

# Sistemas de compensación de transformadores de medida y protección

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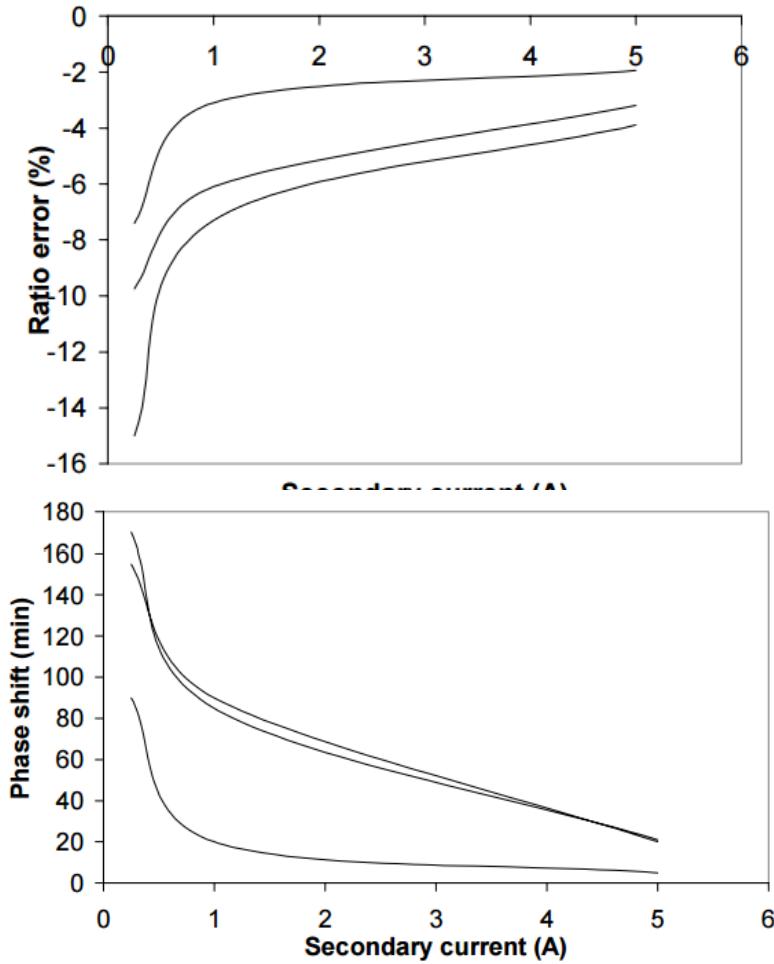
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# Compensación pasiva de CT



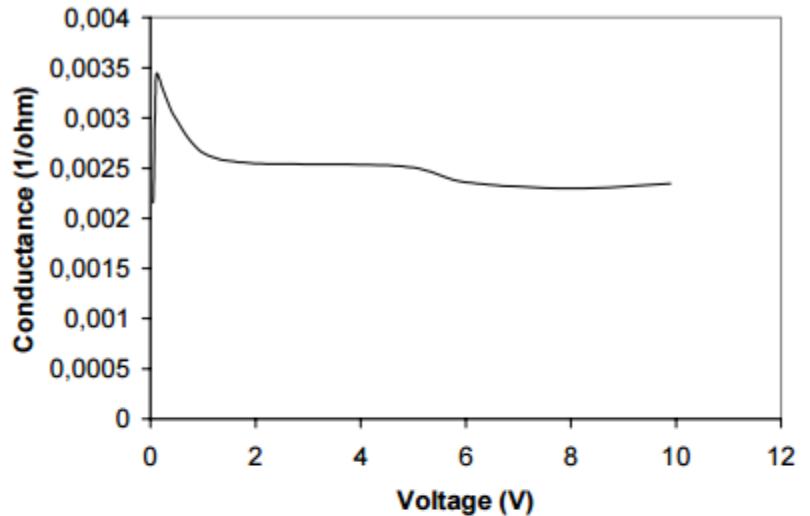
150 A/5 A.



Cargas: 0 VA (curva inferior), 7.5 VA (curva central) y 15 VA (curva superior).

- **Compensación de errores en transformadores de corriente usados en redes de alta tensión**, ALEJANDRO SANTOS , DANIEL SLOMOVITZ, IEEE Revista Latinoamericana, v.: 4 3 , p.:21 - 25, 2006, ISSN: 15480992

