\ 1 \end{pmatrix}$$

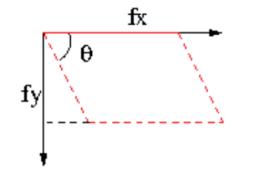
▶ The (internal) calibration matrix (3×3) is:

$$K = \begin{pmatrix} f & c_X \\ f & c_y \\ 1 \end{pmatrix}$$

▶ The projection matrix (3×4) is:

$$P = K (R T)$$

 \triangleright If pixels are trapezoids, we can generalize K:



$$K = \begin{pmatrix} f_X & s & c_X \\ & f_y & c_y \\ & & 1 \end{pmatrix} ext{ (with } s = -f_X \cot \theta ext{)}$$

Function Documentation

```
calibrateCamera() [1/2]
double cv::calibrateCamera ( InputArrayOfArrays
                                                objectPoints,
                           InputArrayOfArrays
                                                imagePoints,
                                                 imageSize,
                           Size
                           InputOutputArray
                                                 cameraMatrix,
                           InputOutputArray
                                                distCoeffs,
                           OutputArrayOfArrays rvecs,
                           OutputArrayOfArrays tvecs,
                           OutputArray
                                                 stdDeviationsIntrinsics,
                           OutputArray
                                                 stdDeviationsExtrinsics,
                           OutputArray
                                                perViewErrors,
                                                 flags = 0,
                           TermCriteria
                                                criteria = TermCriteria(TermCriteria::COUNT+TermCriteria::EPS, 30, DBL_EPSILON)
Python:
                           objectPoints, imagePoints, imageSize, cameraMatrix, distCoeffs[, rvecs[, tvecs[, flags[, criteria]]]]
cv.calibrateCamera(
```