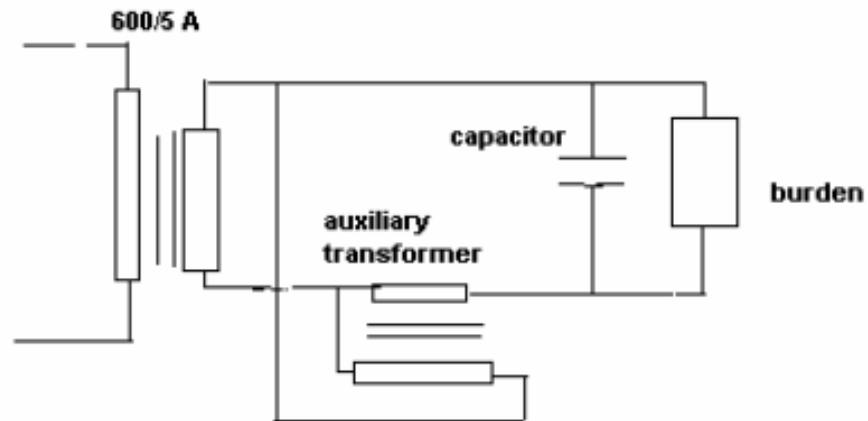
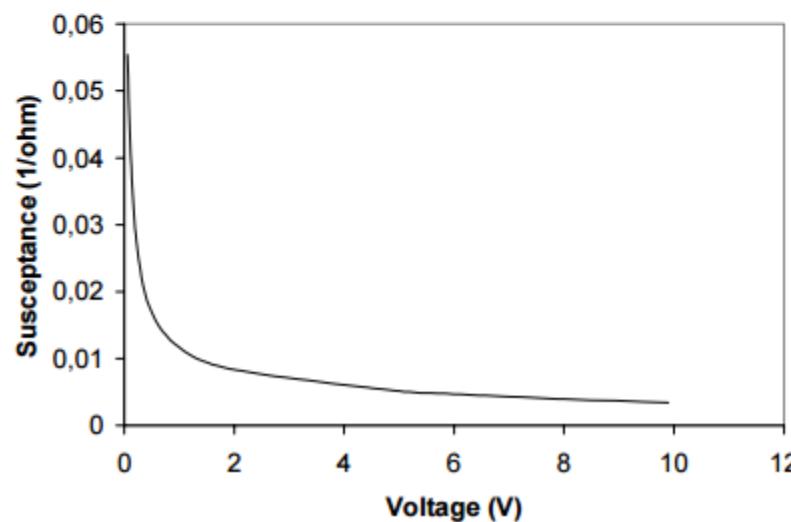
# Compensación pasiva de CT



Impedancia magnetizante

Rm: 300 a 400 ohm  
Xm: 20 a 100 ohm

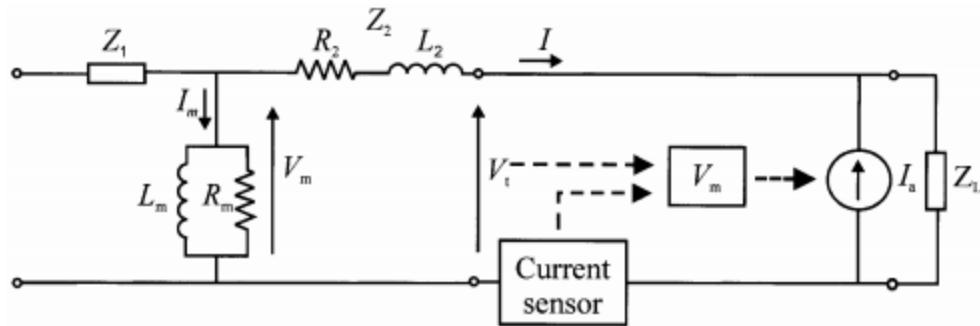
Compensación : C=15 uF



# Compensación pasiva de CT

Ratio Burden (VA)	Current (% of IN)	Ratio error (%)	Phase shift (min)
150/5	5	-15	155
	20	-7	90
	100	-4	20
	120	-4	10
600/5	5	-1,6	45
	20	-1	22
	100	-0,6	7
600/5 Compensado	5	-0,2	16
	20	0	9
	100	0,1	9
	120	0,1	6