Parameters

objectPoints

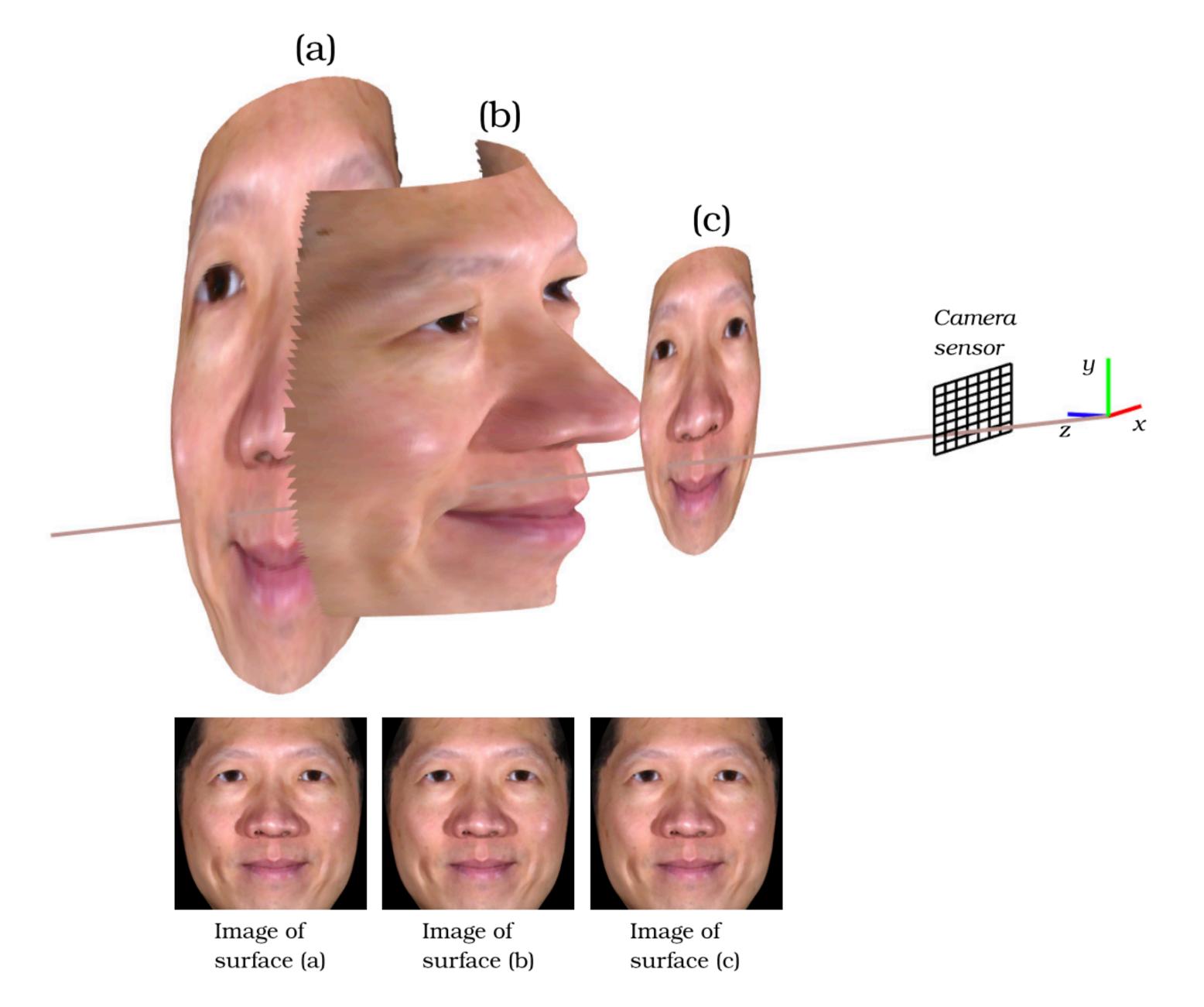
imagePoints

imageSize cameraMatrix

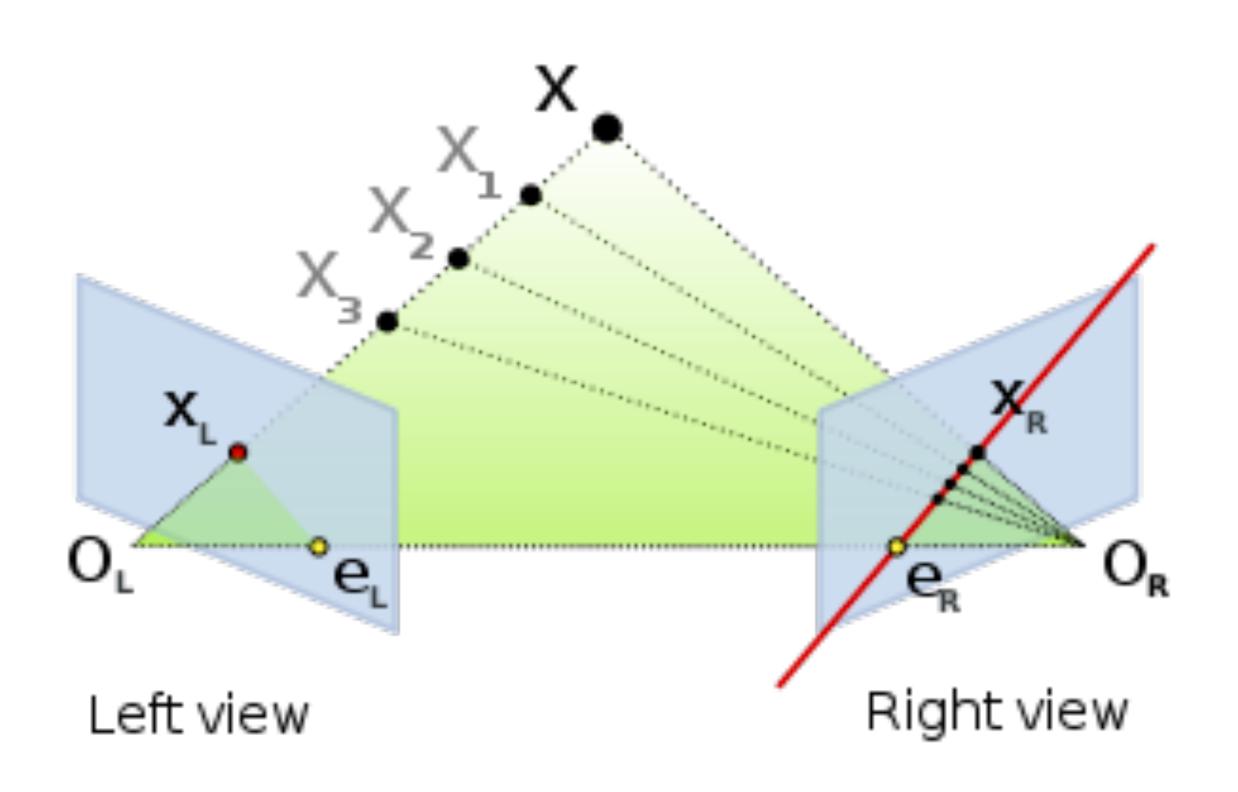
In the new interface it is a vector of vectors of calibration pattern points in the many elements as the number of pattern views. If the same calibration pattern partially occluded patterns or even different patterns in different views. Then plane (thus 0 in the Z-coordinate), if the used calibration pattern is a planar relation in the new interface it is a vector of vectors of the projections of calibration pattern is a planar relation pattern is a vector of vectors of the projections of calibration pattern is a planar relation pattern is a vector of vectors of the projections of calibration pattern is a vector of vectors of the projections of calibration pattern is a vector of vectors of the projections of calibration pattern is a vector of vectors of the projections of calibration pattern is a vector of vectors of the projections of calibration pattern is a vector of vectors of the projections of calibration pattern is a vector of vectors of the projections of calibration pattern is a vector of vectors of the projections of calibration pattern is a vector of vectors of the projections of calibration pattern is a vector of vectors of the projections of calibration pattern is a vector of vectors of the projections of calibration pattern is a vector of vectors of the projections of calibration pattern is a vector of vectors of the projections of calibration pattern is a vector of vectors of the projections of calibration pattern is a vector of vectors of the projections of calibration pattern is a vector of vectors of the projections of calibration pattern is a vector of vectors of the projections of calibration pattern is a vector of vectors of the projections of calibration pattern is a vector of vectors of the vector of vectors of vecto