# Compensación CTs en servicio



$$I_m = \frac{V_m}{R_m} + \frac{V_m}{j\omega L_m}$$

$$V_m = V_t + R_2 I + j\omega L_2 I$$

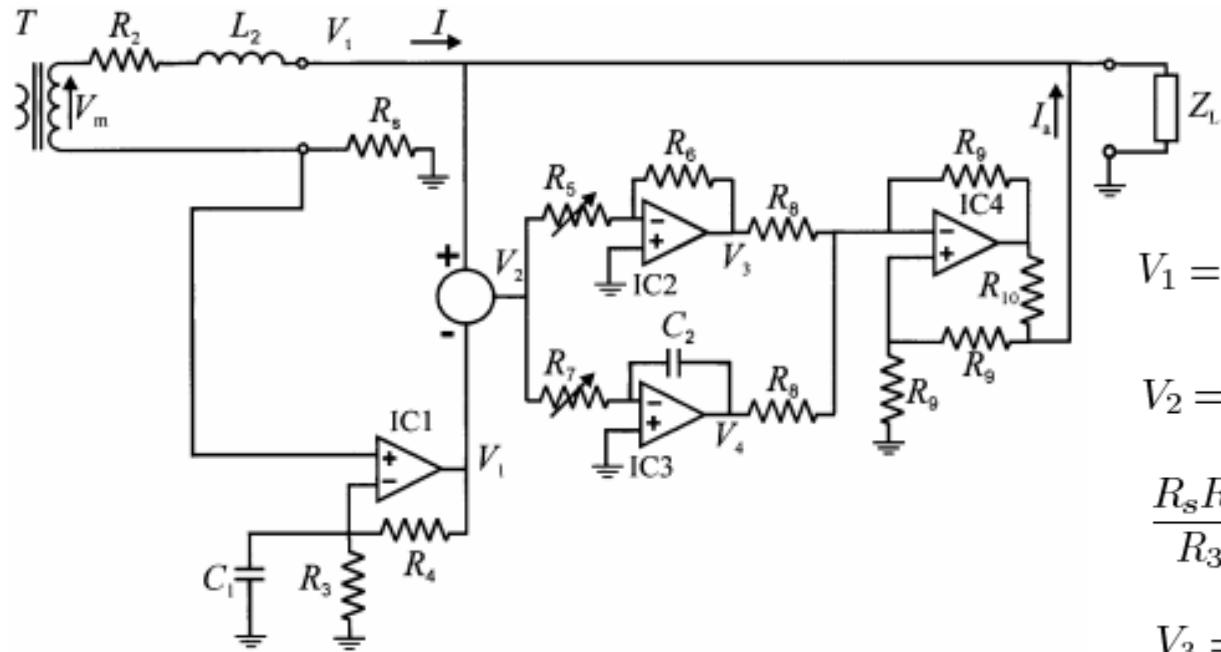
$$I_m = V_t \left( \frac{1}{R_m} - \frac{j}{\omega L_m} \right) + I \left[ \frac{R_2}{R_m} + \frac{L_2}{L_m} + j \left( \frac{\omega L_2}{R_m} - \frac{R_2}{\omega L_m} \right) \right]$$

$$I_a = V_t \left( \frac{1}{k_3} - \frac{j}{\omega k_4} \right) + I \left[ \frac{k_1}{k_3} + \frac{k_2}{k_4} + j \left( \frac{\omega k_2}{k_3} - \frac{k_1}{\omega k_4} \right) \right]$$

The compensation is automatically achieved if the constants  $k_i$  of the electronic control are selected as follows:  $k_1$  is imposed to be equal to  $R_2$ ,  $k_2$  to  $L_2$ ,  $k_3$  to  $R_m$ , and  $k_4$  to  $L_m$ . In this way, the current  $I_a$  (amplitude and phase) is equal to the current  $I_m$ ,

- **Electronic system for increasing the accuracy of in-service instrument-current transformers**, DANIEL SLOMOVITZ, IEEE Transactions on Instrumentation and Measurement, v.: 52 2 , p.:408 - 410, 2003, ISSN: 00189456

# Compensación CTs en servicio



$$V_1 = -R_s \left( 1 + \frac{R_4}{R_3} \right) I - j\omega R_s R_4 C_1 I$$

$$V_2 = V_t + R_s \left( 1 + \frac{R_4}{R_3} \right) I + j\omega R_s R_4 C_1 I.$$

$$\frac{R_s R_4}{R_3} = R_2 \quad R_s R_4 C_1 = L_2$$

$$V_3 = -V_m \frac{R_6}{R_5}$$

$$V_4 = V_m \frac{j}{\omega R_7 C_2}$$

$$I_a = \frac{-V_3 - V_4}{2R_{10}}$$

$$\frac{2R_5 R_{10}}{R_6} = R_m$$

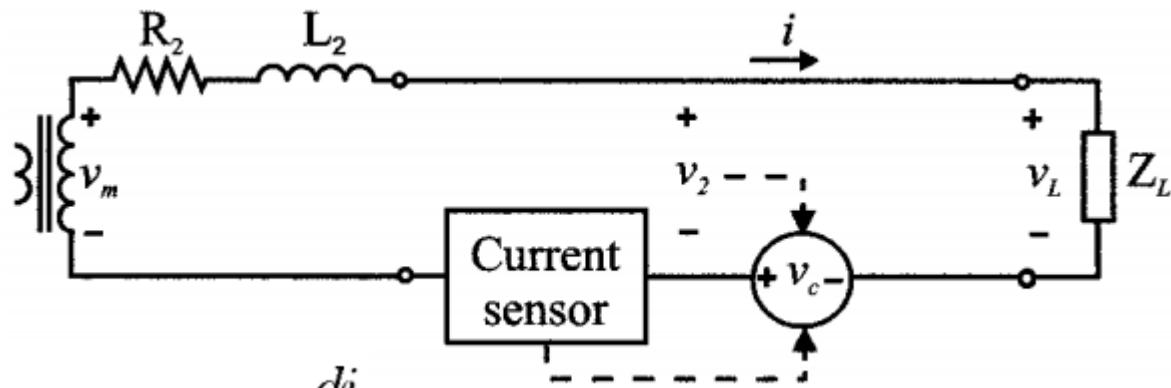
$$2R_7 R_{10} C_2 = L_m$$

# Compensación CTs en servicio

TRANSFORMER ERRORS WITH (COLUMN 3) AND WITHOUT (COLUMN 4)  
THE COMPENSATING CIRCUIT

Current (A)	Burden (Ω)	Error (compensated)		Error (original)	
		%	crad	%	crad
75	0.3	0.010	0.010	-0.11	0.16
500	0.3	0.005	0.008	-0.08	0.11
1800	0.3	0.002	-0.005	-0.07	0.08
75	1.2	0.010	-0.002	-0.21	0.33
500	1.2	-0.022	0.025	-0.17	0.22
1800	1.2	-0.008	0.010	-0.17	0.12