Input/output 3x3 floating-point camera intrinsic metrix $A = \begin{bmatrix} J_x & 0 & c_x \\ 0 & f_y & c_y \\ 0 & 0 & 1 \end{bmatrix}$

Cómo podemos extraer información 3D usando cámaras?

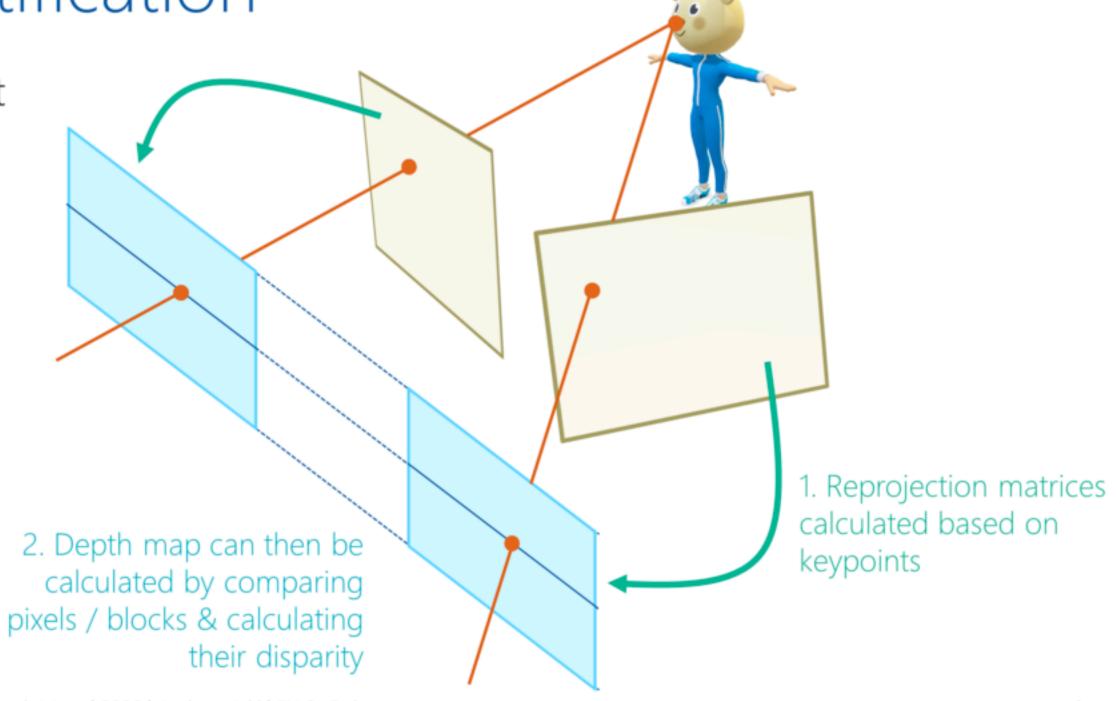


[1] Di Martino, J. Matias, Qiang Qiu, and Guillermo Sapiro. "Rethinking shape from shading for spoofing detection." IEEE Transactions on Image Processing 30 (2020): 1086-1099.