# Compensación pinzas de corriente

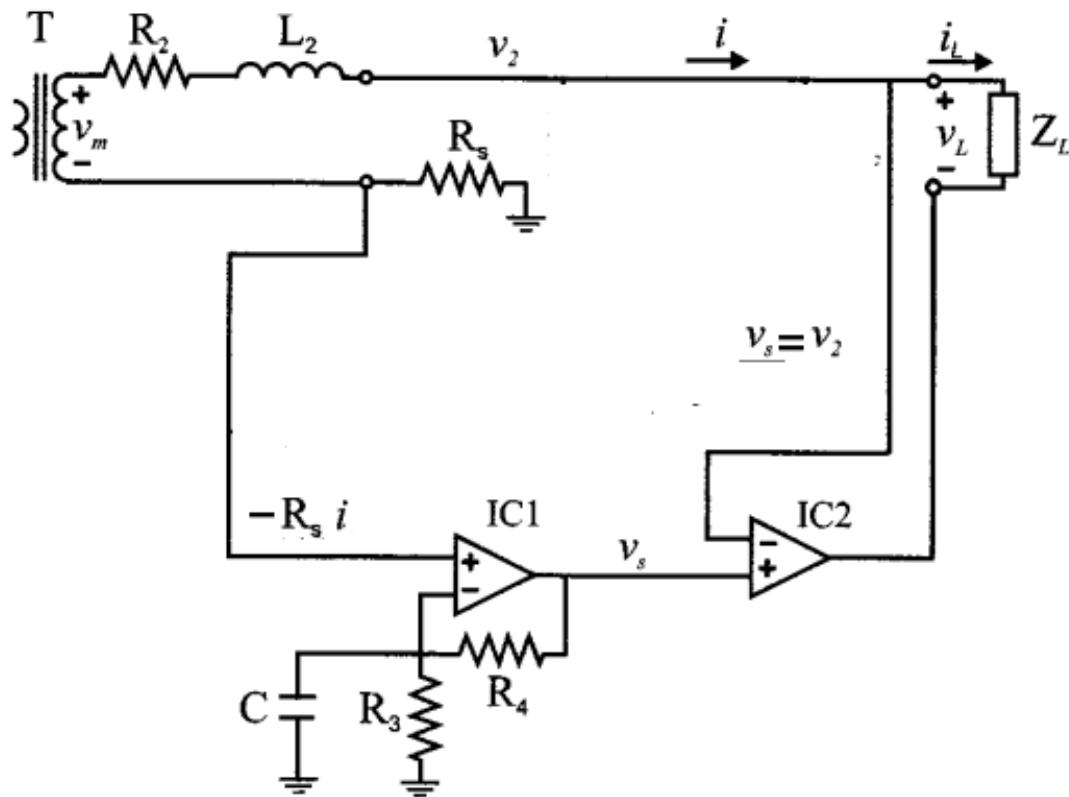


$$v_m = v_2 + R_2 i + L_2 \frac{di}{dt}$$

Si  $v_2 = k_1 i + k_2 \frac{di}{dt}$        $v_m = k_1 i + k_2 \frac{di}{dt} + R_2 i + L_2 \frac{di}{dt}$

Para  $v_m=0$ ,  $k_1=-R_2$ ,  $k_2=-L_2$

# Compensación pinzas de corriente

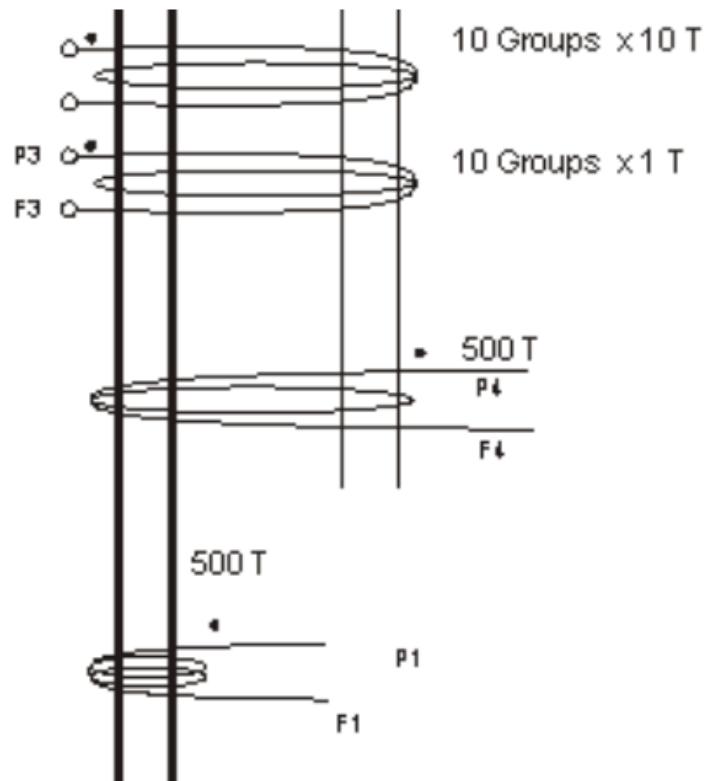


$$v_s = -R_s \left( 1 + \frac{R_4}{R_3} \right) i - R_s R_4 C \frac{di}{dt}$$

$$v_m = R_2 i + L_2 \frac{di}{dt} + v_2 + R_s i$$

$$v_m = \left( R_2 - \frac{R_s R_4}{R_3} \right) i + (L_2 - R_s R_4 C) \frac{di}{dt}$$

# CT doble etapa



- Two-Stage Current Transformer with Electronic Compensation, DANIEL SLOMOVITZ , LEONARDO TRIGO , CARLOS FAVERIO Acta Imeco, v.: 1 1 , p.:85 - 88, 2012

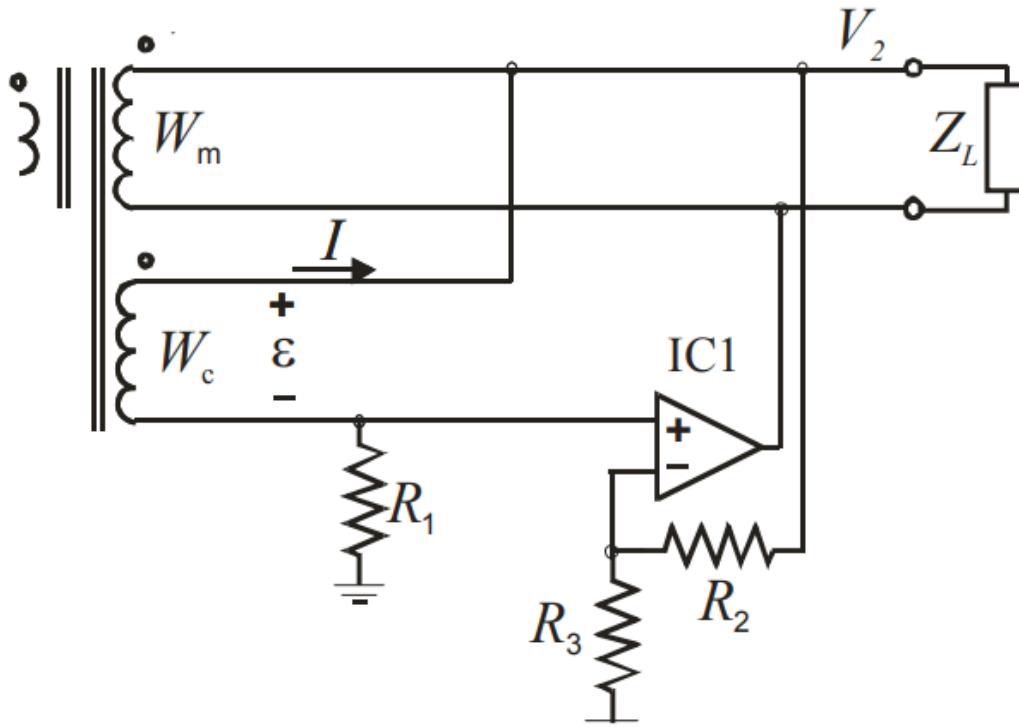
# CT doble etapa

Table 1. Available ratios using different series-parallel connections.

Parallel groups	Groups	Turn/Group	Ratio	Input Current (A)
1	10	10	5	1
2	5	10	10	2
5	2	10	25	5
10	1	10	50	10
1	10	1	50	10
2	5	1	100	20
5	2	1	250	50
10	1	1	500	100