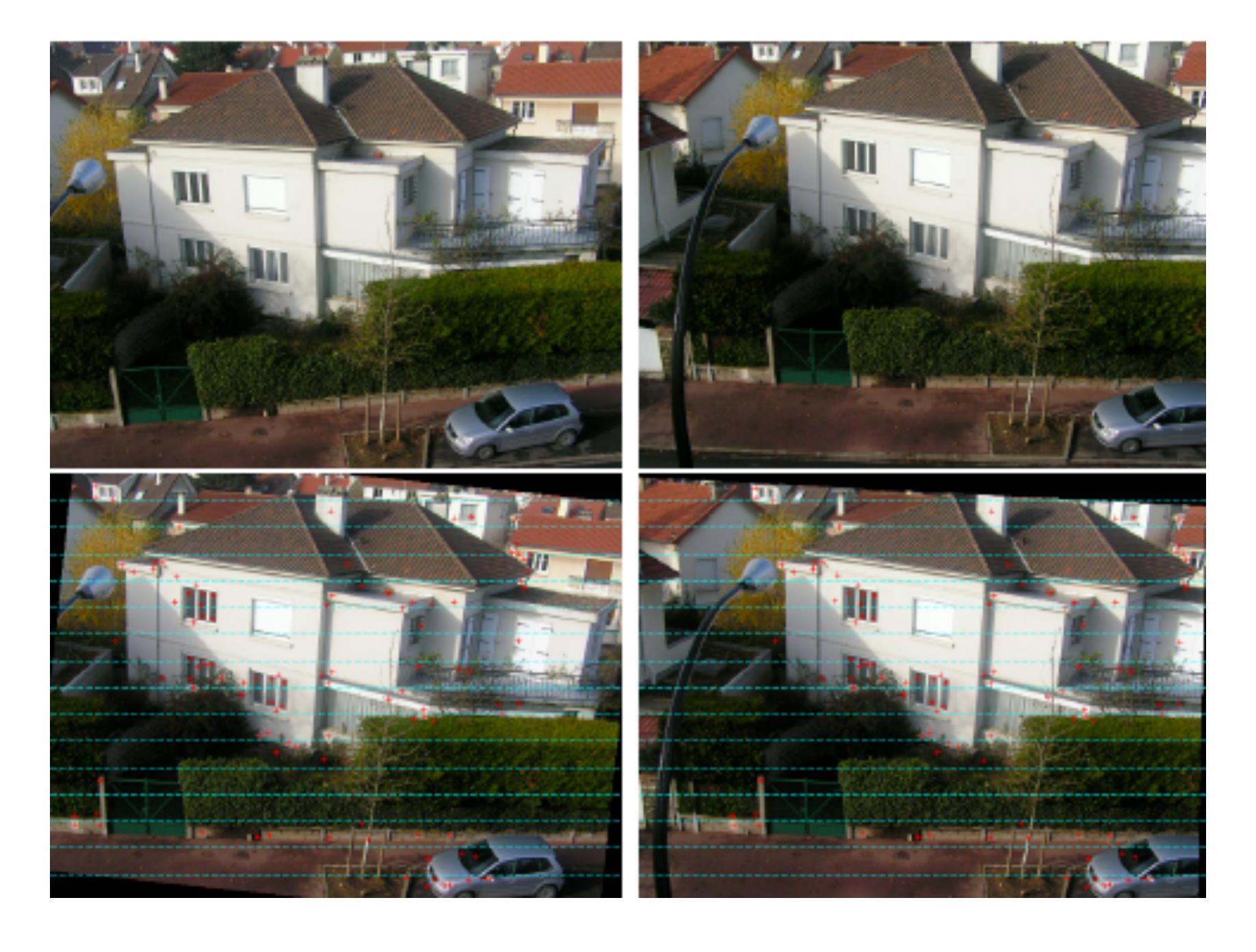


Stereo Rectification

Reproject left & right image planes onto a common plane parallel to the line between camera centers

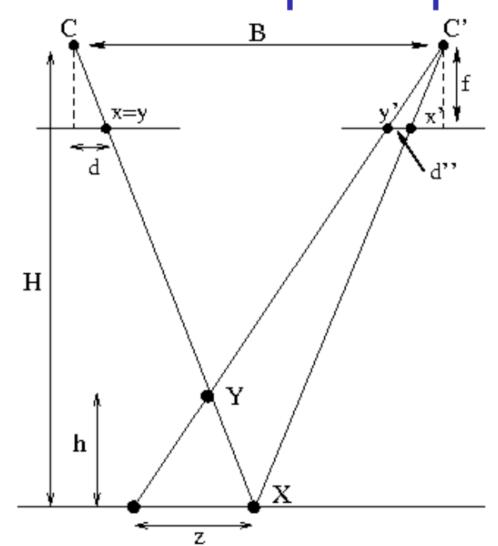


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Triangulation

Fundamental principle of stereo vision



$$h \simeq \frac{z}{B/H}, \quad z = d'' \frac{H}{f}.$$

f focal length.

H distance optical center-ground.

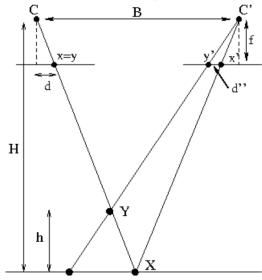
B distance between optical centers (baseline).

Goal

Given two rectified images, point correspondences and computation of their apparent shift (disparity) gives information about relative depth of the scene.

Triangulation

Fundamental principle of stereo vision



$$h \simeq \frac{z}{B/H}, \quad z = d'' \frac{H}{f}.$$

f focaÍ length.

H distance optical center-ground.B distance between optical centers (baseline).

Goal