Secundario: 0.2 A, 10 ohm

# CT doble etapa



$$\varepsilon = I(r + R_1) + V_2$$

$$V_2 = -R_1 I \left( 1 + \frac{R_2}{R_3} \right)$$

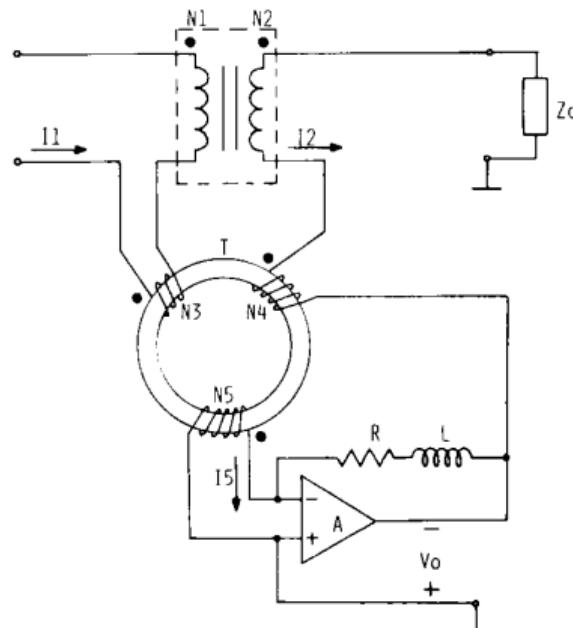
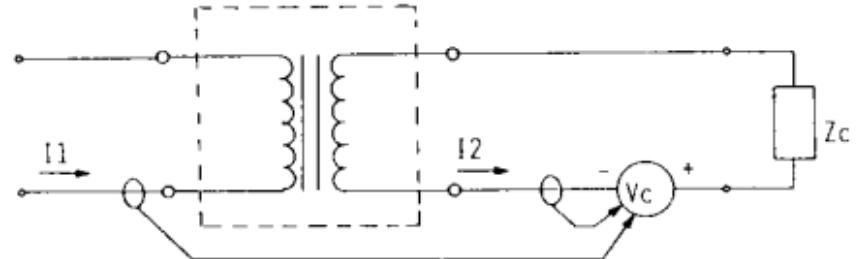
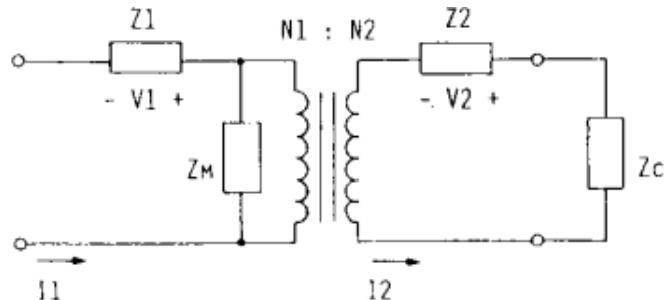
$$\varepsilon = I \left( r - \frac{R_1 R_2}{R_3} \right).$$

If  $r = R_1 R_2 / R_3$ , then  $\varepsilon = 0$ .

Table 2. Calibration of the proposed transformer.

Ratio	Primary current (A)	Error in phase $\times 10^{-6}$	Error in quadrature $\times 10^{-6}$
10	2	-0.6	-0.8
5	1	-0.4	-0.6

# Compensación de VTs



$$R = R_t \cdot (N_5/N_3)/(N_2/N_1 + N_4/N_3)$$

$$L = L_t \cdot (N_5/N_3)/(N_2/N_1 + N_4/N_3)$$

# Compensación de VTs

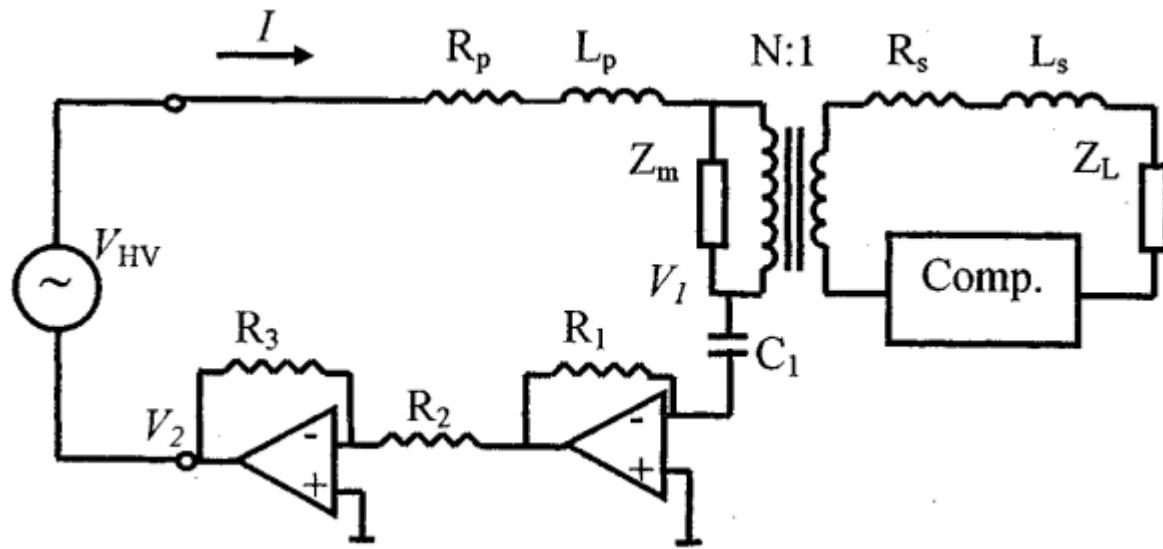
TRANSFORMER ERRORS WITHOUT COMPENSATION

LOAD	INPUT VOLTAGE (V)	RATIO ERROR (%)	PHASE DISPLACEMENT (absolute) (minute)
10VA @ Vn cos phi=0.8	60	-0.56	10
	100	-0.57	11
	130	-0.57	11
	150	-0.61	14

TRANSFORMER ERRORS WITH THE PROPOSED COMPENSATION

LOAD	INPUT VOLTAGE (V)	RATIO ERROR (%)	PHASE DISPLACEMENT (absolute) (minute)
10VA @ Vn cos phi=0.8	60	0.00	0.3
	100	0.00	0.4
	130	0.00	0.5
	150	-0.01	0.7