Given two rectified images, point correspondences and computation of their apparent shift (disparity) gives information about relative depth of the scene.

Let us write again the binocular formulae:

$$\lambda x = K(RX + T)$$
 $\lambda' x' = K'X$

▶ Write $Y^T = \begin{pmatrix} X^T & \lambda & \lambda' \end{pmatrix}$:

$$\begin{pmatrix} KR & -x & 0_3 \\ K' & 0_3 & -x' \end{pmatrix} Y = \begin{pmatrix} KT \\ 0_3 \end{pmatrix}$$

(6 equations ↔ 5 unknowns + 1 epipolar constraint)

- ▶ We can then recover X.
- ightharpoonup Special case: R = Id, $T = Be_1$
- ► We get:

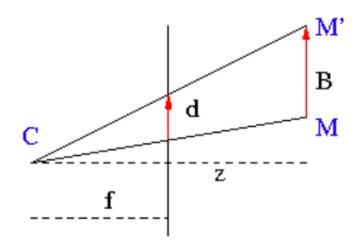
$$z(x - KK^{'-1}x') = \begin{pmatrix} Bf & 0 & 0 \end{pmatrix}^T$$

▶ If also K = K',

$$z = fB/[(x - x') \cdot e_1] = fB/d$$

d is the disparity

Disparity map



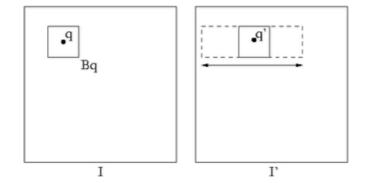
$$z = \frac{fE}{d}$$

Depth z is inversely proportional to disparity d (apparent motion, in pixels).