# Compensación VTs



$$V_1 - V_2 = \left( -\frac{R_1 R_3}{R_2} - j \frac{1}{\omega C} \right) I$$

$$R_p = R_1 R_3 / R_2, \quad \omega L = 1 / (\omega C)$$

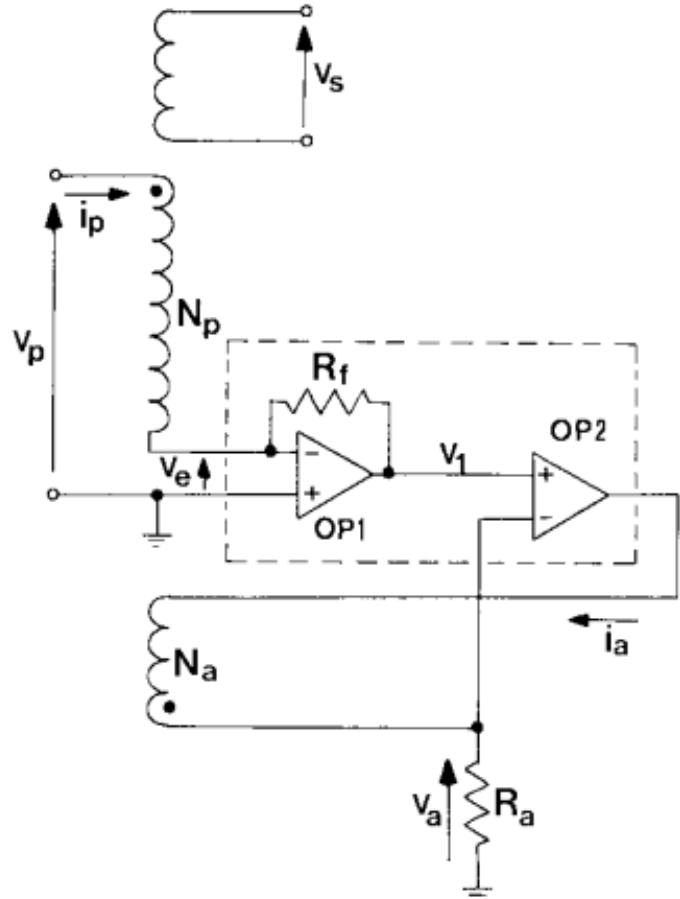
- **Electronic based high-voltage measuring transformers**, DANIEL SLOMOVITZ, IEEE Transactions on Power Delivery, v.: 17 2 , p.:359 - 361, 2002, ISSN: 08858977

# Compensación VTs

30 kV/100 V, 15 VA, class 0.1

CONDITIONS		WITHOUT COMPENSATION		WITH COMPENSATION	
Voltage (kV)	Load (VA)	Ratio Error ( $\mu$ V/V)	Phase ( $\mu$ rad)	Ratio Error ( $\mu$ V/V)	Phase ( $\mu$ rad)
12	0	1200	-520	-12	8
24	0	1260	-450	-1	-11
36	0	900	-270	15	-11
36	15	-240	-550	10	-20

# Reducción de corriente magnetizante en VT



$$i_a = -Ki_p \quad K = R_f/R_a$$

magnetomotive force,  $A$ , is

$$A \text{ (in ampere-turns)} = N_p i_p - N_a i_a$$

$$i_p = A/[N_p(1 + KN_a/N_p)]$$

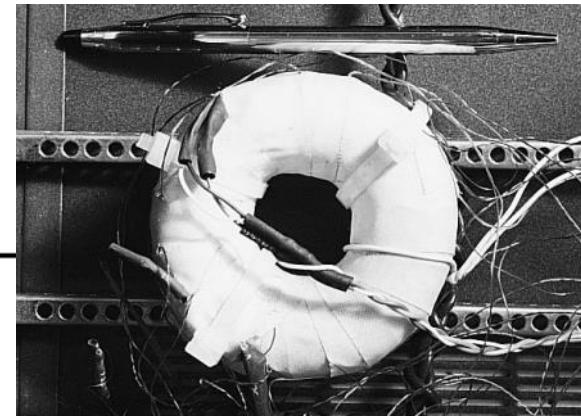
- **Electronic compensation of inductive voltage dividers and standard voltage transformers,**  
DANIEL SLOMOVITZ, IEEE Transactions on Instrumentation and Measurement, v.: 47 2 , p.:465  
- 468, 1999, ISSN: 00189456