- Disparity map: At each pixel, its apparent motion between left and right images.
- We already know disparity at feature points, this gives an idea about min and max motion, which makes the search for matching points less ambiguous and faster.

Local search

At each pixel, we consider a context window and we look for the motion of this window.



Distance between windows:

$$d(q) = \arg\min_{d} \sum_{p \in F} (I(q+p) - I'(q+de_1+p))^2$$

- Variants to be more robust to illumination changes:
 - 1. Translate intensities by the mean over the window.

$$I(q+p) \rightarrow I(q+p) - \sum_{r \in F} I(q+r) / \#F$$

2. Normalize by mean and variance over window.

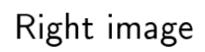


Right image



Left image

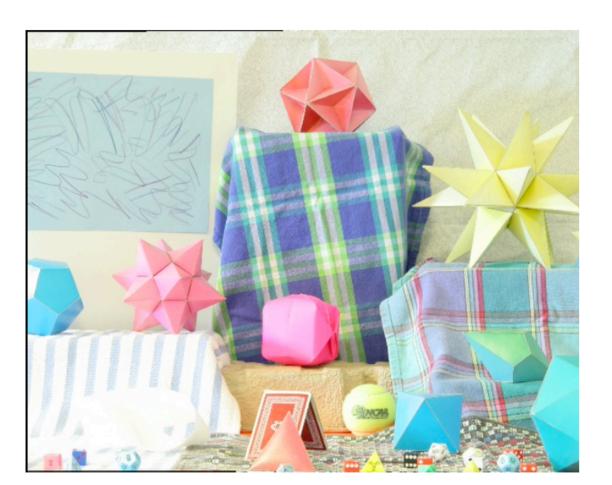


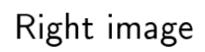


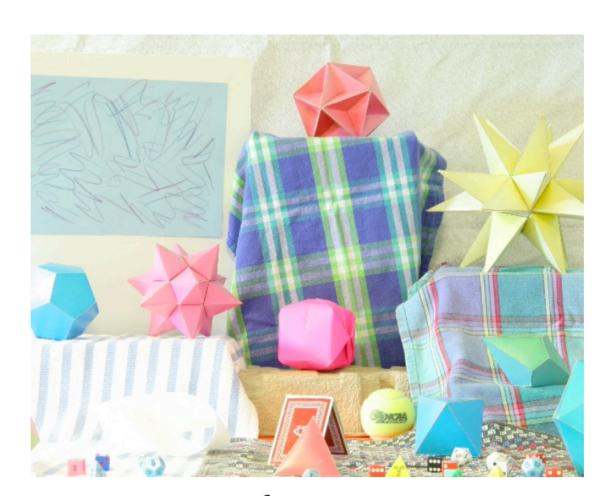


Left image









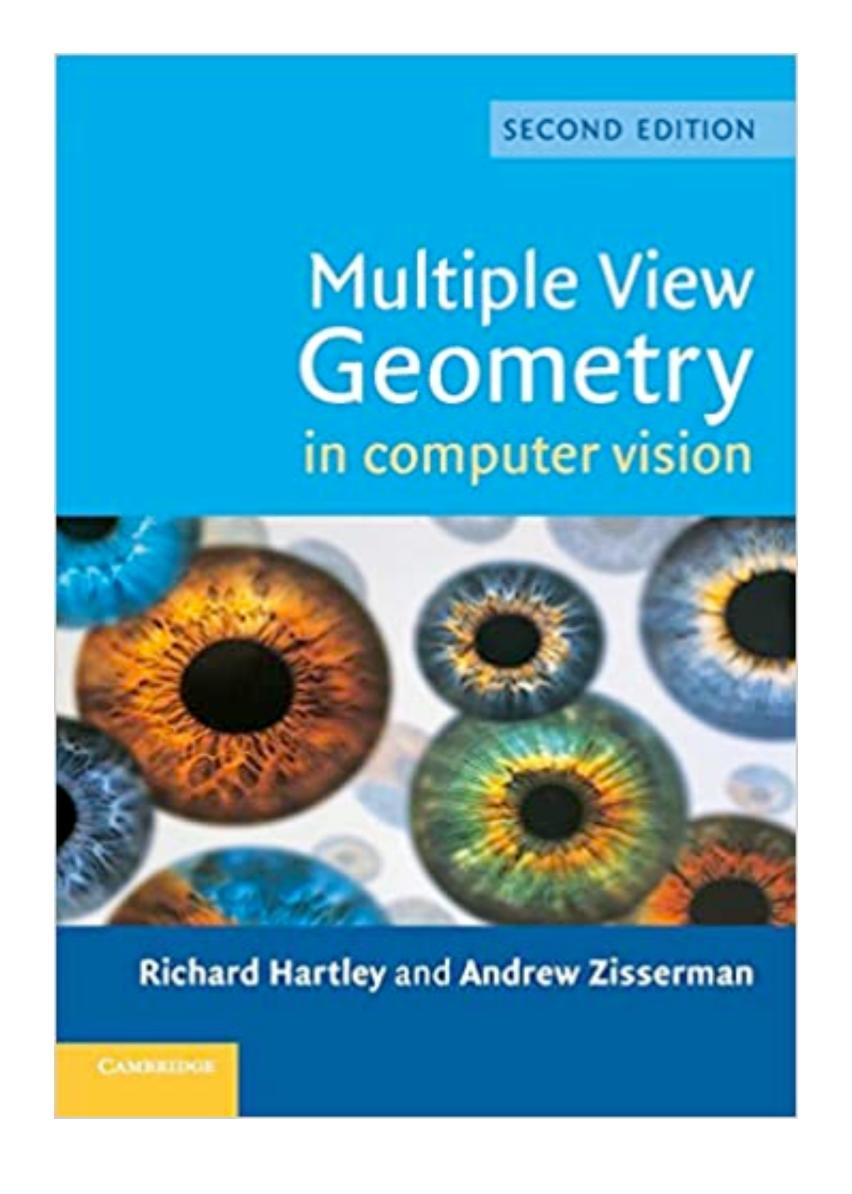
Left image





Resumiendo

- Modela una cámara y cuales son los parámetros más críticos.
- Pinhole model, matrix de proyección, parámetros intrínsecos y extrínsecos.
- Calibración de una cámara.
- Limites de vision monocular.
- Vision stereo puede usarse para obtener información 3D.
- Geometria epipolar.
- Disparidad entre imágenes epistolares contiene información de la profundidad.
- Desafíos asociados con la estimation de correspondencias (crucial para la calibración y para la estimación de correspondencias.





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Pascal Monasse

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https://doi.org/10.5201/ipol.2011.m_qer

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Communicated by Luis Álvarez Demo edited by Agustín Salgado

Abstract

The standard setup in reconstructing the three-dimensional geometry of a scene from a pair of stereo images is to have them rectified, in which case the apparent motion of points is horizontal. With pinhole cameras, it is always possible to find two homographies that rectify the images. The method of Fusiello and Irsara assumes that both cameras are the same with principal point at the center, but keeps the focal length as an unknown. The virtual rotations of the two cameras are then evaluated to minimize the vertical motion of points.

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 An Analysis and Implementation of the Harris Corner **Detector**