# Reducción de corriente magnetizante en VT

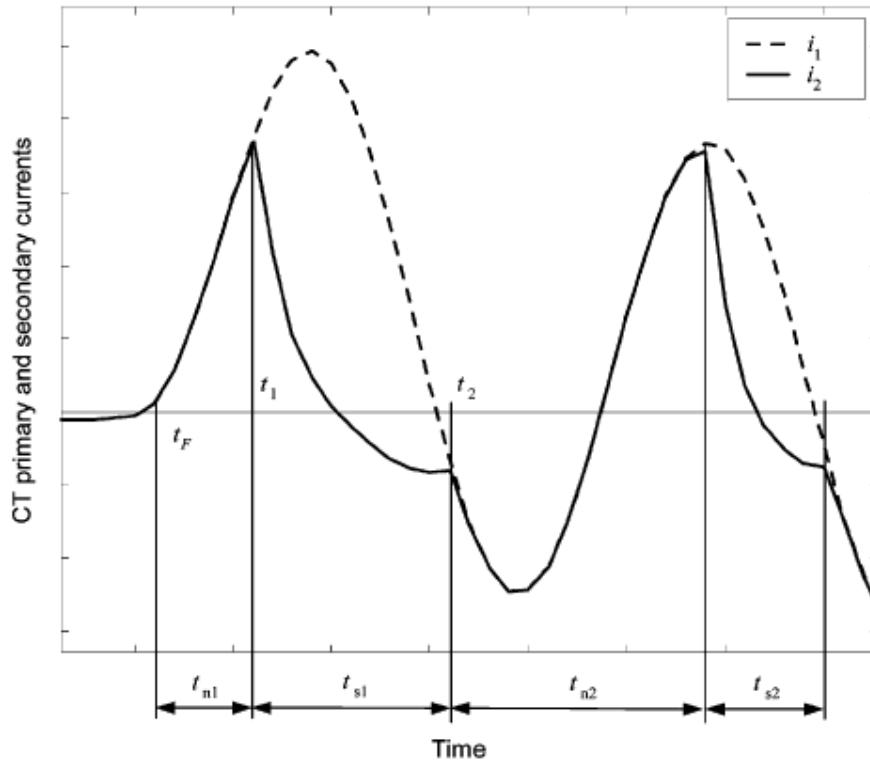
TABLE I

PRIMARY CURRENT AGAINST PRIMARY VOLTAGE. FIRST COLUMN:  
PRIMARY VOLTAGE. SECOND COLUMN: ELECTRONIC COMPENSATION  
CIRCUIT CONNECTED. THIRD COLUMN: WITHOUT COMPENSATION

Voltage (V)	Current with Compensation ( $\mu$ A)	Current without Compensation (mA)
5	3	0.6
10	5	0.9
20	8	1.4
40	17	2.5
70	24	3.8



# Problema de saturación de CTs



# Posibles soluciones

Several approaches may be found in the literature

- determination of CT saturation based on normative recommendations [1] or CT model equations [2];
- detection of CT saturation with the use of algorithmic methods (measurement of certain signal features) (e.g., [3]);
- use of artificial-intelligence techniques [including artificial neural networks (ANNs)] for CT saturation detection and compensation (e.g., [4] and [5]).

[1] *IEEE Guide for the Application of Current Transformers Used for Protective Relaying Purposes, ANSI/IEEE C37.110 Std.*

[2] W. Rebizant, K. Feser, T. Hayder, and L. Schiel, “**Differential relay with adaptation during saturation period of current transformers**,” in *Proc. 14th Power System Protection Conf., Bled, Slovenia, Sep./Oct. 1, 2004*, pp. 124–129.

- [3] Y. Kang, S. Kang, and P. Crossley, “**An algorithm for detecting CT saturation using the secondary current third-derivative function**,” in *Proc. IEEE Bologna PowerTech Conf.*, Jun. 23–26, 2003, pp. 320–326.
- [4] M. M. Saha, J. Izykowski, M. Lukowicz, and E. Rosolowski, “**Application of ANN methods for instrument transformer correction in transmission line protection**,” in *Proc. 7th Int. Conf. Developments in Power System Protection, Amsterdam, The Netherlands*, Apr. 9–12, 2001, pp. 303–306.
- [5] W. Rebizant and D. Bejmert, “**Current transformer saturation detection with genetically optimized neural networks**,” presented at the IEEE PowerTech Conf., St. Petersburg, Russia, Jun. 27–30, 2005, paper 220.
- [6] Y. C. Kang, U. J. Lim, S. H. Kang, and P. A. Crossley, “**Compensation of the distortion in the secondary current caused by saturation and remanence in a CT**,” *IEEE Trans. Power Del.*, vol. 19, no. 4, pp. 1642–1649, Oct. 2004.
- [7] F. M. Arguelles, M. A. Z. Arrieta, J. L. Dominiques, B. L. Jaurrieta, and M. S. Benito, “**A new method for dc offset removal for digital protective relays**,” *Elect. Power Syst. Res.*, vol. 76, pp. 194–199, 2006.

# Estimación de momento de saturación y predicción

## II. DETERMINATION OF THE INSTANT OF SATURATION

The time of saturation may be determined by means of comparison of the predicted (estimated) value of the current sample and the real sample of the secondary current. If the secondary current sample  $i_2(n)$  is substantially smaller than the estimated value of the current  $i_{2e}(n)$ , then one may conclude that the saturation took place some time between the samples  $(n - 1)$  and  $(n)$  (see Fig. 2).

To predict the sample  $i_{2e}(n)$ , which is unknown, one has to use previous samples taken during the undistorted section. The simplest and, at the same time, least accurate method of estimation is based on the assumption that during the time between the samples  $(n - 1)$  and  $(n)$ , the first derivative of the primary current is the same as in the previous sampling period between the samples  $(n - 2)$  and  $(n - 1)$ . This leads to the formula (see Appendix)

$$i_{2e}(n) = 2 * i_2(n - 1) - i_2(n - 2). \quad (1)$$

Fin