2018-10-03 · Javier Sánchez, Nelson Monzón, Agustín Salgado

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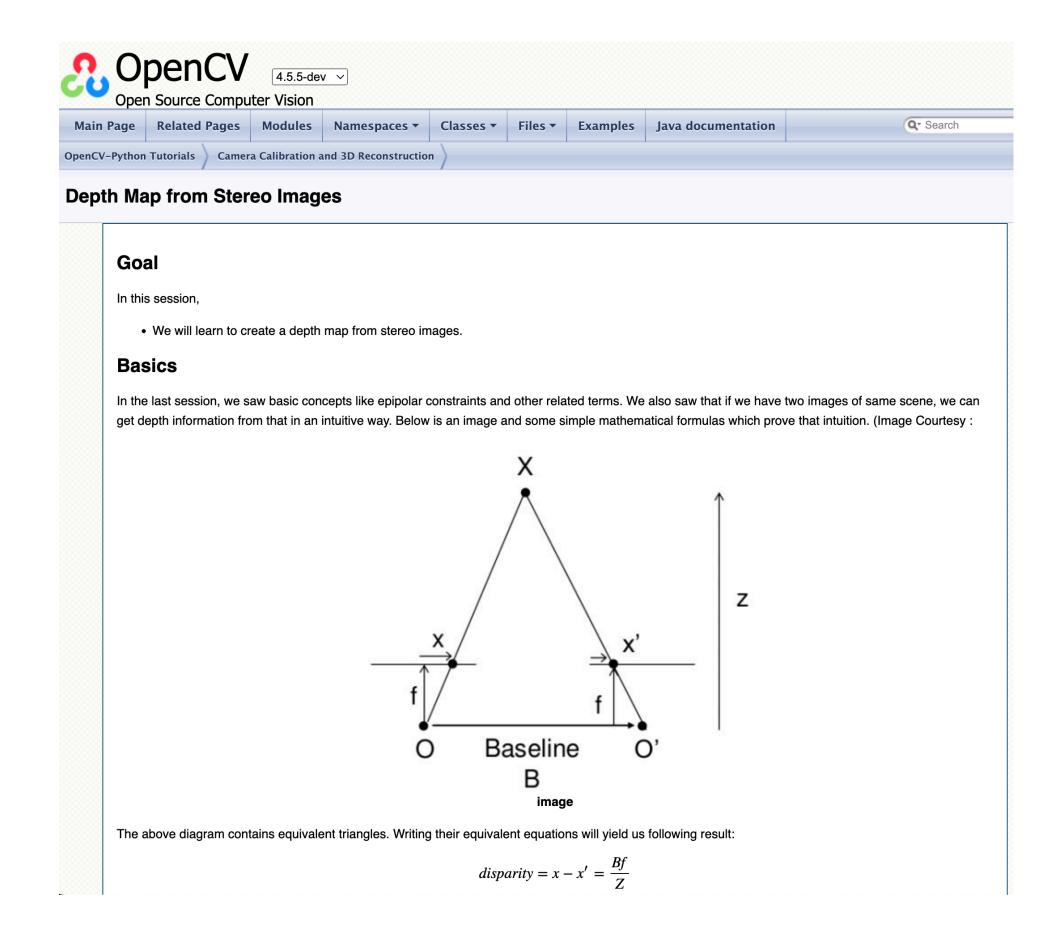
 An Unsupervised Algorithm for Detecting Good Continuation in Dot Patterns

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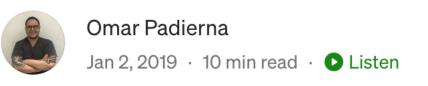
- Generation and Detection of Alignments in Gabor Patterns 2016-11-18 · Samy Blusseau, Rafael Grompone von Gioi
- An Unsupervised Point Alignment Detection Algorithm 2015-12-15 · José Lezama, Gregory Randall, Jean-Michel Morel, Rafael Grompone von Gioi
- Adaptive Anisotropic Morphological Filtering Based on Co-**Circularity of Local Orientations** PREPRINT · Samy Blusseau, Santiago Velasco-Forero, Jesús Angulo,
- Ant Colony Optimization for Estimating Pith Position on **Images of Tree Log Ends** PREPRINT Remi Decelle, Phuc Ngo, Isabelle Debled-Rennesson, Frédéric Mothe, Fleur Longuetaud
- ⇒ Edge and Contour Detection
- Segmentation
- → Texture

Isabelle Bloch











Tutorial: Stereo 3D reconstruction with OpenCV using an iPhone camera. Part III.

Welcome to the third and final part of this <u>3 part tutorial</u> on stereo reconstruction.

A quick recap:



During the <u>first part</u> we covered a brief mention on the steps required for stereo 3D reconstruction and the gist of how stereo reconstruction works.

Muchas gracias, Preguntas?